

Chiral Phonons Arising from Chirality-Selective Magnon-Phonon Coupling

Markus Weißenhofer^{1,2,*} Philipp Rieger^{1,3} M. S. Mrudul¹ Luca Mikadze¹

Ulrich Nowak³ and Peter M. Oppeneer¹

¹*Department of Physics and Astronomy, Uppsala University, P.O. Box 516, S-751 20 Uppsala, Sweden*

²*Department of Physics, Freie Universität Berlin, Arnimallee 14, D-14195 Berlin, Germany*

³*Department of Physics, University of Konstanz, DE-78457 Konstanz, Germany*



(Received 8 November 2024; revised 25 August 2025; accepted 30 October 2025; published 17 November 2025)

Chiral phonons are desirable for applications in spintronics but their generation and control remains a challenge. Here we demonstrate the emergence of truly chiral phonons from selective magnon-phonon coupling in inversion-symmetric magnetic systems. Considering bcc Fe as an example, we quantitatively calculate hybridized magnon-phonon quasiparticle states across the entire Brillouin zone utilizing first-principles calculations. Our findings challenge conventional magnetoelastic interpretations and reveal finite zero-point phonon angular momentum and strong anomalous thermal Hall responses linked to finite (spin) Berry curvatures. Our results further establish that the existence of chiral phonons, particularly along high-symmetry directions, is common in many magnetic materials, offering promising avenues for novel spintronic and phononic devices.

DOI: 10.1103/j7bs-2zbx

Introduction—Chirality, which denotes the asymmetry between a structure and its mirror image, is one of the fundamental properties of matter [1]. In condensed matter physics, it plays a crucial role in the properties of fermionic and bosonic (quasi)particles, such as electrons [2,3], magnons [4–8], and phonons [9–12].

Recent theoretical predictions [9,13] and experimental observations in two-dimensional materials [10] have identified phonon modes with finite angular momentum at high-symmetry points of the Brillouin zone (BZ), arising from the circular (or elliptical) orbital motions of atoms around their equilibrium lattice positions [11,14]. Such phonon angular momentum plays a crucial role in a wide variety of effects ranging from the phonon Hall effect [15–18], the ultrafast Einstein–de Haas [19,20] and Barnett effects [21,22], magnon-phonon conversion [23], to phonon magnetic moments [11,24–26].

While it has become common to refer to all phonons with finite angular momentum $\mathbf{L}$ as chiral [9,13], symmetry arguments suggest that nonpropagating phonons and those propagating in the rotation plane do not possess true chiral character [27,28]. To unambiguously define *truly* chiral phonons [29,30], we introduce the phonon chirality parameter $\Sigma = \mathbf{L} \cdot \mathbf{v}/|\mathbf{v}|$, where $\mathbf{v}$ is the group velocity, based on the

considerations presented in Ref. [28]. Truly chiral phonons are characterized by a finite Σ and have recently been experimentally detected in systems *lacking* inversion ($\mathcal{P}$) symmetry by means of x-ray and Raman spectroscopy [28,31,32], transport [33,34], and torque measurements [35].

Here, we present fully quantitative, first-principles-based calculations to demonstrate the emergence of truly chiral phonons in the $\mathcal{P}$ -symmetric ferromagnetic material bcc Fe as a result of phonon-chirality-selective magnon-phonon coupling. This coupling breaks time-reversal symmetry for the phonons and is derived from a recently developed framework describing the interaction between lattice and magnetic degrees of freedom [36,37]. We further calculate a finite zero-point angular momentum [14] and intrinsic anomalous Hall responses of the coupled magnon-phonon quasiparticles.

Phonon angular momentum—Following Ref. [14], the angular momentum of the phononic system is given by

$$\mathbf{L} = \sum_{\mathbf{k}\lambda} \mathbf{L}_{\mathbf{k}\lambda} \left(n_{\mathbf{k}\lambda} + \frac{1}{2} \right), \quad \mathbf{L}_{\mathbf{k}\lambda} = \sum_{\mu} 2\hbar \text{Re}[\chi_{\mathbf{k}\lambda}^{(\mu)}] \times \text{Im}[\chi_{\mathbf{k}\lambda}^{(\mu)}], \quad (1)$$

where $n_{\mathbf{k}\lambda}$ is the phonon occupation number and the sums are over all phonon branches λ and wave vectors $\mathbf{k}$ in the first BZ, and over all atoms μ in the unit cell [see Supplemental Material (SM) [38] for details]. In the absence of relativistic effects, the phonon frequencies $\omega_{\mathbf{k}\lambda}$ and polarization vectors $\chi_{\mathbf{k}\lambda} = \{\chi_{\mathbf{k}\lambda}^{(\mu)}\}$ are obtained from solving the eigenvalue problem $\mathcal{D}_{\mathbf{k}} \chi_{\mathbf{k}\lambda} = \omega_{\mathbf{k}\lambda}^2 \chi_{\mathbf{k}\lambda}$ for the dynamical matrix $\mathcal{D}_{\mathbf{k}}$ [14]. In inversion-symmetric systems,

*Contact author: markus.weissenhofer@fu-berlin.de

Published by the American Physical Society under the terms of the [Creative Commons Attribution 4.0 International license](#). Further distribution of this work must maintain attribution to the author(s) and the published article's title, journal citation, and DOI. Funded by [Bibsam](#).

to which we will restrict the discussion throughout the Letter, $\mathcal{D}_k$ is real, and hence one can always choose $\chi_{k\lambda} = e^{i\varphi_{k\lambda}} \mathbf{e}_{k\lambda}$, with $\mathbf{e}_{k\lambda}$ being real and $\varphi_{k\lambda}$ an arbitrary phase. We call these phonon modes *linear* (short for linearly polarized), as the associated dynamics of atoms are restricted to the one-dimensional space spanned by $\mathbf{e}_{k\lambda}$. As such, the angular momentum $\mathbf{L}_{k\lambda}$ of all linear phonon modes trivially vanishes.

At a generic nonsymmetric point of the Brillouin zone, all phonon frequencies are different and the associated eigenvectors are unique (up to a phase). Consequently, all phonon modes at such points are linear and must have zero angular momentum, irrespective of representation. However, if two (or more) eigenvalues of the dynamical matrix coincide—e.g., at high-symmetry points, lines, or planes—the eigenspace associated with this particular eigenvalue is two (or higher) dimensional. Considering, e.g., two degenerate transverse phonon modes at some finite $\mathbf{k}$ and $\mathbf{v} \parallel \mathbf{k}$, the corresponding eigenspace can be spanned by two real and orthonormal vectors $\mathbf{e}_{k1}$ and $\mathbf{e}_{k2}$. They represent linear modes that can be superimposed to form left- and right-handed circular phonon modes, $\chi_{k1} = (\mathbf{e}_{k1} + i\mathbf{e}_{k2})/\sqrt{2}$ and $\chi_{k2} = (\mathbf{e}_{k1} - i\mathbf{e}_{k2})/\sqrt{2}$. These modes correspond to the same eigenvalue as the linear modes, but they have a finite phonon chirality $\Sigma = \pm\hbar$, thus representing chiral phonon modes.

