

Search for Feebly Interacting Particles in B Decays with Missing Energy at Belle

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We present a search for an invisible hidden-sector particle X_{inv} , produced in $B^0 \rightarrow \bar{D}^0 X_{\text{inv}}$ and $B^\pm \rightarrow h X_{\text{inv}}$ decays, where $h = \pi^\pm, K^\pm, D_s^\pm, p^\pm$. The search is performed using e^+e^- collision data recorded with the Belle detector, corresponding to 711 fb^{-1} . No significant signal is observed. We set 90% confidence level upper limits ranging between 10^{-4} and 10^{-6} on the branching fraction $\mathcal{B}(B \rightarrow h X_{\text{inv}})$ as a function of $m_{X_{\text{inv}}}$. Corresponding limits are set on $\mathcal{B}(B \rightarrow h X) \times \mathcal{B}(X \rightarrow \gamma\gamma)$ for lifetimes $c\tau_X$ between $10 \text{ }\mu\text{m}$ and 10 m . Many of these limits are the first direct constraints on their respective decays. Our results provide the most stringent exclusion limits to date on the branching fractions for all search channels, and exclude previously unexplored regions of parameter space relevant to several new physics models.

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In recent years, the absence of evidence for physics beyond the standard model (SM) at the energy frontier has shifted attention toward searches for new particles with masses comparable to those of known SM particles. If such particles exist and have so far avoided detection, this would likely be due to their small couplings to SM particles; such hypothetical particles are termed feebly interacting particles (FIPs) [1]. The interactions of FIPs with SM particles can be governed by low-dimensional operators, or *portals*, classified according to mediator spin [2]. This phenomenological framework enables straightforward comparison across experimental searches.

Many particles proposed in extensions to the SM are FIP candidates. Pseudoscalar axionlike particles (ALPs) arise in many extensions to the SM [3–5] and offer potential solutions to longstanding problems in physics [6], as potential dark matter candidates [7–9] or dark sector mediators [10]. Constraints on ALP couplings to photons and electrons are already stringent across the MeV–GeV range [6,11–14]. ALPs produced in flavor-changing neutral current (FCNC) processes, such as those in B decays, are especially promising to detect, as these transitions are suppressed in the SM, enhancing sensitivity to physics beyond the SM [15–24]. These decays depend on effective couplings to flavor-changing currents [25], which receive contributions at tree-level from flavor-violating couplings in the UV [26,27] and at loop-level from the coupling of ALPs to top quarks and $W^\pm$ bosons, which, compared to the couplings to photons and electrons, are less constrained [10,28–33].

Scalars can also be dark matter candidates [34] or dark sector mediators [35], and can play roles in solving a range of problems in physics [29,36–42]. Dedicated studies in B decays further probe their parameter space [43,44]. While less commonly studied in B decays, light vector particles are also in principle allowed [45,46], with potential relevance to the excess rate measured for $B^+ \rightarrow K^+ \nu \bar{\nu}$ [47].

Although portals provide a general classification of models, the observability of a new particle depends on its decay properties. A FIP may appear invisible because it is a dark matter candidate, predominantly decays into dark matter candidates, or because it has a long lifetime and decays outside the detector volume. In any case, the result is a missing energy signature.

In this Letter, we report on a search for an invisible FIP, X_{inv} , produced in $B^0 \rightarrow \bar{D}^0 X_{\text{inv}}$ and $B^\pm \rightarrow h X_{\text{inv}}$ decays, where $h = \pi^\pm, K^\pm, D_s^\pm, p$. Charged-conjugate decays are implied throughout. The data were collected with the Belle detector [48] at the energy-asymmetric e^+e^- KEKB collider [49] at a center-of-mass (c.m.) energy $\sqrt{s} = 10.58 \text{ GeV}$. The search is performed on a dataset containing $(770 \pm 11) \times 10^6$ $e^+e^- \rightarrow \Upsilon(4S) \rightarrow B\bar{B}$ events, corresponding to an integrated luminosity of 711 fb^{-1} .

The search for X_{inv} is carried out by scanning for narrow peaks in the momentum distribution of the recoiling hadron in the frame of its parent (signal-side) B meson, denoted p_h . The other (tag-side) B meson in the event is also reconstructed to kinematically constrain the event. A scan is performed across the p_h distribution looking for excesses above the expected background. The current best limits on the branching fractions of $B^+ \rightarrow K^+ X_{\text{inv}}$ and $B^+ \rightarrow \pi^+ X_{\text{inv}}$ come from searches for the SM channels $B^+ \rightarrow K^+ \nu \bar{\nu}$ and $B^+ \rightarrow \pi^+ \nu \bar{\nu}$ at B -factories, which have excluded branching fractions down to approximately 10^{-5} for both channels [50–53]. Recently, there has been a surge of interest in $b \rightarrow s \nu \bar{\nu}$ transitions, as Belle II reported evidence of $B^+ \rightarrow K^+ \nu \bar{\nu}$ [54]. The best existing limit on $\mathcal{B}(B^+ \rightarrow p X_{\text{inv}})$ is

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about 10^{-6} , set by a recent *BABAR* search [55]. To date, there have been no dedicated searches for the two decays involving charm mesons discussed in this Letter, making this the first search for $B^+ \rightarrow D_s^+ X_{\text{inv}}$ and $B^0 \rightarrow \bar{D}^0 X_{\text{inv}}$.

