DeepQuark: A Deep-Neural-Network Approach to Multiquark Bound States

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For the first time, we implement the deep-neural-network-based variational Monte Carlo approach for the multiquark bound states, whose complexity surpasses that of electron or nucleon systems due to strong SU(3) color interactions. We design a novel and high-efficiency architecture, DeepQuark, to address the unique challenges in multiquark systems such as stronger correlations, extra discrete quantum numbers, and intractable confinement interaction. Our method demonstrates competitive performance with state-of-the-art approaches, including diffusion Monte Carlo and Gaussian expansion method, in the nucleon, doubly heavy tetraquark, and fully heavy tetraquark systems. Notably, it outperforms existing calculations for pentaquarks, exemplified by the triply heavy pentaquark. For the nucleon, we successfully incorporate three-body flux-tube confinement interactions without additional computational costs. In tetraquark systems, we consistently describe hadronic molecule T_{cc} and compact tetraquark T_{bb} with an unbiased form of wave function ansatz. In the pentaquark sector, we obtain weakly bound $\bar{D}^*\Xi_{cc}^*$ molecule $P_{cc\bar{c}}(5715)$ with $S=\frac{5}{2}$ and its bottom partner $P_{bb\bar{b}}(15569)$. They can be viewed as the analogs of the molecular T_{cc}. We recommend experimental search of $P_{cc\bar{c}}(5715)$ in the D-wave $J/\psi\Lambda_c$ channel. DeepQuark holds great promise for extension to larger multiquark systems, overcoming the computational barriers in conventional methods. It also serves as a powerful framework for exploring confining mechanism beyond two-body interactions in multiquark states, which may offer valuable insights into nonperturbative QCD and general many-body physics.

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Introduction—The quark model proposed by Gell-Mann [1] and Zweig [2] provides a remarkably successful framework for understanding the conventional hadron spectrum, classifying hadrons into mesons ($q\bar{q}$) and baryons (qqq). Although multiquark states such as tetraquarks ($qq\bar{q}\,\bar{q}$) and pentaquarks ($qqqq\bar{q}$) were proposed concurrently [1,2], their existence remained elusive until recent years. Since the discovery of the $X(3872)$ in 2003 [3], numerous multiquark candidates have been observed, including many manifestly exotic states like $T_{c\bar{c}1}(3900)$ [4,5], $T_{cc}(3875)^+$ [6,7], $P_{c\bar{c}}$ states [8,9], and $T_{cc\bar{c}\,\bar{c}}(6900)^0$ [10] (see Refs. [11–19] for comprehensive reviews). Elucidating the configurations of these multiquark states poses new challenges to the quark model, and also offers a unique window into the nonperturbative regime of quantum chromodynamics (QCD)—the fundamental theory of strong interactions. The investigation of clustering behaviors in multiquark systems, particularly in distinguishing compact configurations from loosely bound hadronic molecules, offers an unprecedented opportunity to explore quantum many-body dynamics governed by SU(3) color interactions, which is fundamentally different from systems dominated by electromagnetic or nuclear forces.

Solving the quantum many-body problem of multiquark states in quark models can be quite challenging. In addition to the exponential scaling of wave function dimensionality with the particle number, the multiquark systems involve an extra SU(3) color degree of freedom compared to electron and nucleon systems, causing even greater complexity. Moreover, constructing multiquark systems of interest often requires imposing constraints from various quantum numbers—such as spin, parity, flavor, and color—that arise from underlying symmetry principles. These constraints significantly complicate the theoretical treatment. For example, in calculating the ground states of electron systems, spins are usually not explicitly constrained, as the ground state naturally converges to a certain spin configuration. However, in the case of doubly charmed tetraquark T_{cc} [6,7], the total spin should be constrained to