While high-symmetry regions with degenerate phonon energies are certainly interesting from a fundamental perspective, they typically have little relevance for physical effects, as they occupy regions of the BZ with virtually no volume [39]. However, this changes when considering the impact of spin-lattice coupling (SLC) on the phonon band structure. This coupling can bridge the energy gap between two linear phonon modes, enabling them to couple and form a chiral phonon mode. Since SLC is generally a small correction to phonon energies [40], we expect chiral phonons in inversion-symmetric systems to only emerge in regions close to degenerate points, lines, and planes of the *bare* phonon spectrum [41]. This conjecture is demonstrated below, through fully quantitative calculations for the simple monatomic ferromagnet bcc Fe, which serves here as an example. The concepts can be readily applied to any other $\mathcal{P}$ -symmetric magnetic system.

Magnon-phonon coupling—To describe the coupling of spin and lattice degrees of freedom (d.o.f.) we adopt an atomistic approach. We start with the expansion of a phenomenological spin-lattice Hamiltonian up to the third order in d.o.f.,

$$\begin{aligned} \hat{\mathcal{H}}_{\text{SLC}} = & \sum_i \frac{\hat{\mathbf{p}}_i^2}{2m_i} + \sum_{ij,\alpha\beta} \left(\Phi_{ij}^{\alpha\beta} \hat{\mathbf{X}}_i^\alpha \hat{\mathbf{X}}_j^\beta + J_{ij}^{\alpha\beta} \hat{\mathbf{S}}_i^\alpha \hat{\mathbf{S}}_j^\beta \right) \\ & + \sum_{ijk,\alpha\beta\gamma} \left(J_{ijk}^{\alpha\beta\gamma} \hat{\mathbf{S}}_i^\alpha \hat{\mathbf{S}}_j^\beta \hat{\mathbf{X}}_k^\gamma + G_{ijk}^{\alpha\beta\gamma} \hat{\mathbf{S}}_i^\alpha \hat{\mathbf{X}}_j^\beta \hat{\mathbf{P}}_k^\gamma \right), \end{aligned} \quad (2)$$

keeping all terms compatible with inversion and (global) time-reversal symmetry. Here, $\hat{\mathbf{S}}_i^\alpha$ are vector spin operators at the site i with amplitude $|\hat{\mathbf{S}}_i| = S$, and $\hat{\mathbf{X}}_i^\alpha$ and $\hat{\mathbf{P}}_i^\alpha$ are nuclear displacement and momentum operators, respectively. The first three terms of $\hat{\mathcal{H}}_{\text{SLC}}$ are the kinetic energy of the atoms (of mass m_i), the lattice potential (with the force constants $\Phi_{ij}^{\alpha\beta}$ being proportional to the Fourier transform of the dynamical matrix $\mathcal{D}_k^{\alpha\beta}$ [38]), and the generalized Heisenberg interaction [42], where the $J_{ij}^{\alpha\beta}$ also includes magneto-crystalline anisotropy (MCA). The anti-symmetric Dzyaloshinskii-Moriya interaction (DMI) is forbidden for pairs (i, j) whose midpoint is an inversion center.

Coupling between spin and lattice d.o.f. arises from the last two terms of $\hat{\mathcal{H}}_{\text{SLC}}$. The term quadratic in spins and linear in displacements was recently introduced by Hellsvik *et al.* [36], and since then efficient methods to calculate all $J_{ijk}^{\alpha\beta\gamma}$ parameters from first principles have been established [37,43–45].

The last term has gained little attention in the general form expressed here. Particularly, efficient methods to calculate the full set of $G_{ijk}^{\alpha\beta\gamma}$ parameters from first principles are yet to be established. Instead, studies so far mainly investigated two special cases of this term: (i) a purely local term $\sim \sum_i \hat{\mathbf{S}}_i \cdot (\hat{\mathbf{X}}_i \times \hat{\mathbf{P}}_i)$ was used in a semiclassical description of atomic motion in the effective field of the spin [11,21,46], and (ii) a term obtained by fixing the spin orientation, $\sum_{jk,\beta\gamma} G_{jk}^{\beta\gamma} \hat{\mathbf{X}}_j^\beta \hat{\mathbf{P}}_k^\gamma$, that appears, e.g., in the Born-Huang approximation [39,40,47–49].

Magnon and phonon variables can be introduced via the Holstein-Primakoff transformation [50] and normal mode expansion (details in SM [38]). For a monoatomic system and expanding around a ferromagnetic state along z , the magnon-phonon Hamiltonian up to second order in magnon ($\hat{b}_k^{(\dagger)}$) and phonon operators ($\hat{a}_{k,\lambda}^{(\dagger)}$) reads $\hat{\mathcal{H}}_{\text{mp}} = \sum_k \hat{\mathcal{H}}_k$, with

$$\begin{aligned} \hat{\mathcal{H}}_k = & \sum_\lambda \hbar \omega_{k\lambda} \hat{a}_{k\lambda}^\dagger \hat{a}_{k\lambda} + \varepsilon_k \hat{b}_k^\dagger \hat{b}_k \\ & + \sum_\lambda (c_{k\lambda}^- \hat{b}_{-k} + c_{k\lambda}^+ \hat{b}_k^\dagger) (\hat{a}_{k\lambda} + \hat{a}_{-k\lambda}^\dagger) \\ & + \sum_{\lambda\lambda'} g_{k\lambda\lambda'} (\hat{a}_{k\lambda} + \hat{a}_{-k\lambda}^\dagger) (\hat{a}_{-k\lambda'} - \hat{a}_{k\lambda'}^\dagger). \end{aligned} \quad (3)$$

Here, ε_k are the bare magnon energies and zero-point energies have been dropped. The magnon-phonon couplings $c_{k\lambda}^\pm = \sum_\gamma \sqrt{\hbar S^3 / m \omega_{k\lambda}} (\tilde{J}_k^{xzy} \pm i \tilde{J}_k^{yzx}) \chi_{k\lambda}^\gamma$ and phonon-phonon couplings $g_{k\lambda\lambda'} = -(i/2) \hbar S \sqrt{\omega_{k\lambda} / \omega_{k\lambda'}} \sum_\gamma \tilde{G}_k^{z\beta\gamma} \chi_{k\lambda}^\beta (\chi_{k\lambda'}^\gamma)^*$ depend on the Fourier transforms $\tilde{J}_k^{\alpha\beta\gamma} = \sum_{jk} e^{ik \cdot (r_j - r_k)} J_{ijk}^{\alpha\beta\gamma}$ and $\tilde{G}_k^{\alpha\beta\gamma} = \sum_{jk} e^{ik \cdot (r_j - r_k)} G_{ijk}^{\alpha\beta\gamma}$ of the coefficients of the third order terms in Eq. (2). They are relativistic corrections to the

bare modes and proportional to spin-orbit coupling [37,40]. The emergence of chiral phonons has been previously linked to the phonon-phonon coupling term proportional to $g_{k\lambda\lambda'}$ [14,39,49]. Hereinafter we will omit the phonon-phonon coupling $g_{k\lambda\lambda'}$ and instead focus on the magnon-phonon coupling $c_{k\lambda}^{\pm}$. We show that magnon-phonon coupling can give rise to truly chiral phonons in bcc Fe.