While our primary focus is on invisible final states, we also assess the sensitivity of our selection to scenarios where a particle X decays via $X \rightarrow \gamma\gamma$ with decay length comparable to the detector size. Although our analysis is optimized for the invisible case, such visible decays can mimic the X_{inv} signature when X decays outside the sensitive detector volume or when the decay products escape detection.

The Belle detector has a cylindrical symmetry around the beamline, with the z -axis defined as the direction of the electron beam. The Belle detector comprises six sub-detectors, listed in the following from innermost to outermost: the silicon vertex detector, the central drift chamber, the aerogel Cherenkov counter, the time-of-flight scintillation counter, the electromagnetic calorimeter (ECL), and the K_L^0 and muon detector. The ECL consists of a cylindrical barrel region surrounding the beamline and forward and backward end cap regions at either end, with the forward end cap located in the positive z direction. A solenoid produces a 1.5 T magnetic field through the five innermost detectors. Further details of the detector are in Ref. [48].

Signal events are simulated using the Monte Carlo (MC) event generator EvtGen [56] for a range of X_{inv} masses from 1 MeV/ c^2 to just below the kinematically allowed upper limit of $m_B - m_h$, for both invisible X_{inv} and $X \rightarrow \gamma\gamma$. For the latter, the lifetime $c\tau_X$ is generated in a range from 10 μm to 10 m. The background processes $e^+e^- \rightarrow \Upsilon(4S) \rightarrow B\bar{B}$ (with SM B decays) and $e^+e^- \rightarrow q\bar{q}(\gamma)$ (where $q = u, d, s, c$) are simulated using EvtGen and Pythia [57], with final-state radiation simulated using Photos [58]. The detector response is modeled with Geant3 [59]. Both experimental and simulated events are converted to the Belle II format [60], and then reconstructed and analyzed using the Belle II analysis software framework [61,62]. To avoid experimenter's bias, the selection criteria and analysis procedure are finalized using simulated events before examining the data.

The tag-side B meson is reconstructed from hadronic decay modes using the full event interpretation (FEI) algorithm [63]. It must satisfy $M_{\text{bc}} \equiv \sqrt{s/4 - |p_B^*|^2} > 5.27 \text{ GeV}/c^2$ and $|\Delta E| \equiv |E_B^* - \sqrt{s}/2| < 0.1 \text{ GeV}$, where p_B^* and E_B^* are the momentum and energy of the B meson. Here and throughout the Letter, quantities in the e^+e^- c.m. frame are indicated by an asterisk. The signal quality returned by the FEI is required to exceed 0.005, which retains 48% (59%) of signal events and rejects 89% (88%) of background events for charged (neutral) B mesons.

All signal channels contain at least one charged particle in the final state. We select reconstructed trajectories of charged particles (tracks) with a point of closest approach

to the interaction point (IP) in the radial direction satisfying $dr < 2 \text{ cm}$, and in the z -direction satisfying $|dz| < 3 \text{ cm}$. All final-state particles are required to have a momentum $p^* > 0.1 \text{ GeV}/c$.

Charged particles are identified using a binary ratio P of likelihoods $\mathcal{L}$, which compares two particle hypotheses i and j : $P_{ij} \equiv \mathcal{L}_i/(\mathcal{L}_i + \mathcal{L}_j)$ [64]. In the search for $B^+ \rightarrow K^+ X_{\text{inv}}$ ($B^+ \rightarrow \pi^+ X_{\text{inv}}$), we select charged kaons (pions) with 88% (92%) efficiency with a 4% (7%) pion (kaon) mis-identification rate. In the search for $B^+ \rightarrow p X_{\text{inv}}$, protons are identified with 97% efficiency with 18% and $< 1\%$ kaon and electron misidentification rates, respectively.

In the searches for $B^+ \rightarrow D_s^+ X_{\text{inv}}$ and $B^0 \rightarrow \bar{D}^0 X_{\text{inv}}$, the D_s^+ and D^0 mesons are reconstructed from specific final states: $D_s^+ \rightarrow K^+ K^- \pi^+$ and $D^0 \rightarrow K^- \pi^+$, $K^- \pi^+ \pi^0$, or $K^- \pi^+ \pi^- \pi^+$. The π^+ and K^+ candidates in these decays must meet the same IP requirements as above, with looser particle identification selections, corresponding to 97% (98%) charged kaon (pion) efficiency, with a pion (kaon) mis-identification rate of 18% (23%). A vertex fit is performed as detailed in Ref. [65]. The D_s^+ and D^0 candidates are required to lie within 3 times the mass resolution of their nominal masses [66].

Neutral pion candidates are reconstructed using two ECL energy deposits (clusters) not matched with tracks, which we identify as photons, with an invariant mass between 118 MeV/ c^2 and 150 MeV/ c^2 (corresponding to an invariant mass window of approximately $\pm 2\sigma$). This retains 97% of π^0 produced in the decay $\bar{D}^0 \rightarrow K^+ \pi^- \pi^0$. To suppress background in the ECL, we apply minimum photon energy thresholds of 50 MeV in the barrel and 100 MeV in the end caps.

The rest of event (ROE) refers to all reconstructed charged particles and photons in the event that are not associated with the signal- or tag-side decays. Charged particles are only considered in the ROE if $dr < 2 \text{ cm}$ and $|dz| < 5 \text{ cm}$, and photons are only considered if their energies are greater than 50 MeV, 100 MeV, and 150 MeV in the barrel, forward end cap, and backward end cap, respectively. Events are retained only if there are no charged particles in the ROE and the total energy from photons in the ROE (E_{ECL}) does not exceed 1.5 GeV.