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1 to avoid falling into the lower scalar DD threshold. Furthermore, the strong color interaction between (anti) quarks leads to significant correlations, rendering the single-particle approximation—effective in nuclear and atomic systems—invalid. Consequently, the shell structure observed in those systems is absent in multiquark states. Without such a simplified approximation as a guidance or starting point, the full dynamical multichannel treatments of multiquark systems become computationally intensive. Additionally, progress in lattice QCD [20,21] seems to favor the few-body confinement mechanisms over pairwise interactions in multiquarks, introducing new challenges to their quantum many-body descriptions [22]. The aforementioned complexities make comprehensive calculations of multiquark states highly challenging, even for five-body systems. Existing approaches, such as basis expansion methods exemplified by the Gaussian expansion method (GEM) [23], are hindered from complete calculations due to the exponential growth of basis states. Meanwhile, diffusion Monte Carlo (DMC) suffers from the notorious sign problem [24], which severely limits its applicability to such strongly correlated systems. Previous studies on pentaquarks [25–31] made various approximations in the spatial configurations [26–30] or color degree of freedom [25,26,31] to simplify the calculations, which may result in unknown systematical errors and unreliable conclusions.

Recently, the development of machine learning techniques provides a new approach to solving the quantum many-body problem. Motivated by the exceptional capacity of deep neural networks (DNNs) to approximate high-dimensional functions [32], DNNs are anticipated to be a flexible and effective wave function representation capable of capturing complex many-body correlations efficiently [33,34]. DNN-based variational Monte Carlo (VMC) method has been successfully applied to quantum spin systems [35], atomic and molecular physics [36–38], condensed matter [39,40], and nuclear physics [41–47], achieving high accuracies and demonstrating potential for scaling to larger systems. However, its application in multiquark remains unexplored. DNN-based wave functions, which are free from *a priori* assumptions about multiquark configurations, can unbiasedly and consistently describe various multiquark states, including hadronic molecules and compact multiquarks. This capability is supported by the universal approximation theorem of neural networks [48,49] and demonstrated by our architecture and numerical results as follows. Moreover, VMC circumvents the sign problem in imaginary time evolution of DMC, making it capable of handling strongly correlated systems. Meanwhile, unlike basis expansion methods, VMC enables the treatments of complex interactions that go beyond two-body forces even without extra computational costs, paving the way for investigations of confining mechanisms and many-body forces in multiquark states.

In this Letter, we develop a DNN-based VMC approach, DeepQuark, to calculate multiquark bound states in the quark model. A major difference between DeepQuark and previous DNN-based studies is the architecture of many-body wave function. Most of the previous works use a determinant type wave function ansatz [37–39,44], which originates from the idea of single-particle orbitals in electron and nucleon systems, and consider the correlations by multiple determinants, Jastrow factors, and backflow transformation. However, such constructions may not apply to the strongly correlated hadron systems. Instead, we construct the DeepQuark wave function in the coupled color-spin-isospin bases, which represents the correlations in the most general way while automatically enforcing symmetry requirements. We first benchmark our results against GEM and DMC for the nucleon in two different confinement interactions and tetraquark bound states. We further demonstrate DeepQuark's ability for larger systems by investigating triply heavy pentaquarks $QQqq\bar{Q}$ ($Q = b, c; q = u, d$), where bound states that are analogs of the doubly heavy tetraquarks $QQ\bar{q}\,\bar{q}$ are obtained.

Hamiltonian—We employ the nonrelativistic Hamiltonian in a minimal quark model—the AL1 model (where "L" denotes linear confinement interaction) introduced in Refs. [50,51]. The AL1 potential consists of two parts: the one-gluon-exchange interaction V_{OGE}, accounting for the short-range perturbative QCD effects, and a two-body linear confinement term V_{conf}, which models the quark confinement in hadrons:

$$V_{\mathrm{OGE},ij} = -\frac{3}{16}\boldsymbol{\lambda}_i \cdot \boldsymbol{\lambda}_j \left(-\frac{\kappa}{r_{ij}} - \Lambda + \frac{8\pi\kappa'}{3m_i m_j} \frac{e^{-r_{ij}^2/r_0^2}}{\pi^{3/2} r_0^3} \boldsymbol{s}_i \cdot \boldsymbol{s}_j \right),$$
$$V_{\mathrm{conf},ij} = -\frac{3}{16}\boldsymbol{\lambda}_i \cdot \boldsymbol{\lambda}_j \lambda r_{ij}. \tag{1}$$

