Measurement of muon neutrino induced charged current interactions without charged pions in the final state using a new T2K off-axis near detector WAGASCI-BabyMIND

K. Abe,[60] S. Abe,[59] R. Akutsu,[16] H. Alarakia-Charles,[34] Y. I. Alj Hakim,[54] S. Alonso Monsalve,[9] L. Anthony,[21] S. Aoki,[32] K. A. Apte,[21] T. Arai,[59] T. Arihara,[63] S. Arimoto,[33] Y. Ashida,[69] E. T. Atkin,[21] N. Babu,[38] V. Baranov,[39] G. J. Barker,[70] G. Barr,[47] D. Barrow,[47] P. Bates,[37] L. Bathe-Peters,[47] M. Batkiewicz-Kwasniak,[15] N. Baudis,[47] V. Berardi,[22] L. Berns,[69] S. Bhattacharjee,[38] A. Blanchet,[11] A. Blondel,[57,12] P. M. M. Boistier,[5] S. Bolognesi,[5] S. Bordoni,[12] S. B. Boyd,[70] C. Bronner,[72] A. Bubak,[55] M. Buizza Avanzini,[36] F. Cadoux,[12] N. F. Calabria,[22] S. Cao,[20] S. Cap,[12] D. Carabadjac,[36,*] S. L. Cartwright,[54] M. P. Casado,[18,†] M. G. Catanesi,[22] J. Chakrani,[35] A. Chalumeau,[57] D. Cherdack,[17] A. Chvirova,[26] J. Coleman,[37] G. Collazuol,[24] F. Cormier,[65] A. A. L. Craplet,[21] A. Cudd,[6] D. D'Ago,[24] C. Dalmazzone,[57] T. Daret,[5] P. Dasgupta,[8] C. Davis,[48] Yu. I. Davydov,[39] P. de Perio,[29] G. De Rosa,[23] T. Dealtry,[34] C. Densham,[44] A. Dergacheva,[26] R. Dharmapal Banerjee,[71] F. Di Lodovico,[31] G. Diaz Lopez,[57] S. Dolan,[11] D. Douqa,[12] T. A. Doyle,[47] O. Drapier,[36] K. E. Duffy,[47] J. Dumarchez,[57] P. Dunne,[21] K. Dygnarowicz,[68] A. Eguchi,[59] J. Elias,[50] S. Emery-Schrenk,[5] G. Erofeev,[26] A. Ershova,[36] G. Eurin,[5] D. Fedorova,[26] S. Fedotov,[26] M. Feltre,[24] L. Feng,[33] D. Ferlewicz,[57] A. J. Finch,[34] M. D. Fitton,[44] C. Forza,[24] M. Friend,[16,‡] Y. Fujii,[16,‡] Y. Fukuda,[41] Y. Furui,[63] J. García-Marcos,[14] A. C. Germer,[48] L. Giannessi,[12] C. Giganti,[57] M. Girgus,[67] V. Glagolev,[39] M. Gonin,[28] E. A. G. Goodman,[13] K. Gorshanov,[26] P. Govindaraj,[67] M. Grassi,[24] M. Guigue,[57] F. Y. Guo,[43] D. R. Hadley,[70] S. Han,[33,61] D. A. Harris,[73] R. J. Harris,[34,44] T. Hasegawa,[16,‡] C. M. Hasnip,[11] S. Hassani,[5] N. C. Hastings,[16] Y. Hayato,[60,29] I. Heitkamp,[69] D. Henaff,[5] Y. Hino,[16] J. Holeczek,[55] A. Holin,[44] T. Holvey,[47] N. T. Hong Van,[27] T. Honjo,[46] M. C. F. Hooft,[14] K. Hosokawa,[60] J. Hu,[33] A. K. Ichikawa,[69] K. Ieki,[60] M. Ikeda,[60] T. H. Ishida,[69] T. Ishida,[16,‡] M. Ishitsuka,[64] H. Ito,[32] S. Ito,[72] A. Izmaylov,[26] N. Jachowicz,[14] S. J. Jenkins,[37] C. Jesús-Valls,[11] M. Jia,[43] J. J. Jiang,[43] J. Y. Ji,[43] T. P. Jones,[34] P. Jonsson,[21] S. Joshi,[43] C. K. Jung,[43,§] M. Kabirnezhad,[21] A. C. Kaboth,[51] H. Kakuno,[63] J. Kameda,[60] S. Karpova,[12] V. S. Kasturi,[12] Y. Kataoka,[60] T. Katori,[31] A. Kawabata,[30] Y. Kawamura,[46] M. Kawaue,[33] E. Kearns,[2,§] M. Khabibullin,[26] A. Khotjantsev,[26] T. Kikawa,[33] S. King,[31] V. Kiseeva,[39] J. Kisiel,[55] A. Klustová,[21] L. Kneale,[54] H. Kobayashi,[59] Sota. R. Kobayashi,[69] L. Koch,[19] S. Kodama,[59] M. Kolupanova,[26] A. Konaka,[65] L. L. Kormos,[34] Y. Koshio,[45,§] K. Kowalik,[42] Y. Kudenko,[26,‖] Y. Kudo,[72] A. Kumar Jha,[14] R. Kurjata,[68] V. Kurochka,[26] T. Kutter,[38] L. Labarga,[1] M. Lachat,[50] K. Lachner,[9] J. Lagoda,[42] S. M. Lakshmi,[55] M. Lamers James,[70] A. Langella,[23] D. H. Langridge,[51] J.