To further suppress background, we train two boosted decision trees (BDTs) [67] on simulated events. The first classifier, BDT1, suppresses $e^+e^- \rightarrow q\bar{q}$ background using 32 event-shape variables: the ratio of the second to zeroth Fox-Wolfram moment (R_2) [68], 16 modified Fox-Wolfram moments [69,70], thrust-related quantities [71], such as the thrust axes of the B_{tag} and ROE, the cosine of the angle between these axes, the cosine of the angle between the B_{tag} axis and z axis, the CLEO cones [72], the B_{tag} energy difference and flight distance, and missing mass squared. It is trained on $e^+e^- \rightarrow q\bar{q}$ and $B\bar{B}$ events corresponding to 400 fb $^{-1}$.

The second classifier, BDT2, suppresses $B\bar{B}$ background. It is trained on $B\bar{B}$ and signal MC events using 25 of the original 32 variables together with E_{ECL} [71,73], which is highly discriminating against $B\bar{B}$ background. The seven removed variables are strongly correlated either with other input variables in signal MC or with E_{ECL} . BDT2 is trained on simulated $B\bar{B}$ events passing a 90% signal-efficiency requirement on the BDT1 output, using a sample corresponding to about 5 ab^{-1} , together with 75% of the signal MC sample. The different training samples and input variables make the two classifiers complementary, as confirmed by the nondegenerate two-dimensional optimization described below.

The selection criteria for the two classifier outputs are optimized using a two-dimensional grid search, with a Punzi figure of merit [74] with a target statistical significance of 3σ . The selection criteria for the classifier outputs are optimized for each channel individually. Averaged across all channels, a signal efficiency of 84% and background rejection of 86% are achieved. In simulated signal events, the average number of candidates per event is 1.5 for $B^+ \rightarrow hX_{\text{inv}}$ and 1.9 for $B^0 \rightarrow \bar{D}^0 X_{\text{inv}}$. In cases where multiple candidates satisfy the selection criteria, the candidate with the highest FEI signal probability is retained. The correctly reconstructed candidate is selected more than 97% of the time for $B^+ \rightarrow hX_{\text{inv}}$, and 80% of the time for $B^0 \rightarrow \bar{D}^0 X_{\text{inv}}$.

We verify that the BDT classifiers perform similarly in data and simulation by studying two-body SM B decays that are kinematically similar to the signal processes. For $h = K^+$, we examine a sample with two ROE tracks near the $J/\psi \rightarrow \ell^+ \ell^-$ (where $\ell = e, \mu$) peak arising from $B^+ \rightarrow J/\psi K^+$ decays. For $h = D^0$, we examine an E_{ECL} sideband with $2.25 < E_{\text{ECL}} < 3.5 \text{ GeV}$ near the $\pi^0 \rightarrow \gamma\gamma$ peak arising from $B^0 \rightarrow \bar{D}^0 \pi^0$ decays. Classifiers' responses for these channels are validated in these respective sidebands. The BDT output distributions show good agreement between data and simulation [75]; ratios of data to MC BDT outputs are within $\pm 5\%$ across the full range. By contrast, the FEI efficiency exhibits differences of $\sim 20\%$ between data and simulation. This disparity arises because the FEI aggregates thousands of subclassifiers across ~ 200 hadronic decay channels, amplifying small per-variable mismodeling into a cumulative efficiency difference, whereas each BDT uses only ~ 30 event-shape variables whose individual data/MC agreement is validated directly.

The FEI efficiency is calibrated using $B \rightarrow D^{(*)} \ell \nu$ decays [76]. The correction is taken as the ratio of signal yields between real and simulated data; the values are 0.79 ± 0.02 and 0.78 ± 0.02 for charged and neutral B mesons, respectively. These values are cross-checked using sidebands containing $B^+ \rightarrow J/\psi K^+$ and $B^0 \rightarrow \bar{D}^0 \pi^0$ events for charged and neutral B decays, respectively. In the two-track sample, we fully reconstruct the B_{sig} decay $B^+ \rightarrow J/\psi K^+$, requiring $|\Delta E| < 0.1 \text{ GeV}$, and only keep