Here, $\boldsymbol{\lambda}_i$ is the SU(3) Gell-Mann color matrix acting on the i th quark (replaced by $-\boldsymbol{\lambda}^*$ for antiquark), and $\boldsymbol{s}_i$ is the spin operator. This interaction structure closely resembles that of the well-known Cornell model [52,53] but takes the light quark sector into consideration. The parameters of the model, including four constituent quark masses and six potential parameters, were determined by fitting the meson spectra across all flavor sectors.

For baryon systems, an additional phenomenological term $V_{123} = -(C/m_1 m_2 m_3)$ is introduced to mimic the three-body interaction effect [51]. For hadron systems with heavy quarks, this term is suppressed by the heavy quark mass and therefore is neglected in the calculations. For the nucleon, we also test the flux-tube confinement interaction $V_{\mathrm{conf}}^{\mathrm{ft}} = \sigma L_{\mathrm{min}}$, where L_{min} is the minimal length of the color flux tubes connecting three quarks at a junction point [54–56]. More details on the interactions, the model parameters, and the model uncertainty are given in Supplemental Material [57].

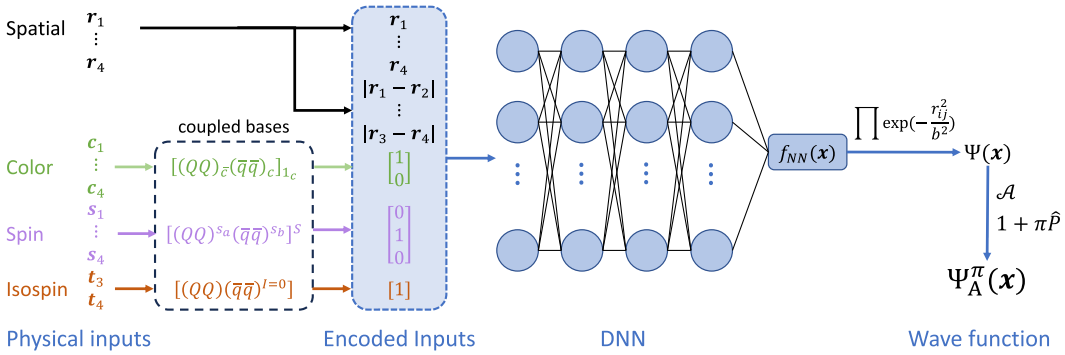


FIG. 1. Architecture of the DeepQuark wave function, taking isoscalar doubly heavy tetraquark as an example. The physical inputs in spatial, color, spin, and isospin degrees of freedom are transformed as the encoded inputs before fed into the DNN. Boundary condition, fermionic antisymmetrization ($\mathcal{A}$), and parity projection $(1+\pi\hat{P})$ are imposed on the scalar output of the DNN $f_{NN}(\boldsymbol{x})$ to obtain the multiquark wave function $\Psi^{\pi}_{\mathrm{A}}(\boldsymbol{x})$.

In the absence of spin-orbit and tensor operators, the total angular momentum J, total orbital angular momentum L, and total spin S are all conserved. Since ground states are expected to be S wave, we have $J=S$.