-F. Laporte,[5] D. Last,[50] N. Latham,[31] M. Laveder,[24] L. Lavitola,[23] M. Lawe,[34] D. Leon Silverio,[58] S. Levorato,[24] S. V. Lewis,[31] B. Li,[9] C. Lin,[21] R. P. Litchfield,[13] S. L. Liu,[43] W. Li,[47] A. Longhin,[24] A. Lopez Moreno,[31] L. Ludovici,[25] X. Lu,[70] T. Lux,[18] L. N. Machado,[13] L. Magaletti,[22] K. Mahn,[40] K. K. Mahtani,[43] M. Mandal,[42] S. Manly,[50] A. D. Marino,[6] D. G. R. Martin,[21] D. A. Martinez Caicedo,[58] L. Martinez,[18] M. Martini,[57,¶] T. Matsubara,[16] R. Matsumoto,[62] V. Matveev,[26] C. Mauger,[48] K. Mavrokoridis,[37] N. McCauley,[37] K. S. McFarland,[50] C. McGrew,[43] J. McKean,[21] A. Mefodiev,[26] L. Mellet,[40] C. Metelko,[37] M. Mezzetto,[24] S. Miki,[60] V. Mikola,[13] E. W. Miller,[21] A. Minamino,[72] O. Mineev,[26] S. Mine,[60,4] J. Mirabito,[2] M. Miura,[60,§] S. Moriyama,[60,§] S. Moriyama,[72] P. Morrison,[13] Th. A. Mueller,[36] D. Munford,[17] A. Muñoz,[36,28] L. Munteanu,[11] Y. Nagai,[8] T. Nakadaira,[16,‡] K. Nakagiri,[60] M. Nakahata,[60,29] Y. Nakajima,[59] K. D. Nakamura,[69] A. Nakano,[69] Y. Nakano,[66] S. Nakayama,[60,29] T. Nakaya,[33,29] K. Nakayoshi,[16,‡] C. E. R. Naseby,[21] D. T. Nguyen,[10] V. Q. Nguyen,[36] K. Niewczas,[14] S. Nishimori,[16] Y. Nishimura,[30] Y. Noguchi,[60] T. Nosek,[42] F. Nova,[44] J. C. Nugent,[21] H. M. O'Keeffe,[34] L. O'Sullivan,[19] R. Okazaki,[30] W. Okinaga,[59] K. Okumura,[61,29] T. Okusawa,[46] N. Onda,[33] N. Ospina,[22] L. Osu,[36] N. Otani,[33] Y. Oyama,[16,‡] V. Paolone,[49] J. Pasternak,[21] D. Payne,[37] T. P. D. Peacock,[54] M. Pfaff,[21] L. Pickering,[44] G. Pintaudi,[72] B. Popov,[57,**] A. J. Portocarrero Yrey,[16] M. Posiadala-Zezula,[67] Y. S. Prabhu,[67] H. Prasad,[71] F. Pupilli,[24] B. Quilain,[28,36] P. T. Quyen,[20,††] E. Radicioni,[22] B. Radics,[73] M. A. Ramirez Delgado,[48] R. Ramsden,[31] P. N. Ratoff,[34] M. Reh,[6] G. Reina,[19] C. Riccio,[43] D. W. Riley,[13] E. Rondio,[42] S. Roth,[52] N. Roy,[73] A. Rubbia,[9] L. Russo,[57] A. Rychter,[68] W. Saenz,[57] K. Sakashita,[16,‡] S. Samani,[12] F. Sánchez,[12] E. M. Sandford,[37] Y. Sato,[64] T. Schefke,[38] C. M. Schloesser,[12] K. Scholberg,[7,§] M. Scott,[21] Y. Seiya,[46,‡‡] T. Sekiguchi,[16,‡] H. Sekiya,[60,29,§] T. Sekiya,[63] D. Seppala,[40] D. Sgalaberna,[9] A. Shaikhiev,[26] M. Shiozawa,[60,29] Y. Shiraishi,[45] A. Shvartsman,[26] N. Skrobova,[26] K. Skwarczynski,[51] D. Smyczek,[52] M. Smy,[4] J. T. Sobczyk,[71] H. Sobel,[4,29] F. J. P. Soler,[13] A. J. Speers,[34] R. Spina,[22] A. Srivastava,[19] P. Stowell,[54] Y. Stroke,[26] I. A. Suslov,[39] A. Suzuki,[32] S. Y. Suzuki,[16,‡] M. Tada,[16,‡] S. Tairafune,[69] A. Takeda,[60] Y. Takeuchi,[32,29] K. Takeya,[45] H. K. Tanaka,[60,§] H. Tanigawa,[16] A. Teklu,[43] V. V. Tereshchenko,[39] N. Thamm,[52] C. Touramanis,[37] N. Tran,[33] T. Tsukamoto,[16,‡] M. Tzanov,[38] Y. Uchida,[21] M. Vagins,[29,4] M. Varghese,[18] I. Vasilyev,[39] G. Vasseur,[5] E. Villa,[11,12] U. Virginet,[57] T. Vladisavljevic,[44] T. Wachala,[15] S.-i. Wada,[32] D. Wakabayashi,[69] H. T. Wallace,[54] J. G. Walsh,[40] L. Wan,[2] D. Wark,[44,47] M. O. Wascko,[47,44] A. Weber,[19] R. Wendell,[33] M. J. Wilking,[53] C. Wilkinson,[35] J. R. Wilson,[31] K. Wood,[35] C. Wret,[21] J. Xia,[56] K. Yamamoto,[46,‡‡] T. Yamamoto,[46] C. Yanagisawa,[43,§§] Y. Yang,[47] T. Yano,[60] K. Yasutome,[33] N. Yershov,[26] U. Yevarouskaya,[43] M. Yokoyama,[59,§]