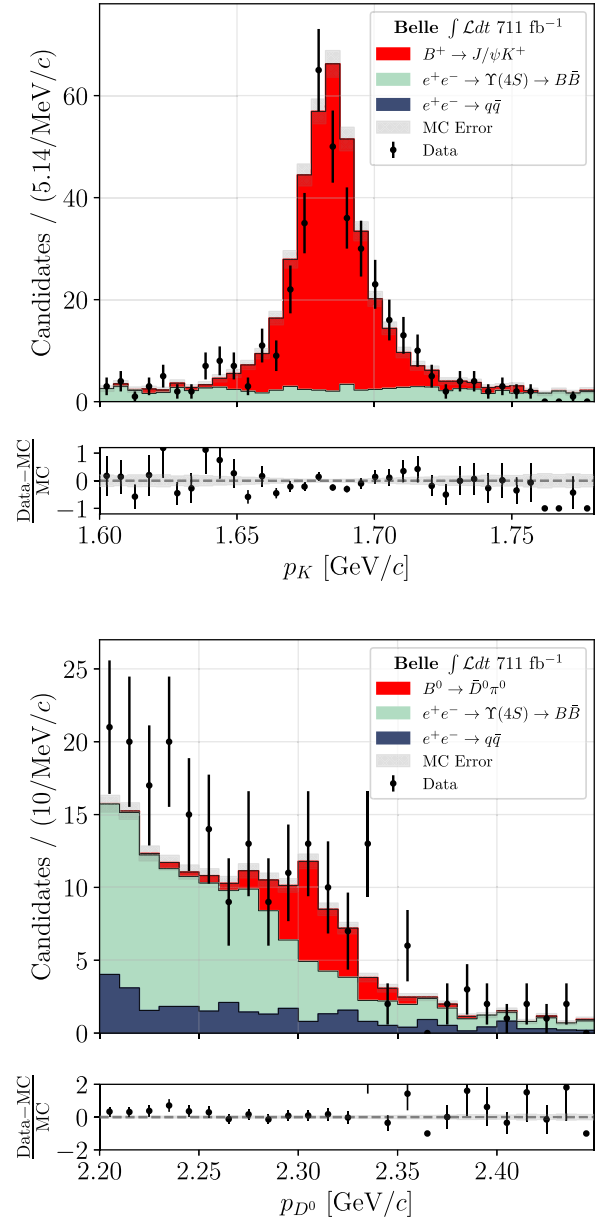


FIG. 1. Momentum distributions of the K^+ and D^0 in the B_{sig} -frame for the two control channels, $B^+ \rightarrow J/\psi K^+$ (top) and $B^0 \rightarrow \bar{D}^0 \pi^0$ (bottom), respectively, overlaid with the expected distributions from simulation.

candidates with $1.6 < p_K < 1.78 \text{ GeV}/c$. No additional selection is applied to the $B^0 \rightarrow \bar{D}^0 \pi^0$ sideband, in which candidates are kept with $2.20 < p_{D^0} < 2.45 \text{ GeV}/c$. The experimental and simulated momentum distributions for both control modes are shown in Fig. 1. We perform a fit to the K^+ and $\bar{D}^0$ momentum distributions. The peaks in these distributions, corresponding to the recoiling J/ψ and π^0 , are modeled using a sum of two Gaussian functions. The background is modeled with a third-order polynomial. The signal peak width is allowed to float in the fit to data. The width scale factor is used to correct for resolution

differences between simulation and experimental data, and is found to be 1.21 ± 0.05 and 1.08 ± 0.23 for $B^+ \rightarrow J/\psi K^+$ and $B^0 \rightarrow \bar{D}^0 \pi^0$, respectively. The ratios of signal yields between experimental and simulated data are 0.75 ± 0.09 and 0.84 ± 0.34 for charged and neutral B mesons, respectively. These values agree with the ratios derived from $B \rightarrow D^{(*)} \ell \nu$ decays.

The signal selection efficiency depends on the decay mode: for $h = \pi^+, K^+, p$, it is around 0.5%, while for $h = D_s^+, \bar{D}^0$, it is around 0.01%, as only a fraction of the D_s^+ and D^0 decays are reconstructed. The efficiency is mostly flat as a function of $m_{X_{\text{inv}}}$, but reduces as $m_{X_{\text{inv}}}$ approaches the kinematic limit of $m_B - m_h$.

The signal yield is extracted by performing extended, unbinned maximum likelihood fits to p_h . The fit model consists of signal and background components. The signal component is modeled as a sum of two Gaussian functions with a shared mean μ and different widths σ_1 and σ_2 . The fit is first performed on simulated signal events, allowing the widths and relative contributions of the Gaussian components to float. Subsequently, these fit results are parametrized as a function of the p_h value corresponding to the generated $m_{X_{\text{inv}}}$ of the sample. The resolution σ of the peak is the quadrature sum of the two width parameters, taking into account their relative weights, and the width scaling factor derived from the control mode fits. This approach provides a well-defined signal probability density function (PDF) at any scan point.

To parametrize the background, we use a kernel density estimator (KDE) [77], with the kernel width set by the local event density. The KDE is built from simulated background events and has a fixed shape during the signal extraction fit. Differences in the p_h distribution between off-resonance data and simulated $e^+e^- \rightarrow q\bar{q}$ events are accounted for by applying a linear correction to the $e^+e^- \rightarrow q\bar{q}$ background PDF. Independent fits are conducted for several hundred mass hypotheses for each channel, with scan steps equal to half the signal resolution. The resolution ranges from about 5 MeV/ c to 40 MeV/ c , generally increasing as $m_{X_{\text{inv}}}$ decreases. The KDE for a given fit window is defined over a $\pm 15\sigma$ window. A combined signal and background fit is performed in a $\pm 10\sigma$ window to mitigate the impact of the KDE boundary problem [77].

For all channels, a toy MC study is performed in which simulated events are sampled with varying yields of signal, $q\bar{q}$, and $B\bar{B}$ background events. The mean signal yield obtained from the combined fitting method closely matches the number of signal events in the sampled datasets, indicating the signal extraction method responds linearly to the presence of signal events.