Neural-network wave function—The architecture of the DeepQuark wave function is illustrated in Fig. 1. The core of the framework is to construct a multiquark wave function with the desired symmetry, namely, a color-singlet state with definite total spin S, isospin I, and parity π that obeys Fermi-Dirac statistics. To that end, we work in the coupled bases. Taking isoscalar vector doubly heavy tetraquark as an example, the color-spin-isospin degrees of freedom can be coupled into the following independent bases:

$$\chi_{\bar{3}_c\otimes 3_c}\phi^{s_a,s_b}\xi^{I=0} = \left[(QQ)^{s_a}_{\bar{3}_c}(\bar{q}\,\bar{q})^{s_b,I=0}_{3_c}\right]^{S=1}_{1_c},$$
$$\chi_{6_c\otimes\bar{6}_c}\phi^{s_a,s_b}\xi^{I=0} = \left[(QQ)^{s_a}_{6_c}(\bar{q}\,\bar{q})^{s_b,I=0}_{\bar{6}_c}\right]^{S=1}_{1_c}, \qquad (2)$$

where s_a and s_b take all possible combinations. χ, ϕ, and ξ represent the color, spin, and isospin coupled bases, which are further mapped into vectors α_c, α_s, and α_t, respectively. Here, α is a standard basis vector in $\mathbb{R}^n$, with n being the number of independent bases. The mapping into standard basis vectors rather than integers from 1 to n ensures that no prejudiced correlation between different bases is introduced. By taking the vectors α as inputs of the DNN, the symmetry information is encoded into the DeepQuark wave function.

For the spatial degree of freedom, we include the (anti) quark coordinates in the center of mass frame $\boldsymbol{r}_i$ and the distances between two (anti)quarks $|\boldsymbol{r}_i-\boldsymbol{r}_j|$ as input features. The inclusion of the distances is redundant in principle but can improve the performance of neural-network wave function [37]. The magnitude of interparticle distance is a nonsmooth function at zero, which could better describe the wave function cusps [37] arising from short-range color Coulomb interaction in Eq. (1). It is also an important variable with direct physical meaning, which can encapsulate interparticle correlations effectively. As the wave function is a function of three-dimensional coordinates $\boldsymbol{r}_i$, it includes contributions from all orbital angular momentum L. The wave function should naturally converge to the S-wave ground state in the optimization process. It is also worth noting that the DeepQuark wave function ansatz does not encode any *a priori* bias toward either molecular or compact states, making it structurally neutral with respect to multiquark configurations.

The input features $\boldsymbol{x}=(\boldsymbol{r}_i,|\boldsymbol{r}_i-\boldsymbol{r}_j|,\alpha_c,\alpha_s,\alpha_t)$ are fed into a DNN with four fully connected hidden layers. Each layer takes the outputs of the previous layer as inputs and carries out the mapping $\boldsymbol{x}_{\mathrm{out}}=\sigma(\boldsymbol{W}\boldsymbol{x}_{\mathrm{in}}+\boldsymbol{c})$, where $\boldsymbol{W}$, $\boldsymbol{c}$ are variational parameters, and $\sigma=\tanh$ is the activation function. Since the parameters are initialized randomly, the initial trial wave function may be broadly distributed in the configuration space. To generate an initial state closer to the ground-state solution for faster convergence, we multiply the scalar output of the network f_{NN} by a boundary factor $\prod_{i<j}\exp(-r_{ij}^2/b^2)$, which constrains the system to a localized region. We take $b=2$–4 fm, which is on the order of the typical range of color confinement, $\Lambda_{\mathrm{QCD}}^{-1}\sim 1$ fm. We have verified that the ground-state results are independent of the boundary parameter b. Finally, the fermionic antisymmetry and parity projection is enforced,

$$\Psi^{\pi}_{\mathrm{A}}(\boldsymbol{x})=(1+\pi\hat{P})\mathcal{A}\left[f_{NN}(\boldsymbol{x})\prod_{i<j}\exp\left(-\frac{r_{ij}^2}{b^2}\right)\right], \qquad (3)$$

where $\hat{P}$ and $\mathcal{A}$ are the spatial inversion operator and antisymmetric operator of identical particles, respectively. Enforcing antisymmetry by explicitly summing over all possible permutations leads to a factorial complexity. However, given the current experimental and theoretical progress, we will only focus on multiquark systems with at most three to four identical particles, and such a complexity is manageable.