For this purpose we use $J_{ijk}^{\alpha\beta\gamma}$ coefficients that were recently calculated from first principles [37]. The bare magnon energies follow $\epsilon_k = S(2d + 2 \sum_j J_{ij} [1 - e^{-ik \cdot (r_j - r_i)}])$, where the isotropic exchange constants $J_{ij} = \frac{1}{3} \sum_{\alpha} J_{ij}^{\alpha\alpha}$ are also taken from first-principles calculations [51] and the MCA energy d is from experiments [52]. The bare phonon frequencies and polarization vectors are calculated using the density-functional perturbation theory implementation of Quantum ESPRESSO [53,54]. Both the bare magnon and phonon band structures are shown in SM [38].

Coupled magnon-phonon band structure—The exact diagonalization of Eq. (3) is performed numerically using Colpa's method [38,55]. The energies of the four bands along different high-symmetry paths in the BZ are shown in Fig. 1, focusing on the regions with greatest modification of the energies compared to the bare modes. The longitudinal acoustic (LA) phonon does not couple to magnons and is thus unaltered by SLC.

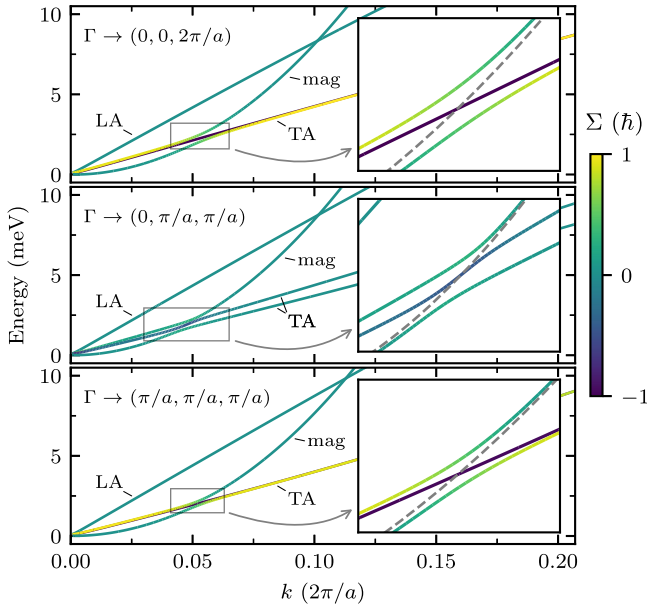


FIG. 1. Coupled magnon-phonon bands in bcc Fe calculated along various high-symmetry paths of the BZ starting from $\Gamma = (0, 0, 0)$. Labels LA, TA, and mag indicate the predominant character of the mode far away from the avoided crossings and the colors encode the phonon chirality $\Sigma = \mathbf{L} \cdot \mathbf{v}/|\mathbf{v}|$, with $\mathbf{v} = \partial\omega/\partial\mathbf{k}$ being the group velocity. The insets are enlargements of the avoided crossings (indicated by the small gray rectangles), and the gray dashed lines are the bare magnon energies. Note that the bare TA modes are degenerate for $\Gamma \rightarrow (0, 0, 2\pi/a)$ and $\Gamma \rightarrow (\pi/a, \pi/a, \pi/a)$.

We observe *avoided crossings* where the bare modes intersect, which indicate the formation of hybrid magnon-phonon quasiparticles, the so-called *magnon polarons* [56]. The energy gaps between the hybridizing modes range from around 0.18 to 0.45 meV. Physically, the magnon-phonon coupling contains an antisymmetric, DMI-like contribution, $c_{k\lambda}^{\pm,a} = \frac{1}{2} \sum_{\gamma} \sqrt{\hbar S^3 / m \omega_{k\lambda}} [(\tilde{J}_k^{xzy} - \tilde{J}_k^{zyx}) \pm i(\tilde{J}_k^{yzx} - \tilde{J}_k^{xzy})] \chi_{k\lambda}^{\gamma}$, and a symmetric, two-site anisotropylike contribution, $c_{k\lambda}^{\pm,s} = \frac{1}{2} \sum_{\gamma} \sqrt{\hbar S^3 / m \omega_{k\lambda}} [(\tilde{J}_k^{xzy} + \tilde{J}_k^{zyx}) \pm i(\tilde{J}_k^{yzx} + \tilde{J}_k^{xzy})] \chi_{k\lambda}^{\gamma}$, both of which are of relativistic origin. In bcc Fe, the DMI-like coupling greatly exceeds the symmetric one [37]. Therefore, the widely used conventional magnetoelastic theory [57] is unable to describe the magnon-phonon dispersion calculated here, as it lacks a term related to DMI. Such a term was only recently derived [58] from the atomistic SLC Hamiltonian (2). In the light of this so-far overlooked DMI-like coupling, established interpretations of magnon-phonon hybridization based on conventional magnetoelastic theory [59–63] have to be reconsidered.

As one key result of this Letter, we find that the magnon mode only hybridizes with one of the TA modes, if the two bare TA phonons are degenerate. In the nondegenerate case, i.e., Γ to $(0, \pi/a, \pi/a)$, there are two avoided crossings with both TA modes in close proximity. Calculating the phonon chirality Σ —which is obtained using the angular momentum eigenvalues of the hybridized system rather than the ones of the bare phonons [38]—for these magnon-phonon modes, we reveal that the magnons selectively couple to phonons with one chirality. We note that upon reversal of the magnetization from z to $-z$, the magnons instead only couple to phonons with opposite chirality. We further emphasize that the magnon-phonon coupling also lifts the degeneracy of the phonons far away from the avoided crossing regions, leading to a small energy gap of the order of 1 μ eV between the two chiral phonon modes. This value is comparable to that predicted from phonon-phonon coupling [39]. However, it remains to be determined whether such a small gap persists when the spectrum is broadened and renormalized by higher-order phonon-phonon or magnon-phonon scattering.