The only background processes that can mimic the peaking structure of the signal are two-body B decays. For common processes with narrow peaks, such as $B^+ \rightarrow K^+ \bar{D}^0$, events within three times the resolution of the peak are vetoed. For some of these processes, such as

$B^+ \rightarrow K^+ f_0(1370)$, the recoil peak is so broad that it can be safely treated as a non-peaking background. For very rare processes where the expected number of events is below the expected sensitivity of the search, such as $B^+ \rightarrow K^+ K^{*0}(892)$ (which has a branching fraction $\mathcal{O}(10^{-7})$) [78], a signal-like PDF component corresponding to the SM particle mass is added to the fit, and its yield is allowed to float within $\pm 100\%$ of the predicted branching fraction or two events, whichever is greater.

The dominant systematic uncertainty is the 2.5% uncertainty on the FEI correction factor for both charged and neutral B mesons. Other sources include uncertainties in particle identification, tracking efficiency, corrections made to the p_h distributions from $e^+e^- \rightarrow q\bar{q}$ events, and limited signal MC statistics. For channels involving D_s^+ and $\bar{D}^0$ mesons, uncertainties in the branching fractions of the specific decay modes used for their reconstruction are included, with an additional uncertainty from π^0 reconstruction in the $\bar{D}^0$ case. Peaking background yields also contribute to the total uncertainty. Statistical uncertainties dominate across all five channels, while total systematic uncertainties remain below a few percent.

The branching fraction $\mathcal{B}(B \rightarrow h X_{\text{inv}})$ is extracted directly from an extended maximum likelihood fit to the p_h spectrum. The selection efficiency and the number of $B\bar{B}$ pairs are included as nuisance parameters, allowing their associated uncertainties to be propagated through the fit.

The local significance for each mass hypothesis is defined as $\mathcal{S}_{\text{local}} = \sqrt{2 \cdot (\log \mathcal{L}_{s+b} - \log \mathcal{L}_b)}$, where $\mathcal{L}$ denotes the maximum likelihood under the signal-plus-background and background-only hypotheses. Given the scan over several hundred mass points per channel, the look-elsewhere effect [79] is addressed by converting $\mathcal{S}_{\text{local}}$ to a global significance $\mathcal{S}_{\text{global}}$ using the trial factor method of Ref. [80].

No significant excess is observed. The most significant local excess, $\mathcal{S}_{\text{local}} = 2.95\sigma$, is observed at $m_{X_{\text{inv}}} = 3.28 \text{ GeV}/c^2$ in the $B^+ \rightarrow \pi^+ X_{\text{inv}}$ channel, corresponding to $\mathcal{S}_{\text{global}} = 0.65\sigma$ [75]. Upper limits at the 90% confidence level (CL) are set as a function of $m_{X_{\text{inv}}}$ using the modified frequentist CL_s method [81]. Limits on the branching fraction are computed at each mass point, as shown in Fig. 2. Notably, the limit on $\mathcal{B}(B^+ \rightarrow K^+ X_{\text{inv}})$ excludes a two-body explanation of the observed excess in $B^+ \rightarrow K^+ \nu \bar{\nu}$ [82] in the mass ranges $m_{X_{\text{inv}}} < 1.74$, $2.11 < m_{X_{\text{inv}}} < 2.93$, $3.15 < m_{X_{\text{inv}}} < 3.48$, and $3.55 < m_{X_{\text{inv}}} < 4.70 \text{ GeV}/c^2$. The vetoed mass regions—(1.74, 2.11), (2.93, 3.15), and (3.48, 3.55) GeV/c^2 , corresponding to $D^{(*)0}$, $\eta_c/J/\psi$, and χ_{c1} —remain viable for such an explanation [83].

Searches for long-lived particles that decay via $X \rightarrow \gamma\gamma$ are motivated by many ALP models [1, 28]. Here, X refers to a FIP that may not be completely invisible due to a lab-frame decay length on a similar scale as the detector.

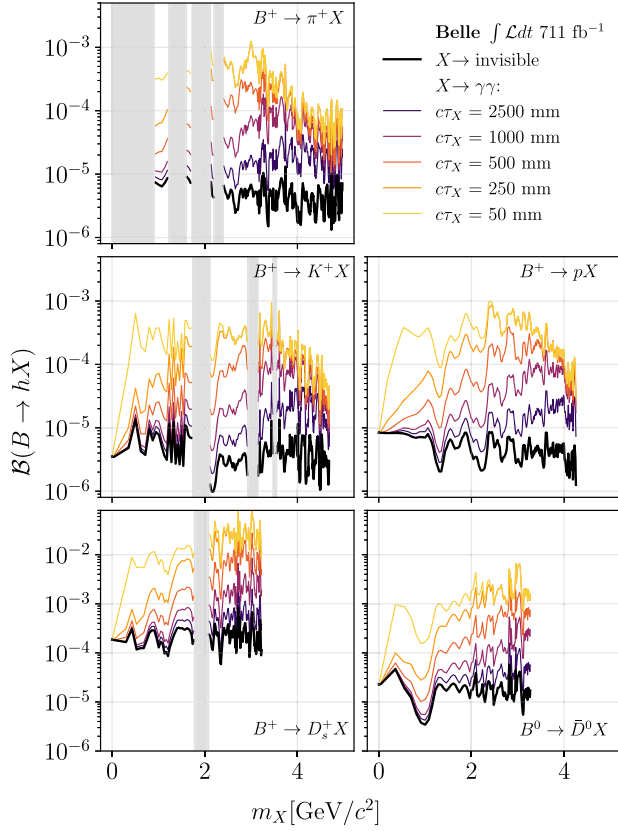


FIG. 2. Upper limits on the branching fraction $\mathcal{B}(B \rightarrow hX_{\text{inv}})$ at 90% CL as a function of $m_{X_{\text{inv}}}$ are shown in black. Replacing the invisible decay assumption with $X \rightarrow \gamma\gamma$ yields the colored limits, shown for several orders of magnitude of $c\tau_X$. Mass regions vetoed for known SM particles π^0 , $K^{(*)0}$, $D^{(*)0}$, η_c , χ_{c1} , and $\psi(2S)$ are shaded gray. Not all veto regions apply to every channel.