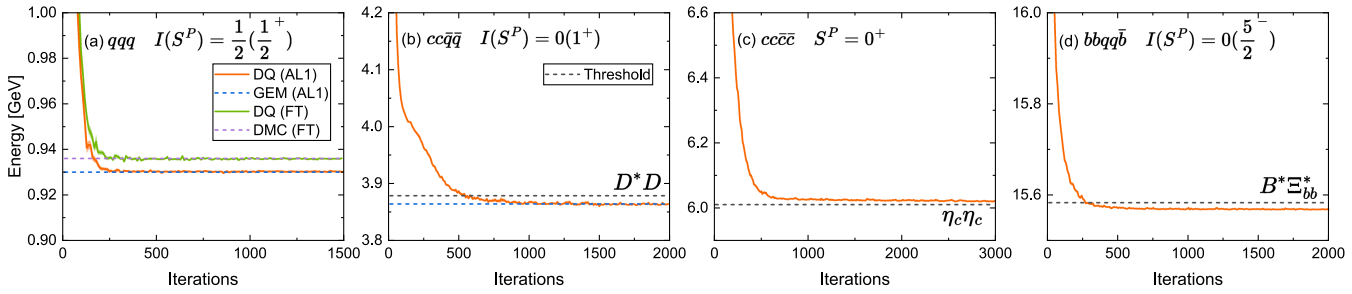


FIG. 2. The energy estimate as a function of iteration steps for the (a) nucleon in the AL1 potential and flux-tube confinement interaction (FT), (b) isoscalar vector doubly charmed tetraquark, (c) scalar fully charmed tetraquark, and (d) isoscalar triply bottomed tetraquark systems in the optimization progress of DeepQuark (DQ). The Monte Carlo standard errors of the energies are shown by the shaded area, which are very tiny. The lowest two-body dissociation thresholds are represented by the black dashed lines. The ground-state energies given by the GEM [58,59] and DMC [58] are displayed by the blue and purple dashed lines, respectively, for comparison.

The DNN is trained in an unsupervised way using the variational principle. A good enough wave function ansatz converges to the ground state in the optimization process. More details can be found in Supplemental Material [57].

Results and discussion—As a warm-up exercise, we test DeepQuark on few-electron systems, including $e^+e^-(\mathrm{Ps})$, $e^+e^-e^-(\mathrm{Ps}^-)$, and $e^+e^+e^-e^-(\mathrm{Ps}_2)$. They can be regarded as the quantum electrodynamics counterparts of multiquark systems [74]. The DeepQuark results can reach a high accuracy with less than 1% relative difference compared to the benchmark energies (see Supplemental Material [57]).

The optimization performance of DeepQuark in hadron systems is shown in Fig. 2. We take four systems as examples, including the nucleon, doubly charmed and fully charmed tetraquarks, and triply bottomed pentaquark. It can be seen that DeepQuark achieves good convergence within a few thousand iterations for all these systems. The statistical uncertainties (i.e., the Monte Carlo standard errors shown in Fig. 2) of the DeepQuark energy results are below 0.1 MeV, which are significantly smaller than the model uncertainty and can therefore be neglected. In the nucleon system, DeepQuark quickly converges to the benchmark results from GEM and DMC [58] for both two-body AL1 interaction in Eq. (1) and flux-tube confinement interaction. Calculating flux-tube interactions is computationally intractable in basis expansion methods, whereas DeepQuark handles them efficiently through Monte Carlo evaluation. This highlights DeepQuark's ability in managing complicate potentials of various forms.