Qualitatively, the selective coupling of magnons to chiral phonons with positive Σ can be understood by noting that both spin precession and atomic revolution occur in the same counterclockwise direction [64]. A more quantitative way to understand this phenomenon is to first express the bare phonons in a circular basis before calculating their hybridization with magnons. This approach is only valid along high-symmetry paths in the BZ where the bare TA phonon modes are degenerate (e.g., the paths shown in the top and bottom panels of Fig. 1). Notably, in this basis, the magnon-phonon coupling $c_{k\lambda}^{\pm}$ for one of the phonon modes, specifically that of circular phonons with $\Sigma = -\hbar$, vanishes exactly. Selective hybridization between magnons and nonpropagating circularly polarized phonons has been

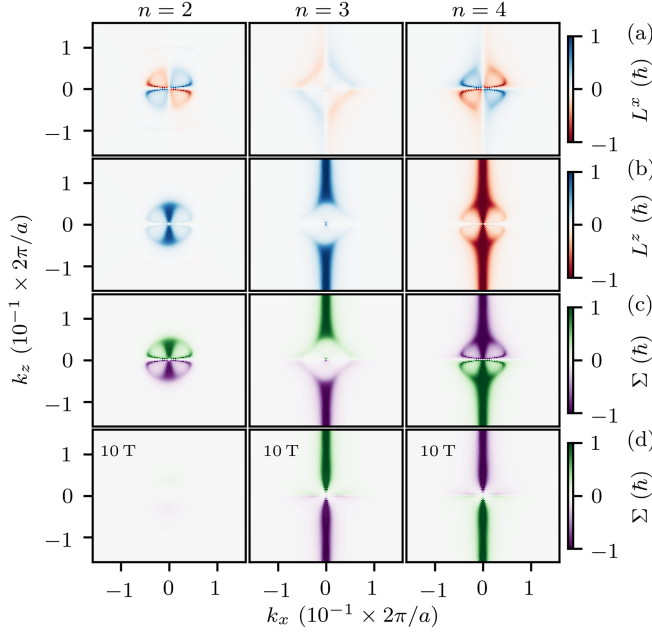


FIG. 2. Phonon angular momenta and chiralities of the coupled magnon-phonon bands computed for bcc Fe. Plots in each row illustrate (a) L^x , (b) L^z , (c) Σ without applied magnetic field, and (d) Σ with a field of $B = 10$ T for the different magnon-phonon modes with label $n \in \{2, 3, 4\}$. The mode with $n = 1$ (LA phonon) is achiral and hence not shown. L^y is zero in the k_x - k_z plane depicted here.

measured recently in the layered zigzag antiferromagnet FePSe₃ [65].

The phonon angular momentum and chirality in the k_x - k_z plane of the BZ are shown in Fig. 2 (results for other planes are discussed in SM [38]). As argued above, truly chiral phonons primarily occur in close proximity of the high-symmetry axes—here, the k_z axis—where they arise as a superposition of the degenerate bare TA phonons. Note that phonons along k_x and k_y remain linear. This symmetry breaking arises from the orientation of magnetization along the z direction in combination with spin-orbit coupling [66].

The emergence of chiral phonons in a roughly circular pattern around the Γ point [see Figs. 2(a) and 2(b)] is a result of magnon-phonon hybridization. This can be demonstrated by applying an external magnetic field in the direction of the magnetization. A magnetic field B shifts the bare magnon energies by $\epsilon_k \rightarrow \epsilon_k + \mu_s B$, with $\mu_s = 2.2 \mu_B$ being the saturation magnetic moment of bcc Fe [67]. For field strengths of $B = 10$ T the energies of the bare magnons are way above those of the TA phonons [68], making avoided crossings impossible and confining the chiral phonons to the vicinity of the k_z direction; see Fig. 2(d). This proves that magnon-phonon coupling can induce chiral phonons without direct hybridization with magnons, i.e., if their energies are very different.

Next, we calculate the equilibrium phonon angular momentum for bcc Fe via Eq. (1); see Fig. 3. In thermal

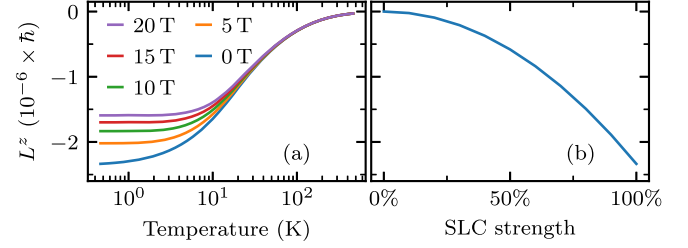


FIG. 3. Nonzero component L_z of the equilibrium phonon angular momentum per unit cell for bcc Fe, shown in (a) versus temperature and for applied magnetic fields as labeled and in (b) versus rescaled SLC strength.

equilibrium the occupation numbers of a magnon-phonon state with energy ϵ_{kn} follow the Bose-Einstein distribution, $n_{kn} = 1/(e^{\epsilon_{kn}/k_B T} - 1)$. The scaling of the equilibrium phonon angular momentum with temperature T is shown in Fig. 3(a). We find that the system has a small, but finite zero-point angular momentum $L(T \rightarrow 0) = \sum_{kn} \frac{1}{2} L_{kn}$ [14], because the angular momenta of the different modes do not fully cancel. This is a result of the nonunitary nature of the Bogoliubov-Valatin transformation applied within Colpa's method [38]. Moreover, it is observed that the equilibrium phonon angular momentum vanishes in the limit of high temperatures. It can be proven analytically that $L(T \rightarrow \infty) = 0$ is true for all inversion-symmetric systems with magnon-phonon coupling [38].

By changing the applied magnetic field we can eliminate the impact of BZ regions with avoided crossings on L , revealing the dominant role of chiral phonons without substantial hybridization with magnons in the high-temperature limit. To further elucidate the concept of zero-point angular momentum, we vary the strength of SLC from 0% to 100% [Fig. 3(b)]. This scaling highlights that the angular momentum arises solely from relativistic effects, emphasizing the intrinsic link between spin-orbit coupling and the observed zero-point contributions.