The sensitivity to such decays is evaluated by applying the nominal $B \rightarrow hX_{\text{inv}}$ selection criteria to the aforementioned simulated signal sample containing $B \rightarrow hX(\rightarrow \gamma\gamma)$ decays. We stress that this is not a dedicated search for $X \rightarrow \gamma\gamma$; nor is any alternative reconstruction or statistical treatment performed. Instead, the $X \rightarrow \gamma\gamma$ study serves only to quantify at what lifetimes such decays would mimic the invisible scenario under the nominal selection. These results are shown as the colored lines in Fig. 2. Since the selection criteria are designed to reject events with substantial E_{ECL} , and the decay products of $X \rightarrow \gamma\gamma$ are more likely to be detected in the ECL for smaller values of $c\tau_X$, the sensitivity is worse at shorter lifetimes.

For some benchmark masses and lifetimes, the X selection efficiency was recalculated for several other final states: e^+e^- , $\mu^+\mu^-$, $\pi^+\pi^-$, K^+K^- , $\pi\pi\eta$, and $\pi\pi\gamma$. Photon pairs, for a given m_X and τ_X , are the decay products that deposit the most energy in the ECL and therefore cause the event to fail the $E_{\text{ECL}} < 1.5$ GeV requirement. This makes the $X \rightarrow \gamma\gamma$ limits from this work, at any given $c\tau_X$, a conservative estimate for any of the other final states listed

above, several of which are interesting in the context of hadronically decaying ALP scenarios [84,85].

In summary, we present a search for invisible particles X_{inv} produced in $B^+ \rightarrow hX_{\text{inv}}$, $h = \pi^+, K^+, p, D_s^+$, and $B^0 \rightarrow \bar{D}^0 X_{\text{inv}}$ decays, using the 711 fb^{-1} Belle dataset. No significant excess is observed, and 90% upper limits are set on the branching fraction $\mathcal{B}(B \rightarrow hX_{\text{inv}})$ for all channels. We provide another set of limits under the alternative assumption that the new particle decays via $X \rightarrow \gamma\gamma$ and has a lifetime $c\tau_X$ between 10 μm and 10 m. These results provide the most stringent branching fraction exclusion limits in these channels to date and are the first search results for the channels $B^+ \rightarrow \pi^+ X_{\text{inv}}$, $B^+ \rightarrow D_s^+ X_{\text{inv}}$, and $B^0 \rightarrow \bar{D}^0 X_{\text{inv}}$.

The limits in Fig. 2 place the strongest constraints on the ALP-W coupling, several ALP-quark couplings, and the dark scalar-Higgs mixing parameter (outlined in the End Matter). Furthermore, the limits on $B^+ \rightarrow pX_{\text{inv}}$ provide the best constraints on the B -mesogenesis [86,87] parameter space, and on the b quark coupling to the lightest neutralino in R-parity-violating supersymmetry models [88].

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Data availability—The data behind the plots is publicly available from HEPData [89].

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End Matter

The decay width for the $B^+ \rightarrow K^+ a$ production process is given by Ref. [28] as $\Gamma(B^+ \rightarrow K^+ a) = m_B^3 |g_{abs}|^2 (1 - m_K^2/m_B^2)^2 f_0^2(m_a^2) \lambda_{Ka}^{1/2} / 64\pi$, with hadronic form factor $f_0(m_a^2) = 0.330 / (1 - m_a^2/37.46)$ [33] and Källén function $\lambda_{Ka} = (1 - (m_a + m_K)^2/m_B^2)(1 - (m_a -$

$m_K)^2/m_B^2)$ [90]. The quark coupling g_{abs} relates to the ALP-W coupling g_{aW} via $g_{abs} = -3\sqrt{2}G_F m_W^2 g_{aW} \sum_{q=c,t} V_{qb} V_{qs}^* f(m_q^2/m_W^2) / 16\pi^2$, with $f(x) = x[1 + x(\log x - 1)] / (1 - x^2)$, G_F the Fermi constant, V_{qs} CKM elements, and m_B , m_K , m_W , m_a , m_q the masses of the