Y. Yoshimoto,[59] N. Yoshimura,[33] R. Zaki,[73] A. Zalewska,[15] J. Zalipska,[42] G. Zarnecki,[15] J. Zhang,[65,3] X. Y. Zhao,[9] H. Zheng,[43] H. Zhong,[32] T. Zhu,[21] M. Ziembicki,[68] E. D. Zimmerman,[6] M. Zito,[57] and S. Zsoldos[31]

(T2K Collaboration)

[1]*University Autonoma Madrid, Department of Theoretical Physics, 28049 Madrid, Spain*
[2]*Boston University, Department of Physics, Boston, Massachusetts, USA*
[3]*University of British Columbia, Department of Physics and Astronomy, Vancouver, British Columbia, Canada*
[4]*University of California, Irvine, Department of Physics and Astronomy, Irvine, California, USA*
[5]*IRFU, CEA, Université Paris-Saclay, F-91191 Gif-sur-Yvette, France*
[6]*University of Colorado at Boulder, Department of Physics, Boulder, Colorado, USA*
[7]*Duke University, Department of Physics, Durham, North Carolina, USA*
[8]*Eötvös Loránd University, Department of Atomic Physics, Budapest, Hungary*
[9]*ETH Zurich, Institute for Particle Physics and Astrophysics, Zurich, Switzerland*
[10]*VNU University of Science, Vietnam National University, Hanoi, Vietnam*
[11]*CERN European Organization for Nuclear Research, CH-1211 Genéve 23, Switzerland*
[12]*University of Geneva, Section de Physique, DPNC, Geneva, Switzerland*
[13]*University of Glasgow, School of Physics and Astronomy, Glasgow, United Kingdom*
[14]*Ghent University, Department of Physics and Astronomy, Proeftuinstraat 86, B-9000 Gent, Belgium*
[15]*H. Niewodniczanski Institute of Nuclear Physics PAN, Cracow, Poland*
[16]*High Energy Accelerator Research Organization (KEK), Tsukuba, Ibaraki, Japan*
[17]*University of Houston, Department of Physics, Houston, Texas, USA*
[18]*Institut de Fisica d'Altes Energies (IFAE)—The Barcelona Institute of Science and Technology, Campus UAB, Bellaterra (Barcelona) Spain*
[19]*Institut für Physik, Johannes Gutenberg-Universität Mainz, Staudingerweg 7, 55128 Mainz, Germany*
[20]*Institute For Interdisciplinary Research in Science and Education (IFIRSE), ICISE, Quy Nhon, Vietnam*
[21]*Imperial College London, Department of Physics, London, United Kingdom*
[22]*INFN Sezione di Bari and Università e Politecnico di Bari, Dipartimento Interuniversitario di Fisica, Bari, Italy*
[23]*INFN Sezione di Napoli and Università di Napoli, Dipartimento di Fisica, Napoli, Italy*
[24]*INFN Sezione di Padova and Università di Padova, Dipartimento di Fisica, Padova, Italy*
[25]*INFN Sezione di Roma and Università di Roma "La Sapienza," Roma, Italy*
[26]*Institute for Nuclear Research of the Russian Academy of Sciences, Moscow, Russia*
[27]*International Centre of Physics, Institute of Physics (IOP), Vietnam Academy of Science and Technology (VAST), 10 Dao Tan, Ba Dinh, Hanoi, Vietnam*
[28]*ILANCE, CNRS—University of Tokyo International Research Laboratory, Kashiwa, Chiba 277-8582, Japan*
[29]*Kavli Institute for the Physics and Mathematics of the Universe (WPI), The University of Tokyo Institutes for Advanced Study, University of Tokyo, Kashiwa, Chiba, Japan*
[30]*Keio University, Department of Physics, Kanagawa, Japan*
[31]*King's College London, Department of Physics, Strand, London WC2R 2LS, United Kingdom*
[32]*Kobe University, Kobe, Japan*
[33]*Kyoto University, Department of Physics, Kyoto, Japan*
[34]*Lancaster University, Physics Department, Lancaster, United Kingdom*
[35]*Lawrence Berkeley National Laboratory, Berkeley, California, USA*
[36]*Ecole Polytechnique, IN2P3-CNRS, Laboratoire Leprince-Ringuet, Palaiseau, France*
[37]*University of Liverpool, Department of Physics, Liverpool, United Kingdom*
[38]*Louisiana State University, Department of Physics and Astronomy, Baton Rouge, Louisiana, USA*
[39]*Joint Institute for Nuclear Research, Dubna, Moscow Region, Russia*
[40]*Michigan State University, Department of Physics and Astronomy, East Lansing, Michigan, USA*
[41]*Miyagi University of Education, Department of Physics, Sendai, Japan*
[42]*National Centre for Nuclear Research, Warsaw, Poland*
[43]*State University of New York at Stony Brook, Department of Physics and Astronomy, Stony Brook, New York, USA*
[44]*STFC, Rutherford Appleton Laboratory, Harwell Oxford, and Daresbury Laboratory, Warrington, United Kingdom*
[45]*Okayama University, Department of Physics, Okayama, Japan*
[46]*Osaka Metropolitan University, Department of Physics, Osaka, Japan*
[47]*Oxford University, Department of Physics, Oxford, United Kingdom*