For tetraquark states, we investigate two systems that are of most concern, the isoscalar doubly heavy tetraquark $QQ\bar{q}\,\bar{q}(T_{QQ})$ and fully heavy tetraquark $QQ\bar{Q}\,\bar{Q}(T_{4Q})$. The existence of a deeply bound T_{QQ} state for large enough heavy quark mass has long been anticipated [75,76] and was also predicted by lattice QCD study [77,78]. Moreover, great experimental progress has been made in the discovery of T_{cc} [6,7]. The T_{4Q} system serves as a clear platform to investigate the short-range gluon exchange and confinement interaction, as it is less affected by the chiral dynamics. Bound states in such a system are inconclusive but a family of T_{4c} resonances have been discovered experimentally [10,79,80]. Recently, the CMS collaboration determined three T_{4c} resonances with high significances and analyzed their quantum numbers to be $J^{PC}=2^{++}$ [81]. In Table I, we present the ground-state properties of these tetraquark states and compare them with the results from GEM, which was shown to be a superior numerical approach to solving tetraquark bound states [59]. For T_{QQ} systems, the DeepQuark ground-state energies are consistent with the GEM results in general, and lower the energies by $\simeq$1 MeV (see Table I). This shows that DeepQuark has a stronger expressive power for the multiquark wave function than GEM, as indicated by the variational principle. The ground state of T_{bb} is dominated by the $\chi_{\bar{3}_c\otimes 3_c}$ color configuration, whereas T_{cc} exhibits sizable contributions from both $\chi_{\bar{3}_c\otimes 3_c}$ and $\chi_{6_c\otimes\bar{6}_c}$ configurations. Starting from a randomly initialized trial wave function, DeepQuark naturally converges to these two ground states with distinct mixing effects, demonstrating its strong capability in handling coupled-channel problems. On the other hand, no bound state solution is found in T_{4Q} systems. The ground-state energies lie above the lowest meson-meson thresholds, and the color proportions $\chi_{\bar{3}_c\otimes 3_c}:\chi_{6_c\otimes\bar{6}_c}\simeq 1:2$ are in accordance with the meson-meson scattering states [82]. However, since the DeepQuark wave function is constrained in a localized space, it cannot converge to an ideal scattering state with zero relative momentum. Therefore, the ground-state energies are $\sim$10 MeV above the thresholds and the color proportions slightly deviates from $\chi_{\bar{3}_c\otimes 3_c}:\chi_{6_c\otimes\bar{6}_c}\simeq 1:2$.

The DeepQuark wave function can consistently describe multiquark states with various configurations. It is capabale of capturing the dynamical effects in different systems, converging to a compact T_{bb} state and a molecular T_{cc} state. The root-mean-square (rms) radii of T_{bb} and T_{cc} are shown in Table I. T_{bb} is a distinct compact tetraquark, where two bottom quarks form a compact diquark cluster of 0.33 fm and the light quarks orbit around the heavy

TABLE I. Ground-state energies, color proportions, and rms radii (in fm) of the isoscalar doubly heavy ($QQ\bar{q}\,\bar{q}$) and fully heavy ($QQ\bar{Q}\,\bar{Q}$) tetraquark systems. The binding energies ΔE (in MeV) are with respect to the lowest dihadron thresholds listed in the third column. "NB" indicates no bound state solution. The statistical errors of the energies from DeepQuark (DQ) are less than 0.1 MeV. The ground-state energies from GEM [59] are listed for comparison.

			DQ						GEM [59]
	S^P	Thresholds	ΔE	$\chi_{\bar{3}_c\otimes 3_c}$	$\chi_{6_c\otimes\bar{6}_c}$	$r_{Q\bar{q}}$	r_{QQ}	$r_{\bar{q}\,\bar{q}}$	ΔE
$cc\bar{q}\,\bar{q}$	1^+	D^*D	-15	55%	45%	1.06	1.24	1.41	-14
$bb\bar{q}\,\bar{q}$	1^+	$\bar{B}^*\bar{B}$	-153	97%	3%	0.69	0.33	0.78	-152
$cc\bar{c}\,\bar{c}$	$0^+, 1^+, 2^+$	$\eta_c\eta_c, \eta_c J/\psi, J/\psi J/\psi$	NB	∼34%	∼66%				NB
$bb\bar{b}\,\bar{b}$	$0^+, 1^+, 2^+$	$\eta_b\eta_b, \eta_b\Upsilon, \Upsilon\Upsilon$	NB	∼34%	∼66%				NB