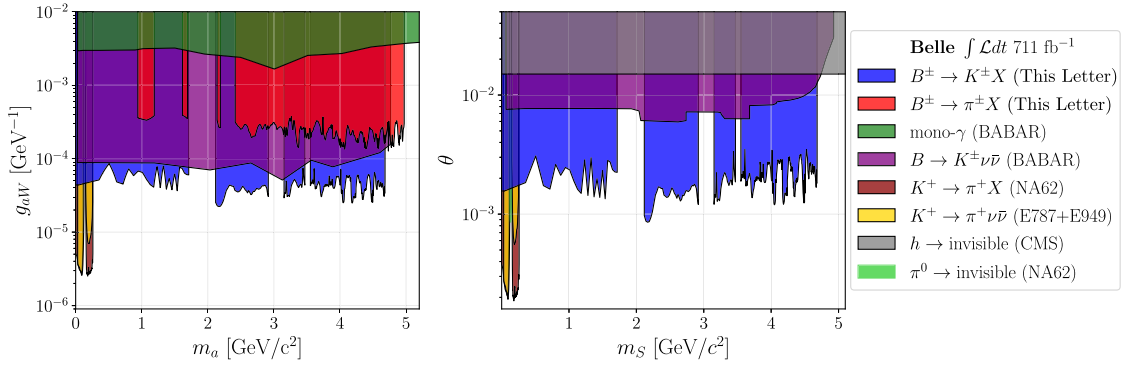


FIG. 3. Excluded regions for $m_{X_{\text{inv}}}$ up to 5.1 GeV/c² at 90% CL shown for: (a) the coupling g_{aW} in the invisible ALP scenario from Ref. [28], and (b) the mixing angle θ for the dark scalar in the missing energy scenario from Ref. [43]. Exclusions from *BABAR* [50,91], NA62 [21,23], E949 [24], and CMS [92] are overlaid for comparison.

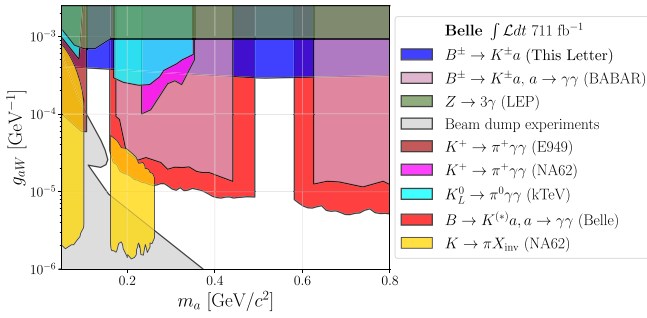


FIG. 4. Limits on the coupling strength g_{aW} assuming the ALP decays via $a \rightarrow \gamma\gamma$, including the constraints from other experiments presented in Ref. [28], with the addition of more recent constraints that appear in Ref. [14].

corresponding particles. Analogous expressions apply for $B^+ \rightarrow \pi^+ a$.

Figure 3(a) shows limits on g_{aW} for invisible ALPs. For $a \rightarrow \gamma\gamma$ decays, the lifetime follows from $\Gamma_a = g_{aW}^2 m_a^3 \sin^4 \theta_W / 64\pi$ (θ_W the Weinberg angle); the corresponding 90% CL upper limits are shown in Fig. 4.

Following Ref. [19], the limits in Fig. 2 are mapped to ALP-quark couplings g_q . The resulting exclusions in Fig. 5 illustrate the complementary sensitivity of different B decay channels.

For a dark scalar S produced in B decays, Ref. [43] gives $\Gamma(B^+ \rightarrow K^+ S) = \sqrt{2} G_F |C_{bs}|^2 (m_b + m_s)^2 (m_B^2 - m_K^2)^2 [(m_B^2 - m_K^2 - m_S^2)^2 - 4m_K^2 m_S^2]^{1/2} f_0^2(m_S^2) / [64\pi m_B^3 (m_b - m_s)^2]$, with scalar form factor $f_0(q^2)$ from Ref. [44] and Wilson