[48]University of Pennsylvania, Department of Physics and Astronomy, Philadelphia, Pennsylvania, USA
[49]University of Pittsburgh, Department of Physics and Astronomy, Pittsburgh, Pennsylvania, USA
[50]University of Rochester, Department of Physics and Astronomy, Rochester, New York, USA
[51]Royal Holloway University of London, Department of Physics, Egham, Surrey, United Kingdom
[52]RWTH Aachen University, III. Physikalisches Institut, Aachen, Germany
[53]School of Physics and Astronomy, University of Minnesota, Minneapolis, Minnesota, USA
[54]University of Sheffield, School of Mathematical and Physical Sciences, Sheffield, United Kingdom
[55]University of Silesia, Institute of Physics, Katowice, Poland
[56]SLAC National Accelerator Laboratory, Stanford University, Menlo Park, California, USA
[57]Sorbonne Université,
CNRS/IN2P3, Laboratoire de Physique Nucléaire et de Hautes Energies (LPNHE), Paris, France
[58]South Dakota School of Mines and Technology,
501 East Saint Joseph Street, Rapid City, SD 57701, South Dakota, USA
[59]University of Tokyo, Department of Physics, Tokyo, Japan
[60]University of Tokyo, Institute for Cosmic Ray Research, Kamioka Observatory, Kamioka, Japan
[61]University of Tokyo, Institute for Cosmic Ray Research,
Research Center for Cosmic Neutrinos, Kashiwa, Japan
[62]Institute of Science Tokyo, Department of Physics, Tokyo, Japan
[63]Tokyo Metropolitan University, Department of Physics, Tokyo, Japan
[64]Tokyo University of Science, Faculty of Science and Technology,
Department of Physics, Noda, Chiba, Japan
[65]TRIUMF, Vancouver, British Columbia, Canada
[66]University of Toyama, Department of Physics, Toyama, Japan
[67]University of Warsaw, Faculty of Physics, Warsaw, Poland
[68]Warsaw University of Technology, Institute of Radioelectronics and Multimedia Technology, Warsaw, Poland
[69]Tohoku University, Faculty of Science, Department of Physics, Miyagi, Japan
[70]University of Warwick, Department of Physics, Coventry, United Kingdom
[71]Wroclaw University, Faculty of Physics and Astronomy, Wroclaw, Poland
[72]Yokohama National University, Department of Physics, Yokohama, Japan
[73]York University, Department of Physics and Astronomy, Toronto, Ontario, Canada

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We report a flux-integrated cross section measurement of muon neutrino interactions on water and hydrocarbon via charged current reactions without charged pions in the final state with the WAGASCI-BabyMIND detector, which was installed in the T2K near detector hall in 2018. The detector is located 1.5° off-axis and is exposed to a more energetic neutrino flux than ND280, another T2K near detector, which is located at a different off-axis position. The total flux-integrated cross section is measured to be $1.26 \pm 0.18(\mathrm{stat} + \mathrm{syst}) \times 10^{-39}\ \mathrm{cm}^2/\mathrm{nucleon}$ on CH and $1.44 \pm 0.21(\mathrm{stat} + \mathrm{syst}) \times 10^{-39}\ \mathrm{cm}^2/\mathrm{nucleon}$ on H_2O. These results are compared to model predictions provided by the NEUT v5.3.2 and GENIE v2.8.0 Monte Carlo generators and the measurements are compatible with these models. Differential cross sections in muon momentum and cosine of the muon scattering angle are also reported. This is the first such measurement reported with the WAGASCI-BabyMIND detector and utilizes the 2020 and 2021 datasets.

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[*]Also at Université Paris-Saclay.
[†]Also at Departament de Fisica de la Universitat Autonoma de Barcelona, Barcelona, Spain.
[‡]Also at J-PARC, Tokai, Japan.
[§]Also an affiliated member at Kavli IPMU (WPI), The University of Tokyo, Japan.
[‖]Also at Moscow Institute of Physics and Technology (MIPT), Moscow region, Russia and National Research Nuclear University "MEPhI," Moscow, Russia.
[¶]Also at IPSA-DRII, Paris, France.
[**]Also at JINR, Dubna, Russia.
[††]Also at the Graduate University of Science and Technology, Vietnam Academy of Science and Technology, Ho Chi Min city, Vietnam.
[‡‡]Also at Nambu Yoichiro Institute of Theoretical and Experimental Physics (NITEP), Osaka, Japan.
[§§]Also at BMCC/CUNY, Science Department, New York, New York, USA.