Intrinsic anomalous Hall responses—Nontrivial (spin) Berry curvature arising due to magnon-polaron formation can lead to the emergence of Hall-type quantum transport phenomena of heat and spin angular momentum, manifested in thermal Hall and spin Nernst effects [69–71]. The Berry curvature of the n th band can be obtained by casting the Hamiltonian in a Bogoliubov-de Gennes form [72], which gives

$$\Omega_{\mu\nu}^n(\mathbf{k}) = 2i\hbar^2 \sum_{m \neq n}^{2N_b} g_{nn} g_{mm} \frac{\langle n_k | \hat{v}_\mu | m_k \rangle \langle m_k | \hat{v}_\nu | n_k \rangle}{[(g\mathcal{E}_k)_{nn} - (g\mathcal{E}_k)_{mm}]^2}, \quad (4)$$

where $|n_k\rangle$ is an eigenstate of $\hat{\mathcal{H}}_k$, N_b is the number of magnon-phonon bands, $\mathcal{E}_k = \text{diag}(\epsilon_{k1}, \dots, \epsilon_{kN_b}, \epsilon_{-k1}, \dots, \epsilon_{-kN_b})$ is a matrix containing the eigenenergies, $\hat{\mathbf{v}} = \hbar^{-1} \partial_{\mathbf{k}} \hat{\mathcal{H}}_k$ is the velocity operator, and $g = \sigma_z \otimes \mathbb{1}_{N_d \times N_d}$,

with σ_z being the z component of the Pauli matrices and $\mathbb{1}_{N_b \times N_b}$ the unit matrix of dimension N_b . For details, see Ref. [70].

Hereinafter, we consider an ultrathin, quasi-two-dimensional layer of bcc Fe by restricting the $\mathbf{k}$ values to a plane through the BZ that includes Γ . Integrating the Berry curvature of the n th band over such plane yields the respective first Chern number C_n . For example, for the k_x - k_y plane it reads $C_n = (1/2\pi) \int dk_x dk_y \Omega_{xy}^n(\mathbf{k})$. Even though we obtain finite Berry curvatures as a result of time-reversal symmetry breaking via the SLC, Chern numbers of the magnon-phonon bands are zero; i.e., the band structure is topologically trivial [73]. This is because there are two topological gaps, one at the aforementioned avoided crossing region and a second one close to Γ , with an opposite sign of Berry curvature. Note that for calculating the Chern numbers, we apply a small magnetic field of $B \geq 0.5$ T to broaden the Berry curvature close to Γ and converge the computations with reasonable numerical effort.

The anomalous magnon-phonon thermal Hall conductivity $\kappa_{\mu\nu}$ and the spin Nernst coefficient $\alpha_{\mu\nu}^{S_\tau}$, respectively, relate a transverse heat current and a transverse spin current to an applied temperature gradient, expressed as $J_\mu = -\sum_\nu \kappa_{\mu\nu} \partial_\nu T$ and $J_\mu^{S_\tau} = -\sum_\nu \alpha_{\mu\nu}^{S_\tau} \partial_\nu T$. Within linear response theory, $\kappa_{\mu\nu}$ is related to the Berry curvature via [74–77]

$$\kappa_{\mu\nu} = -\frac{k_B^2 T}{\hbar \mathcal{A}} \sum_{\mathbf{k}} \sum_{n=1}^{N_b} c_2(n_{kn}) \Omega_{\mu\nu}^n(\mathbf{k}), \quad (5)$$

where $\mathcal{A}$ is the area of the system and $c_2(x) = (1+x)[\ln((1+x)/x)]^2 - (\ln x)^2 - 2\text{Li}_2(-x)$, with $\text{Li}_2(x)$ being the second order polylogarithm function. Similarly, the spin Nernst coefficient $\alpha_{\mu\nu}^{S_\tau}$ can be obtained from the spin Berry curvature $\Omega_{\mu\nu}^{S_\tau, n}(\mathbf{k})$ via [69,78,79]

$$\alpha_{\mu\nu}^{S_\tau} = -\frac{2k_B}{\mathcal{A}} \sum_{\mathbf{k}} \sum_{n=1}^{N_b} c_1(n_{kn}) \Omega_{\mu\nu}^{S_\tau, n}(\mathbf{k}), \quad (6)$$

$$\Omega_{\mu\nu}^{S_\tau, n}(\mathbf{k}) = 2i\hbar^2 \sum_{m \neq n}^{2N_b} g_{nn} g_{mm} \frac{\langle n_{\mathbf{k}} | \hat{J}_\mu^{S_\tau} | m_{\mathbf{k}} \rangle \langle m_{\mathbf{k}} | \hat{v}_\nu | n_{\mathbf{k}} \rangle}{[(g\mathcal{E}_{\mathbf{k}})_{nn} - (g\mathcal{E}_{\mathbf{k}})_{mm}]^2}, \quad (7)$$

with $c_1(x) = (1+x)\ln(1+x) - x\ln x$, and $\hat{J}_\mu^{S_\tau} = \frac{1}{4} \{\hat{v}_\mu, g\hat{S}_\tau\}$.

Both anomalous transport coefficients, calculated for an ultrathin Fe(001) film by summing $\mathbf{k}$ over the k_x - k_y plane, are shown in Fig. 4. They turn out to be significantly larger than what has been calculated previously for magnon-polaron bands in honeycomb ferromagnets [70] and ferromagnets [69]. This is because in bcc Fe the magnon-phonon modes with finite (spin) Berry curvature have rather low energies, thus contributing strongly to transport. By varying the applied magnetic field, we further demonstrate the tunability of κ_{xy} and $\alpha_{xy}^{S_\tau}$. As mentioned earlier,

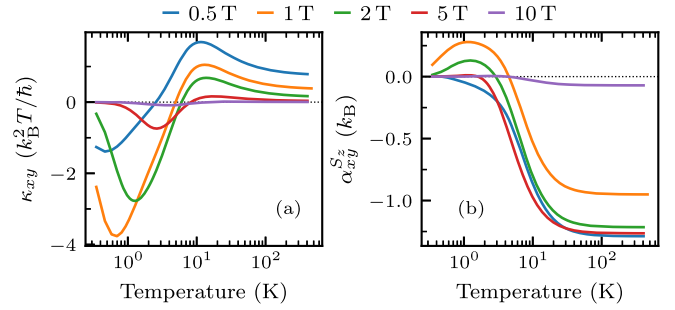


FIG. 4. Anomalous thermal Hall conductivity (a) and spin Nernst coefficient (b) due to magnon-polarons in an ultrathin Fe (001) film. The magnetization is in out-of-plane direction and a magnetic field with values as labeled is applied in the same direction.

strong applied fields suppress the hybridization of magnons and phonons by shifting the bare magnon energies above those of the transverse acoustic TA phonons. This underscores that the emergence of intrinsic anomalous Hall responses is fundamentally linked to the formation of magnon-polaron hybrid bands.