diquark. It is worth noting that a deeply bound T_{bb} state with a binding energy of around 150 MeV is in agreement with lattice QCD results, see Refs. [77,78]. In contrast to the compact T_{bb}, the size of T_{cc} is significantly larger, with $r_{cc}, r_{\bar{q}\,\bar{q}} > r_{c\bar{q}}$, suggesting a molecular structure of two charmed mesons [83]. A loosely bound molecular T_{cc} is in agreement with the experimental results [6,7]. The separation between two charmed mesons becomes larger when the binding energy is tuned to be as small as the experimental one [84].

Inspired by the existence of $\bar{Q}\,\bar{Q}\,qq$ bound states, we further employ DeepQuark to investigate the isoscalar triply heavy pentaquark ($QQqq\bar{Q}$), which is the partner of the doubly heavy tetraquark if we consider the diquark-antiquark symmetry [85,86], namely, replacing a heavy antiquark $\bar{Q}$ by a heavy diquark QQ. As the two heavy quarks may form a compact object with the same color representation $\bar{3}_c$ as the antiquark, it is expected that the interactions in these two systems are similar, and $\bar{Q}\,\bar{Q}\,qq$ bound states may imply the existence of $QQqq\bar{Q}$ bound states. DeepQuark has great advantages in extending to such pentaquark systems, since the computational complexity is almost the same as solving the tetraquark systems. A complete set of color basis for the pentaquark is given by

$$\begin{aligned}
\chi_{\bar{3}_c\otimes\bar{3}_c} &= \{[(QQ)_{\bar{3}_c}(qq)_{\bar{3}_c}]_{3_c}\bar{Q}\}_{1_c},\\
\chi_{\bar{3}_c\otimes 6_c} &= \{[(QQ)_{\bar{3}_c}(qq)_{6_c}]_{3_c}\bar{Q}\}_{1_c},\\
\chi_{6_c\otimes\bar{3}_c} &= \{[(QQ)_{6_c}(qq)_{\bar{3}_c}]_{3_c}\bar{Q}\}_{1_c}.
\end{aligned} \tag{4}$$

We show the ground-state properties in Table II. In contrast to the expectations from diquark-antiquark symmetry, we find no bound state in the $S=\frac{1}{2},\frac{3}{2}$ $QQqq\bar{Q}$ systems. The reason is that the existence of $\bar{Q}$ breaks the diquark-antiquark symmetry by taking one of the heavy quarks to form a quarkonium $(Q\bar{Q})_{1_c}$, which is more stable and has lower energy than the configuration with $(QQ)_{\bar{3}_c}$. The ground states in these systems are scattering states of a heavy quarkonium and a singly heavy baryon. However, in $S=\frac{5}{2}$ system, an S-wave $S=\frac{3}{2}$ singly heavy isoscalar baryon is not allowed by the antisymmetry of light quarks. As a result, the lowest threshold is $\bar{D}^*\Xi_{cc}^*$ for $ccqq\bar{c}$ and $B^*\Xi_{bb}^*$ for $bbqq\bar{b}$. We find bound state solutions $P_{cc\bar{c}}(5715)$ and $P_{bb\bar{b}}(15569)$, whose binding energies are 3 and 14 MeV, respectively. They may decay to meson-baryon channels with lower total spin if spin-orbit coupling is considered. For example, $P_{cc\bar{c}}(5715)$ may be searched for in the $J/\psi\Lambda_c$ channel, but its width is expected to be suppressed by the D-wave decay. From the rms radii of $P_{cc\bar{c}}(5715)$, the distance $r_{cc}=0.5$ fm is consistent with the compact size of Ξ_{cc}^*, whereas $r_{c\bar{c}}=1.73$ fm is substantially larger. The spatial separation suggests a molecular configuration composed of loosely bound $\bar{D}^*$ and Ξ_{cc}^*, which is analogous to the molecular T_{cc}. $P_{bb\bar{b}}(15569)$ exhibits a similar configuration, but its size is compacted by the heavy quark mass.