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I. INTRODUCTION

In order to improve our understanding of the phenomenon of neutrino oscillations, a new generation of experiments is required with increased detector mass, higher-power beam, and better near detectors yielding improved statistics and sensitivity. Within the paradigm of three Dirac neutrinos with their flavor states being linear combinations of their mass eigenstates, as determined by the Pontecorvo-Maki-Nakagawa-Sakata (PMNS) mixing matrix [1], the remaining major unknowns are the ordering of the mass eigenstates and the value of the *CP* symmetry violating parameter. Together with the hypothetical existence of sterile neutrinos these are the main questions to be addressed by several long- and short-baseline neutrino oscillation experiments. The precision of measurements performed in experiments like T2K [2], NOvA [3], Hyper-Kamiokande [4], and DUNE [5] relies strongly on reducing the systematic uncertainties originating from our limited knowledge of neutrino-nucleus cross sections [6]. T2K uses a neutrino beam peaked in the sub-GeV energy range, hence the main neutrino interaction channel is charged current quasielastic (CCQE) scattering with a nucleon. This interaction mode is described with the standard Llewellyn Smith formalism [7] but it is far from being fully understood due to the axial structure of the weak current and complications introduced through nuclear effects, as neutrino oscillation experiments use complex nuclear targets such as carbon, water, or argon. Other interaction modes bring their own unknowns and this motivates experimental efforts to measure neutrino cross sections with different fluxes, targets, and definitions of the experimental signal.

The T2K experiment uses Super-Kamiokande, a water Cherenkov detector [8], as the far detector to measure neutrinos after oscillation, and ND280 [9] as the near detector, measuring the neutrino flux before oscillation. The primary target material in ND280 is hydrocarbon and, therefore, it is highly desirable to also measure neutrino interactions on a water target at the near detector site. WAGASCI-BabyMIND with its mixed water and hydrocarbon composition allows the simultaneous measurement of the neutrino cross section on both of these target materials, motivating its construction and inclusion within the T2K experiment.

The WAGASCI-BabyMIND is the collective name of the detectors shown in Fig. 1. It was installed in 2018 at the main ND280 [10] complex in a position 1.5° off-axis on the B2 floor of the Neutrino Monitoring building of the Japan-Proton Accelerator Research Complex (J-PARC). Together, the WAter Grid And SCIntillator modules (WAGASCI), proton module (PM), wall muon range detectors (WMs), and Baby Magnetized Iron Neutrino Detector (BabyMIND) form an integrated system of detectors. In this paper, we present new cross section measurements made by the WAGASCI-BabyMIND on both H_2O and CH targets.

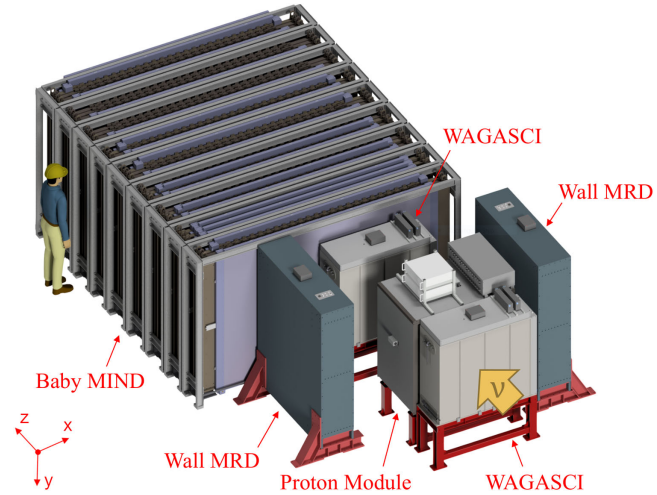

FIG. 1. Configuration of the WAGASCI-BabyMIND. A large orange arrow represents the neutrino beam direction.

For the neutrinos provided by the J-PARC accelerator, at the WAGASCI-BabyMIND position the energy spectrum has a peak around 0.7 GeV, compared to 0.6 GeV at the 2.5° off-axis position where the ND280 detector is located, as shown in Fig. 2.

At these higher neutrino energies, interactions other than CCQE, such as pion production and multinucleon knock-out, become more significant compared to lower neutrino energy events seen by ND280. They can contribute to the experimental signal measured in this paper defined as a muon and no charged pions in the final state. We work with final states, as a charged pion may be produced and then absorbed, or it may be below the tracking threshold, resulting in no reconstructed track.

We measured both flux-integrated cross sections and also the differential cross section in the resultant lepton's momentum and the cosine of it's scattering angle.

The current statistics available for physics analysis are 2.96×10^{20} protons on target (POT) in the neutrino mode

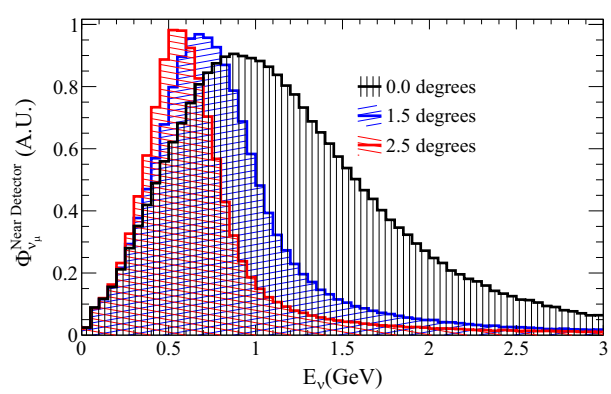

FIG. 2. Neutrino flux produced by the J-PARC accelerator at different off-axis angles. The WAGASCI-BabyMIND is located 1.5° off-axis, where the neutrino flux is peaked at 0.7 GeV.

accumulated since 2018. This is compared to the ND280 statistics of 9.78×10^{20} accumulated since 2010. With this dataset it was possible to extract the one-dimensional differential cross sections.