Conclusions—We have demonstrated the existence of truly chiral phonons arising from chirality-selective magnon-phonon coupling in inversion-symmetric magnetic systems. Our first-principles-based approach provides a robust, quantitative framework for understanding the hybridized magnon-phonon quasiparticle states across the entire BZ. Given that magnon-phonon coupling in bcc Fe is primarily influenced by a DMI-like term, we conclude that previous interpretations of magnon-phonon hybridization based on conventional magnetoelastic theory, which does not account for such a term, must be reconsidered. We further reveal the existence of a finite zero-point phonon angular momentum—an entirely quantum mechanical phenomenon without classical counterpart—emerging from the intricate coupling between phononic zero-point fluctuations and those of the spin angular momenta. Additionally, we observe strong and tunable anomalous Hall responses arising from finite (spin) Berry curvatures associated with magnon-phonon hybridization.

Our results imply that the existence of truly chiral phonons along high-symmetry directions, featuring at least two degenerate bare phonon modes, is an abundant characteristic in many magnetic materials. Since the ability to control and utilize these chiral phonons opens new avenues for transporting angular momentum and manipulating magnetic order, this finding will certainly prove useful in the search for potential material candidates for novel spintronic or phononic devices.

Acknowledgments—M. W. and P. M. O. acknowledge support from the German Research Foundation (Deutsche Forschungsgemeinschaft) through CRC/TRR 227 “Ultrafast Spin Dynamics” (Project MF, Project ID No. 328545488). M. W. and M. S. M. thank José Ángel

Castellanos-Reyes for stimulating discussions. U. N. acknowledges support from the Germany Research Foundation through CRC 1432 (Project No. 425217212) and the RU ChiPS (Project No. 541503763). This work has furthermore been supported by the Swedish Research Council (VR), the Knut and Alice Wallenberg Foundation (Grants No. 2022.0079 and No. 2023.0336), and by the EIC Pathfinder OPEN Grant No. 101129641 (OBELIX). The calculations were enabled by resources provided by the National Academic Infrastructure for Supercomputing in Sweden (NAISS) at NSC Linköping partially funded by the Swedish Research Council through Grant Agreement No. 2022-06725.

- [1] R. S. Cahn, C. Ingold, and V. Prelog, Specification of molecular chirality, *Angew. Chem., Int. Ed. Engl.* **5**, 385 (1966).
- [2] S.-Y. Xu *et al.*, Discovery of a Weyl fermion semimetal and topological Fermi arcs, *Science* **349**, 613 (2015).
- [3] G. Chang, B. J. Wieder, F. Schindler, D. S. Sanchez, I. Belopolski, S.-M. Huang, B. Singh, D. Wu, T.-R. Chang, T. Neupert, S.-Y. Xu, H. Lin, and M. Z. Hasan, Topological quantum properties of chiral crystals, *Nat. Mater.* **17**, 978 (2018).
- [4] B. Roessli, P. Böni, W. E. Fischer, and Y. Endoh, Chiral fluctuations in MnSi above the Curie temperature, *Phys. Rev. Lett.* **88**, 237204 (2002).
- [5] R. Lebrun, A. Ross, S. A. Bender, A. Qaiumzadeh, L. Baldrati, J. Cramer, A. Brataas, R. A. Duine, and M. Kläui, Tunable long-distance spin transport in a crystalline antiferromagnetic iron oxide, *Nature (London)* **561**, 222 (2018).
- [6] Y. Nambu, J. Barker, Y. Okino, T. Kikkawa, Y. Shiomi, M. Enderle, T. Weber, B. Winn, M. Graves-Brook, J. M. Tranquada, T. Ziman, M. Fujita, G. E. W. Bauer, E. Saitoh, and K. Kakurai, Observation of magnon polarization, *Phys. Rev. Lett.* **125**, 027201 (2020).
- [7] Y. Liu, Z. Xu, L. Liu, K. Zhang, Y. Meng, Y. Sun, P. Gao, H.-W. Zhao, Q. Niu, and J. Li, Switching magnon chirality in artificial ferrimagnet, *Nat. Commun.* **13**, 1264 (2022).
- [8] L. Šmejkal, A. Marmodoro, K.-H. Ahn, R. González-Hernández, I. Turek, S. Mankovsky, H. Ebert, S. W. D'Souza, O. Šipr, J. Sinova, and T. Jungwirth, Chiral magnons in antiferromagnetic RuO₂, *Phys. Rev. Lett.* **131**, 256703 (2023).
- [9] L. Zhang and Q. Niu, Chiral phonons at high-symmetry points in monolayer hexagonal lattices, *Phys. Rev. Lett.* **115**, 115502 (2015).
- [10] H. Zhu, J. Yi, M.-Y. Li, J. Xiao, L. Zhang, C.-W. Yang, R. A. Kaindl, L.-J. Li, Y. Wang, and X. Zhang, Observation of chiral phonons, *Science* **359**, 579 (2018).
- [11] D. M. Juraschek and N. A. Spaldin, Orbital magnetic moments of phonons, *Phys. Rev. Mater.* **3**, 064405 (2019).
- [12] T. Wang, H. Sun, X. Li, and L. Zhang, Chiral phonons: Prediction, verification, and application, *Nano Lett.* **24**, 4311 (2024).
- [13] H. Chen, W. Zhang, Q. Niu, and L. Zhang, Chiral phonons in two-dimensional materials, *2D Mater.* **6**, 012002 (2018).
- [14] L. Zhang and Q. Niu, Angular momentum of phonons and the Einstein-de Haas effect, *Phys. Rev. Lett.* **112**, 085503 (2014).
- [15] C. Strohm, G. L. J. A. Rikken, and P. Wyder, Phenomenological evidence for the phonon Hall effect, *Phys. Rev. Lett.* **95**, 155901 (2005).
- [16] G. Grissonnanche, S. Thériault, A. Gourgout, M.-E. Boulanger, E. Lefrançois, A. Ataei, F. Laliberté, M. Dion, J.-S. Zhou, S. Pyon, T. Takayama, H. Takagi, N. Doiron-Leyraud, and L. Taillefer, Chiral phonons in the pseudogap phase of cuprates, *Nat. Phys.* **16**, 1108 (2020).
- [17] S. Park and B.-J. Yang, Phonon angular momentum Hall effect, *Nano Lett.* **20**, 7694 (2020).
- [18] B. Flebus and A. H. MacDonald, Phonon Hall viscosity of ionic crystals, *Phys. Rev. Lett.* **131**, 236301 (2023).
- [19] C. Dornes *et al.*, The ultrafast Einstein-de Haas effect, *Nature (London)* **565**, 209 (2019).
- [20] S. R. Tauchert, M. Volkov, D. Ehberger, D. Kazenwadel, M. Evers, H. Lange, A. Donges, A. Book, W. Kreuzpaintner, U. Nowak, and P. Baum, Polarized phonons carry angular momentum in ultrafast demagnetization, *Nature (London)* **602**, 73 (2022).
- [21] J. Luo, T. Lin, J. Zhang, X. Chen, E. R. Blackert, R. Xu, B. I. Yakobson, and H. Zhu, Large effective magnetic fields from chiral phonons in rare-earth halides, *Science* **382**, 698 (2023).
- [22] C. S. Davies, F. G. N. Fennema, A. Tsukamoto, I. Razdolski, A. V. Kimel, and A. Kirilyuk, Phononic switching of magnetization by the ultrafast Barnett effect, *Nature (London)* **628**, 540 (2024).
- [23] J. Holanda, D. S. Maior, A. Azevedo, and S. M. Rezende, Detecting the phonon spin in magnon-phonon conversion experiments, *Nat. Phys.* **14**, 500 (2018).
- [24] D. M. Juraschek, M. Fechner, A. V. Balatsky, and N. A. Spaldin, Dynamical multiferroicity, *Phys. Rev. Mater.* **1**, 014401 (2017).
- [25] Y. Ren, C. Xiao, D. Saporov, and Q. Niu, Phonon magnetic moment from electronic topological magnetization, *Phys. Rev. Lett.* **127**, 186403 (2021).
- [26] M. Basini, M. Pancaldi, B. Wehinger, M. Udina, V. Unikandanunni, T. Tadano, M. C. Hoffmann, A. V. Balatsky, and S. Bonetti, Terahertz electric-field-driven dynamical multiferroicity in SrTiO₃, *Nature (London)* **628**, 534 (2024).
- [27] S.-W. Cheong and X. Xu, Magnetic chirality, *npj Quantum Mater.* **7**, 40 (2022).
- [28] H. Ueda, M. García-Fernández, S. Agrestini, C. P. Romao, J. van den Brink, N. A. Spaldin, K.-J. Zhou, and U. Staub, Chiral phonons in quartz probed by x-rays, *Nature (London)* **618**, 946 (2023).
- [29] L. D. Barron, *Molecular Light Scattering and Optical Activity*, 2nd ed. (Cambridge University Press, Cambridge, England, 2004).
- [30] D. M. Juraschek *et al.*, Chiral phonons, *Nat. Phys.* **21**, 1532 (2025).
- [31] K. Ishito, H. Mao, Y. Kousaka, Y. Togawa, S. Iwasaki, T. Zhang, S. Murakami, J.-i. Kishine, and T. Satoh, Truly chiral phonons in α -HgS, *Nat. Phys.* **19**, 35 (2023).
- [32] K. Ishito, H. Mao, K. Kobayashi, Y. Kousaka, Y. Togawa, H. Kusunose, J.-i. Kishine, and T. Satoh, Chiral