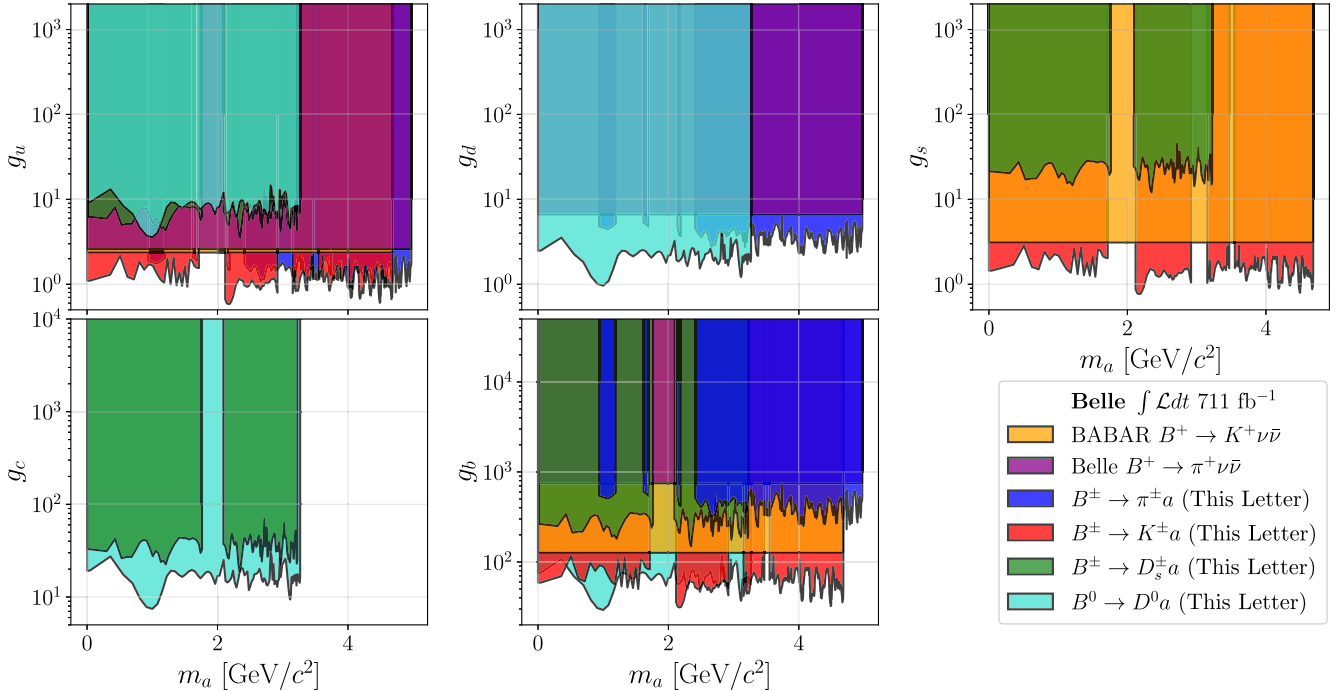


FIG. 5. 90% confidence level exclusion regions on the ALP-quark couplings described in Ref. [19].

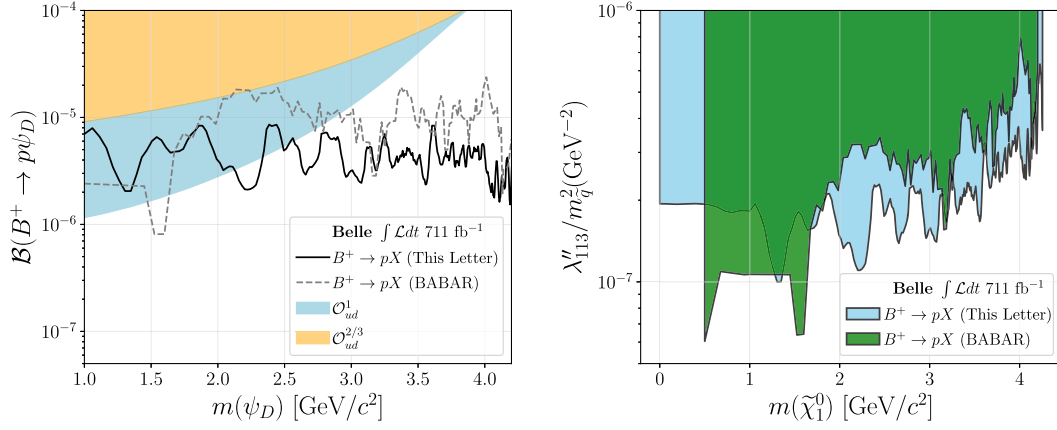


FIG. 6. Left: Theory expectation for the B -mesogenesis effective operators with 90% CL upper limits on the branching fraction $B^+ \rightarrow p\psi_D$ derived from the Belle dataset. Right: Excluded parameter space by *BABAR* and Belle (this Letter) for the RPV coupling λ''_{113} as a function of neutralino mass.

coefficient $C_{bs} = 3\sqrt{2}G_F m_t^2 V_{tb} V_{ts}^* \sin\theta / 16\pi^2 + \mathcal{O}(m_S^2/m_W^2)$, where θ is the dark scalar-Higgs mixing angle and m_t, m_S are the top quark and dark scalar masses.

Whether S decays visibly or invisibly depends on θ and the Yukawa coupling y_χ to dark fermions χ . Reference [43] gives the invisible rate $\Gamma(S \rightarrow \chi\chi) = y_\chi^2 m_S \cos^2\theta (1 - 4m_\chi^2/m_S^2)^{3/2} / 8\pi$. Assuming y_χ is large enough that $\mathcal{B}(S \rightarrow \chi\chi) \approx 1$, the limits in Fig. 2 map onto θ as shown in Fig. 3(b).

B mesogenesis is a baryogenesis mechanism in which B mesons decay to dark baryons ψ_D in the early Universe [86] via $B \rightarrow \mathcal{B}_{ij} \mathcal{M} \psi_D$, where $\mathcal{B}$ is a baryon containing quarks $i = u, c$ and $j = d, s$, and $\mathcal{M}$ is a meson. Effective operators $\mathcal{O}_{ij}$ describe each $\bar{b} \rightarrow ij\psi_D$ vertex; the proton

final state probed here constrains only $\mathcal{O}_{ud}$. Producing the observed baryon asymmetry requires $\mathcal{B}(B^+ \rightarrow \mathcal{B}_{ij} \mathcal{M} \psi_D) > 10^{-6}$ [87]. Using the multi-body to two-body relation given therein, this requirement maps onto the colored regions in Fig. 6. The $B^+ \rightarrow pX$ limit in Fig. 2 rules out B mesogenesis for dark baryon masses above $2.5 \text{ GeV}/c^2$ and between 2.15 and $2.3 \text{ GeV}/c^2$.

The R-parity violating (RPV) supersymmetric process $B^+ \rightarrow p\tilde{\chi}_0$, with $\tilde{\chi}_0$ the lightest neutralino, is also constrained by the $B^+ \rightarrow pX$ limits. Production depends on $\lambda''_{113}/m_{\tilde{q}}^2$, where $m_{\tilde{q}}$ is the squark mass. Mapping Fig. 2 onto this coupling versus neutralino mass using Ref. [88], we exclude lower coupling values than *BABAR* between $0-0.5 \text{ GeV}/c^2$ and for most masses above $2 \text{ GeV}/c^2$.