The results presented in this paper follow previous cross section measurements on a standalone WAGASCI module [11]. Here we report the first measurement with the full WAGASCI-BabyMIND setup. The results reported in the paper are the first obtained using a new near detector in T2K with a water component and measure the carbon/oxygen cross section ratio at a higher energy than ND280.

Our paper is organized as follows. In Sec. II the T2K experimental setup is described, including a detailed description of the WAGASCI-BabyMIND in Sec. II B. The simulation and selection of events is explained in Sec. III. In Sec. IV, the methods and calculation formulae are described. The sources of systematic uncertainty are reported in Sec. V. We validated our statistical approach and selected samples with simulated data studies, and the results of the studies are briefly summarized in Sec. VI. In Sec. VII, we present the integrated and two differential cross section results on H_2O and CH targets. The paper is concluded in Sec. VIII.

II. THE T2K EXPERIMENT

The T2K experiment has achieved several major milestones, including the first observation of electron neutrino appearance in a muon neutrino beam [12] and precision measurements of θ_{23}—a key parameter in the PMNS mixing matrix [13]. Moreover, T2K recently demonstrated sensitivity to measuring δ_{CP}, a parameter of the PMNS matrix responsible for the violation of the CP symmetry in neutrino interactions [14,15]. These observations are crucial for understanding the fundamental properties of neutrinos and their role in the Universe [16].

A. The muon neutrino beam

The T2K experiment utilizes a muon neutrino beam produced at the J-PARC facility. Protons are accelerated to 30 GeV in stages by three accelerators [17]. These high-energy protons collide with a graphite target producing secondary particles, predominantly pions. The pions are focused in the forward direction by three magnetic horns, which also defocus particles with the wrong charge, thereby enhancing the purity of the neutrino beam. As these pions travel through a 96-m-long decay pipe they decay, predominantly producing muon neutrinos or muon antineutrinos in either forward horn current or reverse horn current mode.

B. The WAGASCI-BabyMIND

Near detectors, such as the WAGASCI-BabyMIND [11] shown in Fig. 1 and ND280 [10], measure the unoscillated neutrino flux. This allows for detailed measurements of neutrino interactions and cross sections before oscillation, helping to constrain the oscillation measurements at the far detector and deepening our understanding of neutrino interactions in the energy range of interest.

In the remainder of this paper, the WAGASCI and PM detectors are occasionally referred to as "vertex" detectors, as the neutrino interactions in these detectors were considered signals for cross section extraction. Meanwhile, the BabyMIND and WM detectors are referred to as "muon range detectors" (MRDs), as their primary function is to track muons resulting from neutrino interactions. The BabyMIND and WM detectors were never used as target detectors in this paper.

All subdetectors of the WAGASCI-BabyMIND use the same principle to track the particles from neutrino interactions. They are composed of scintillator bars of various lengths and shapes, inside which are inserted wavelength-shifting fibers that gather and transport scintillation light to a multipixel photon counter (MPPC).

The WAGASCI serves as the primary water target for neutrinos and consists of a three-dimensional grid of scintillators immersed in water, allowing for high signal purity. The internal structure and dimensions are explained in detail in Ref. [11].

The PM is a scintillator tracking module which complements the WAGASCI by providing a purely hydrocarbon target. It is used for estimating background events that originate in the WAGASCI scintillators.

The fiducial mass of the PM is 313 kg of CH and that of the WAGASCI is 229 kg of H_2O and 62 kg of CH in total. By combining events from both the WAGASCI and the PM in the cross section fit, we can decorrelate the cross sections on water and hydrocarbon. A similar strategy was employed by the ND280 detector, as described in Ref. [18]. The geometry of the PM is briefly discussed in Ref. [2], while the performance of the scintillator bars is described in Ref. [19].

A preliminary cross section measurement [11] was performed between 2017 and 2018 using only one WAGASCI module and the PM as target detectors and an INGRID module [20] as a downstream muon range detector. In the measurement presented in this paper, we have improved the detectable phase space of the downrange muons by replacing the INGRID module with two new detectors:

(1) One BabyMIND detector, installed downstream of the WAGASCI and made of 33 magnetized iron planes and 18 scintillator planes. It provides the capability to identify the charge of muons by the curvature of their tracks and precisely measure their momentum by measuring their penetration distance. A more in-depth description of the structure and performance can be found in [21,22]. The BabyMIND and WAGASCI are not aligned along the flux axis because of the narrow available space in the B2 pit.