- phonons: Circularly polarized Raman spectroscopy and *ab initio* calculations in a chiral crystal tellurium, *Chirality* **35**, 338 (2023).
- [33] K. Kim, E. Vetter, L. Yan, C. Yang, Z. Wang, R. Sun, Y. Yang, A. H. Comstock, X. Li, J. Zhou, L. Zhang, W. You, D. Sun, and J. Liu, Chiral-phonon-activated spin Seebeck effect, *Nat. Mater.* **22**, 322 (2023).
- [34] K. Ohe, H. Shishido, M. Kato, S. Utsumi, H. Matsuura, and Y. Togawa, Chirality-induced selectivity of phonon angular momenta in chiral quartz crystals, *Phys. Rev. Lett.* **132**, 056302 (2024).
- [35] H. Zhang, N. Peshcherenko, F. Yang, T. Z. Ward, P. Raghuvarshi, L. Lindsay, C. Felsner, Y. Zhang, J.-Q. Yan, and H. Miao, Measurement of phonon angular momentum, *Nat. Phys.* **21**, 1387 (2025).
- [36] J. Hellsvik, D. Thonig, K. Modin, D. Iușan, A. Bergman, O. Eriksson, L. Bergqvist, and A. Delin, General method for atomistic spin-lattice dynamics with first-principles accuracy, *Phys. Rev. B* **99**, 104302 (2019).
- [37] S. Mankovsky, S. Polesya, H. Lange, M. Weißenhofer, U. Nowak, and H. Ebert, Angular momentum transfer via relativistic spin-lattice coupling from first principles, *Phys. Rev. Lett.* **129**, 067202 (2022).
- [38] See Supplemental Material at <http://link.aps.org/supplemental/10.1103/j7bs-2zbx> for the derivation of the phonon angular momentum and the magnon-phonon Hamiltonian, the bare band structures, the results for phonon angular momentum and chirality in other planes of the BZ, a summary of Colpa's method, and a proof that $L(T \rightarrow \infty) = 0$.
- [39] S. Coh, Classification of materials with phonon angular momentum and microscopic origin of angular momentum, *Phys. Rev. B* **108**, 134307 (2023).
- [40] S. Ren, J. Bonini, M. Stengel, C. E. Dreyer, and D. Vanderbilt, Adiabatic dynamics of coupled spins and phonons in magnetic insulators, *Phys. Rev. X* **14**, 011041 (2024).
- [41] We use the term *bare* modes to describe phonon or magnon modes in the absence of spin-lattice coupling.
- [42] U. Nowak, Classical spin models, in *Handbook of Magnetism and Advanced Magnetic Materials*, edited by H. Kronmüller and S. Parkin (John Wiley & Sons, Ltd, New York, 2007).
- [43] H. Lange, S. Mankovsky, S. Polesya, M. Weißenhofer, U. Nowak, and H. Ebert, Calculating spin-lattice interactions in ferro- and antiferromagnets: The role of symmetry, dimension, and frustration, *Phys. Rev. B* **107**, 115176 (2023).
- [44] S. Mankovsky, H. Lange, S. Polesya, and H. Ebert, Spin-lattice interaction parameters from first principles: Theory and implementation, *Phys. Rev. B* **107**, 144428 (2023).
- [45] I. P. Miranda, M. Pankratova, M. Weißenhofer, A. B. Klautau, D. Thonig, M. Pereiro, E. Sjöqvist, A. Delin, M. I. Katsnelson, O. Eriksson, and A. Bergman, Spin-lattice couplings in 3d ferromagnets: Analysis from first-principles, *Phys. Rev. Mater.* **9**, 024409 (2025).
- [46] T. Kahana, D. A. B. Lopez, and D. M. Juraschek, Light-induced magnetization from magnonic rectification, *Sci. Adv.* **10**, eado0722 (2024).
- [47] C. A. Mead and D. G. Truhlar, On the determination of Born-Oppenheimer nuclear motion wave functions including complications due to conical intersections and identical nuclei, *J. Chem. Phys.* **70**, 2284 (1979).
- [48] M. Born and K. Huang, *Dynamical Theory of Crystal Lattices* (Oxford University Press, New York, 1996), 10.1093/oso/9780192670083.001.0001.
- [49] L. Zhang, J. Ren, J.-S. Wang, and B. Li, The phonon Hall effect: Theory and application, *J. Phys. Condens. Matter* **23**, 305402 (2011).
- [50] T. Holstein and H. Primakoff, Field dependence of the intrinsic domain magnetization of a ferromagnet, *Phys. Rev.* **58**, 1098 (1940).
- [51] O. N. Mryasov, A. J. Freeman, and A. I. Liechtenstein, Theory of non-Heisenberg exchange: Results for localized and itinerant magnets, *J. Appl. Phys.* **79**, 4805 (1996).
- [52] I. Razdolski, A. Alekhin, N. Ilin, J. P. Meyburg, V. Roddatis, D. Diesing, U. Bovensiepen, and A. Melnikov, Nanoscale interface confinement of ultrafast spin transfer torque driving non-uniform spin dynamics, *Nat. Commun.* **8**, 15007 (2017).
- [53] P. Giannozzi *et al.*, Quantum ESPRESSO: A modular and open-source software project for quantum simulations of materials, *J. Phys. Condens. Matter* **21**, 395502 (2009).
- [54] P. Giannozzi *et al.*, Advanced capabilities for materials modelling with Quantum ESPRESSO, *J. Phys. Condens. Matter* **29**, 465901 (2017).
- [55] J. Colpa, Diagonalization of the quadratic boson Hamiltonian, *Physica (Amsterdam)* **93A**, 327 (1978).
- [56] Y. Li, C. Zhao, W. Zhang, A. Hoffmann, and V. Novosad, Advances in coherent coupling between magnons and acoustic phonons, *APL Mater.* **9**, 060902 (2021).
- [57] C. Kittel, Physical theory of ferromagnetic domains, *Rev. Mod. Phys.* **21**, 541 (1949).
- [58] M. Weißenhofer, H. Lange, A. Kamra, S. Mankovsky, S. Polesya, H. Ebert, and U. Nowak, Rotationally invariant formulation of spin-lattice coupling in multiscale modeling, *Phys. Rev. B* **108**, L060404 (2023).
- [59] R. M. White, M. Sparks, and I. Ortenburger, Diagonalization of the antiferromagnetic magnon-phonon interaction, *Phys. Rev.* **139**, A450 (1965).
- [60] A. Rückriegel, P. Kopietz, D. A. Bozhko, A. A. Serga, and B. Hillebrands, Magnetoelastic modes and lifetime of magnons in thin yttrium iron garnet films, *Phys. Rev. B* **89**, 184413 (2014).
- [61] A. Kamra, H. Keshtgar, P. Yan, and G. E. W. Bauer, Coherent elastic excitation of spin waves, *Phys. Rev. B* **91**, 104409 (2015).
- [62] S. Streib, N. Vidal-Silva, K. Shen, and G. E. W. Bauer, Magnon-phonon interactions in magnetic insulators, *Phys. Rev. B* **99**, 184442 (2019).
- [63] A. G. Gurevich and G. A. Melkov, *Magnetization Oscillations and Waves* (CRC Press, London, 2020).
- [64] Classically, a spin $\mathbf{S}$ in a magnetic field $\mathbf{H}$ precesses as $\dot{\mathbf{S}} = -[\gamma/\mu_s](\mathbf{S} \times \mathbf{H})$; i.e., it follows a counterclockwise motion.
- [65] J. Cui, E. V. Boström, M. Ozerov, F. Wu, Q. Jiang, J.-H. Chu, C. Li, F. Liu, X. Xu, A. Rubio, and Q. Zhang, Chirality selective magnon-phonon hybridization and magnon-induced chiral phonons in a layered zigzag antiferromagnet, *Nat. Commun.* **14**, 3396 (2023).