Conclusions and outlooks—We introduce a novel and high-efficiency DNN-based VMC approach, DeepQuark, to solving the multiquark bound states. We exploit the expressive power of DNN to construct an unbiased and symmetry-informed wave function ansatz, which is capable

TABLE II. Ground-state energies, color proportions, and rms radii (in fm) of the isoscalar triply heavy pentaquark ($QQqq\bar{Q}$) systems. The remaining notations follow the same conventions as in Table I.

	S^P	Thresholds	ΔE	$\chi_{\bar{3}_c\otimes\bar{3}_c}$	$\chi_{\bar{3}_c\otimes 6_c}$	$\chi_{6_c\otimes\bar{3}_c}$	r_{QQ}	r_{Qq}	r_{qq}	$r_{Q\bar{Q}}$	$r_{q\bar{Q}}$
$ccqq\bar{c}$	$\frac{1}{2}^-,\frac{3}{2}^-$	$\eta_c\Lambda_c, J/\psi\Lambda_c$	NB	∼35%	0%	∼65%					
	$\frac{5}{2}^-$	$\bar{D}^*\Xi_{cc}^*$	-3	27%	73%	0%	0.50	1.39	1.90	1.73	1.38
$bbqq\bar{b}$	$\frac{1}{2}^-,\frac{3}{2}^-$	$\eta_b\Lambda_b, \Upsilon\Lambda_b$	NB	∼35%	0%	∼65%					
	$\frac{5}{2}^-$	$B^*\Xi_{bb}^*$	-14	19%	80%	1%	0.30	0.89	1.22	0.88	0.88

of handling complex interactions and describing various multiquark configurations. DeepQuark is competitive with state-of-the-art approaches including DMC and GEM in baryon and tetraquark systems, reaching high accuracies on ground-state energies with low computational costs. In the nucleon, DeepQuark easily adapts both two-body and flux-tube interactions. In tetraquark systems, it consistently describes meson molecule T_{cc} and compact tetraquark T_{bb}. Moreover, we employ DeepQuark to investigate triply heavy pentaquark ($QQqq\bar{Q}$) systems. We obtain weakly bound $\bar{D}^*\Xi_{cc}^*$ molecule $P_{cc\bar{c}}(5715)$ with $S=\frac{5}{2}$ and its bottom partner $P_{bb\bar{b}}(15569)$. They can be viewed as the analogs of the molecular T_{cc}. We recommend experimental search for $P_{cc\bar{c}}(5715)$ in the D-wave $J/\psi\Lambda_c$ channel, which could be explored in future LHCb experiments.

DeepQuark holds great promise for extension to diverse pentaquark and even hexaquark systems, overcoming the computational barriers that limit conventional methods. Such investigations can provide forward-looking predictions for future experiments. Furthermore, DeepQuark is capable of incorporating a variety of potential models with different dynamical ingredients, including complex interactions beyond two-body forces. It therefore provides a powerful framework for investigating lattice-inspired potentials and exploring the confining mechanisms of tetraquark states in future studies, potentially offering valuable insights into the multiquark internal structures and nonperturbative QCD. The techniques employed in DeepQuark could enrich the toolkit of deep learning approaches integrated with physics, particularly shedding new light on quantum many-body phenomena.

The codes are developed on top of JAX [60], FLAX [61], and the NetKet package [62,63].

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Data availability—The data supporting this study's findings are available within the Letter. The codes that can reproduce the reported results are available on GitHub [87].

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