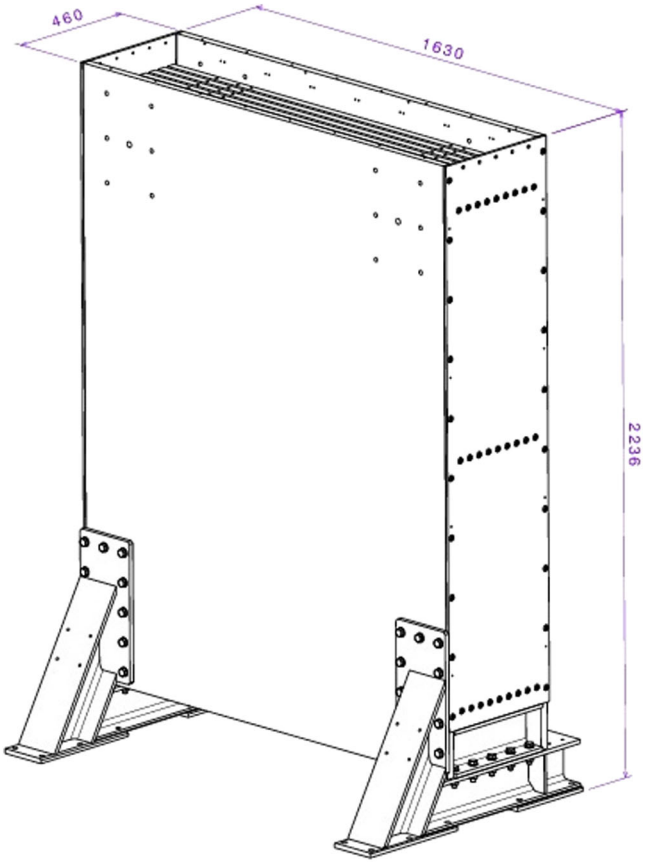

FIG. 3. External dimensions of one of the WM detectors with a size in mm. It consists of 11 layers of iron plate (each 1.8 m high, 1.6 m long, and 3 cm thick) and 10 layers of scintillator. Each layer of scintillator is made up of eight plastic scintillator plates, each 1.8 m high, 0.2 m long, and 7 mm thick.

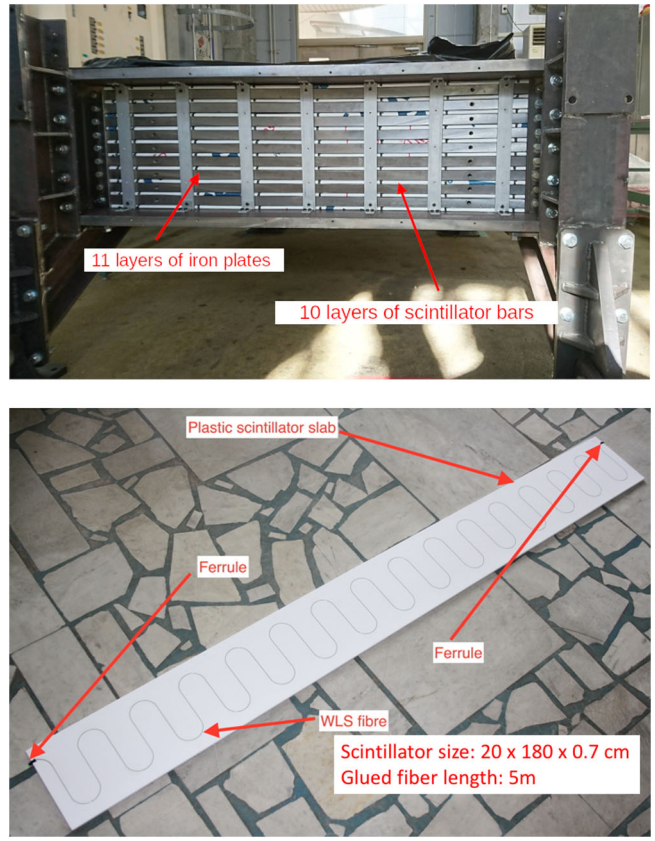

FIG. 4. Internal structure of one of the WM detectors. The structure and size of both detectors is identical. Top view: view of the WM from the bottom with the lid opened and before the readout electronics were installed. Bottom view: a single scintillator bar where the S-shape pattern of the wavelength-shifting fiber is clearly visible.

(2) Two WM detectors were installed on either side of the WAGASCI. They consist of ten scintillator tracking planes interleaved with iron planes and can detect muon tracks at a high angle relative to the beam direction, enhancing the detection efficiency for such events and increasing the observable phase space of the neutrino interaction measurements. The mechanical structure is illustrated in Figs. 3 and 4. Since these scintillators have a large width relative to their thickness, wavelength-shifting fibers (Kuraray Y-11) with a diameter of 1.0 mm were embedded in a wavy pattern (S-shape), as shown in Fig. 4, otherwise, the light yield from a hit would be decreased due to the scintillator attenuation. As a result, the wavelength-shifting fibers become longer, and both sides were read out to maximize the light yield and provide timing information by comparing the relative readout time. The skewed position of the WMs, seen in Fig. 1, was chosen to maximize the angular coverage.

Thus, for the first time, a measurement was done on the complete and final set of detectors. In this analysis, these three MRDs were not used as target detectors.

III. SIGNAL DEFINITIONS AND SELECTION STRATEGY

A. Signal and sideband definitions

The signal considered in this analysis was a muon neutrino charged current interaction on CH or H_2O targets without charged pions in the final state. Unlike other T2K CC0π cross sections, events with a neutral pion in the final state were accepted within the CC0$\pi^{\pm}$ sample since WAGASCI-BabyMIND is not capable of identifying these kind of shower events.