- [66] M. S. Dresselhaus, G. Dresselhaus, and A. Jorio, *Group Theory: Application to the Physics of Condensed Matter* (Springer Berlin, Heidelberg, 2008).
- [67] R. F. L. Evans, W. J. Fan, P. Chureemart, T. A. Ostler, M. O. A. Ellis, and R. W. Chantrell, Atomistic spin model simulations of magnetic nanomaterials, *J. Phys. Condens. Matter* **26**, 103202 (2014).
- [68] A minimum of $B \approx 4.5$ T is needed to shift the bare magnons energies above those of the bare TA phonons.
- [69] S. Park, N. Nagaosa, and B.-J. Yang, Thermal Hall effect, spin Nernst effect, and spin density induced by a thermal gradient in collinear ferrimagnets from magnon-phonon interaction, *Nano Lett.* **20**, 2741 (2020).
- [70] J. N. Kløgetvedt and A. Qaiumzadeh, Tunable topological magnon-polaron states and intrinsic anomalous Hall phenomena in two-dimensional ferromagnetic insulators, *Phys. Rev. B* **108**, 224424 (2023).
- [71] S. Bao, Z.-L. Gu, Y. Shangguan, Z. Huang, J. Liao, X. Zhao, B. Zhang, Z.-Y. Dong, W. Wang, R. Kajimoto, M. Nakamura, T. Fennell, S.-L. Yu, J.-X. Li, and J. Wen, Direct observation of topological magnon polarons in a multiferroic material, *Nat. Commun.* **14**, 6093 (2023).
- [72] A. Mook, J. Henk, and I. Mertig, Thermal Hall effect in noncollinear coplanar insulating antiferromagnets, *Phys. Rev. B* **99**, 014427 (2019).
- [73] C.-Z. Chang, C.-X. Liu, and A. H. MacDonald, Colloquium: Quantum anomalous Hall effect, *Rev. Mod. Phys.* **95**, 011002 (2023).
- [74] L. Zhang, Berry curvature and various thermal Hall effects, *New J. Phys.* **18**, 103039 (2016).
- [75] R. Matsumoto, R. Shindou, and S. Murakami, Thermal Hall effect of magnons in magnets with dipolar interaction, *Phys. Rev. B* **89**, 054420 (2014).
- [76] S. Murakami and A. Okamoto, Thermal Hall effect of magnons, *J. Phys. Soc. Jpn.* **86**, 011010 (2017).
- [77] X.-T. Zhang, Y. H. Gao, and G. Chen, Thermal Hall effects in quantum magnets, *Phys. Rep.* **1070**, 1 (2024).
- [78] G. Go and S. K. Kim, Tunable large spin Nernst effect in a two-dimensional magnetic bilayer, *Phys. Rev. B* **106**, 125103 (2022).
- [79] B. Li, S. Sandhoefner, and A. A. Kovalev, Intrinsic spin Nernst effect of magnons in a noncollinear antiferromagnet, *Phys. Rev. Res.* **2**, 013079 (2020).