Charged pions, however, can be identified in the detector (see Sec. III F for details). The H_2O and CH mass ratio in WAGASCI is 4:1, hence samples of events with a vertex inside a WAGASCI module include both H_2O and CH interactions, whereas samples of events with a vertex inside the PM include only CH interactions. We performed a simultaneous fit of H_2O and CH when calculating the measured cross sections to decouple these contributions. The fit results reflect the difference between the cross sections of CH and H_2O, which was one of the goals of this analysis.

The dominant background to the CC0$\pi^{\pm}$ signal comes from CC1$\pi^{\pm}$ events when a charged pion was misidentified as a muon or was not reconstructed. We defined the sideband as CC1$\pi^{\pm}$ to give data-based constraints on this interaction process in the cross section fitting (see Sec. IV for details). Furthermore, there may be out-of-fiducial-volume (OOFV) background events whose secondary particles penetrate the fiducial volume and contaminate our signal events. The main components of this background were cosmic muons and the interaction of beam neutrinos with the concrete walls of the experimental hall, which can produce secondary particles that contaminate signal events. A "sand muon" sample is mainly produced in the sand or concrete wall surrounding the detector hall and can be selected as single track events (usually a muon) originating outside the fiducial volume, going through the first layer of WAGASCI and reaching one of the downstream muon detectors. They were usually discarded as background, but can be used as a tool for reconstruction studies, especially in cases like ours where the statistics of the signal sample were relatively low.

B. Monte Carlo simulation

The selection criteria were studied using Monte Carlo (MC) simulations. A MC framework was developed to generate simulated datasets for this analysis with the approach consistent with that adopted in the previous analysis [11]. Simulated datasets for each interaction target were produced and included the initial neutrino flux properties, particle information, hit/track information, etc. The T2K neutrino flux at 1.5° off-axis was simulated using the T2K package JNUBEAM (version 2021.2) [23]. The output of the simulated flux information was fed into the T2K neutrino interaction generator, NEUT (version 5.3.2) [24]. Using the kinematic variables of the generated final-state particles of the simulated neutrino-nucleus interaction as input, the detector response was then simulated by Geant4 (version 4.10.6.2) [25] with the "QGSP BERT" model, which also simulates the subsequent secondary or tertiary interactions within the detector material.

C. Reconstruction

The reconstruction techniques were based on those implemented for the previous analysis [11] but extended so that the methods could be applied to all the detectors, including the magnetized detector, BabyMIND. The modifications were done by tuning the reconstruction parameters on a detector-by-detector basis. The track reconstruction process was composed of three steps: track seeding, track matching, and reconstruction of track properties. The track seeding tries to find track candidates using hit information. After track candidates were found in each detector, tracks were connected between multiple detectors. Once a matched track was reconstructed, the algorithm reconstructed a vertex by identifying the most upstream hit of the matched track. Finally, we extracted track parameters such as momentum, angle, charge, and particle type based on the reconstructed tracks.

D. Signal purity and efficiency

We set cut values as part of the event selection to maximize the figure of merit defined by $N_{\mathrm{sig}}/\sqrt{N_{\mathrm{sig}}+N_{\mathrm{bg}}}$, where $N_{\mathrm{sig(bg)}}$ was the number of signal (background) events. As the figure of merit depends on the signal purity and efficiency, increasing purity whilst maintaining the signal efficiency as much as possible was the key to optimizing the cut values. Signal purity (ρ) and efficiency (ϵ) are defined by

$$\rho = \frac{N_{\mathrm{sig,allsel}}}{N_{\mathrm{allsel}}}, \qquad \epsilon = \frac{N_{\mathrm{sig,allsel}}}{N_{\mathrm{sig}}}, \tag{1}$$

where $N_{\mathrm{sig,allsel}}$ means the number of signal events satisfying all selection criteria and N_{allsel} is the total number of events passing all the selection criteria.

E. Phase-space restrictions

Phase-space restrictions on the cosine of the muon angle ($\cos\theta_\mu$) and the muon momentum (p_μ) were imposed in this analysis to maintain high signal efficiency in the selected sample. These restrictions were $\cos\theta_\mu > 0.34$ (i.e., $\theta_\mu < 70^o$) and $p_\mu > 300$ MeV/c.

F. Selection criteria

The flow of cuts used in this analysis is shown in Fig. 5. In this analysis, we used only events where a muon candidate produced in a vertex detector was matched with either BabyMIND or one of the WMs. Unmatched events were rejected with these criteria defining the "preselection." The subsequent cut criteria are described as follows.

1. Fiducial volume

We defined a fiducial volume cut for each of the vertex detectors. The fiducial volume cut played an important role in suppressing the beam-induced muon background. Figure 6 shows the comparisons of the vertex distributions after preselection and the fiducial volume cut; the events selected by these cuts are defined as the control sample. The coordinate system used in Fig. 6 is the same as defined in Fig. 1. For each detector the origins of the X and Y are the center of the scintillator and that of Z is the most downstream scintillator location.

The data and MC differed by 10% for the WAGASCI sample. A possible reason for the smaller number of MC events compared to the data was that some tracks were misreconstructed due to less efficient MPPC channels in the WAGASCIs. We found the data-MC agreement, especially for the vertex Z position, was improved by lowering

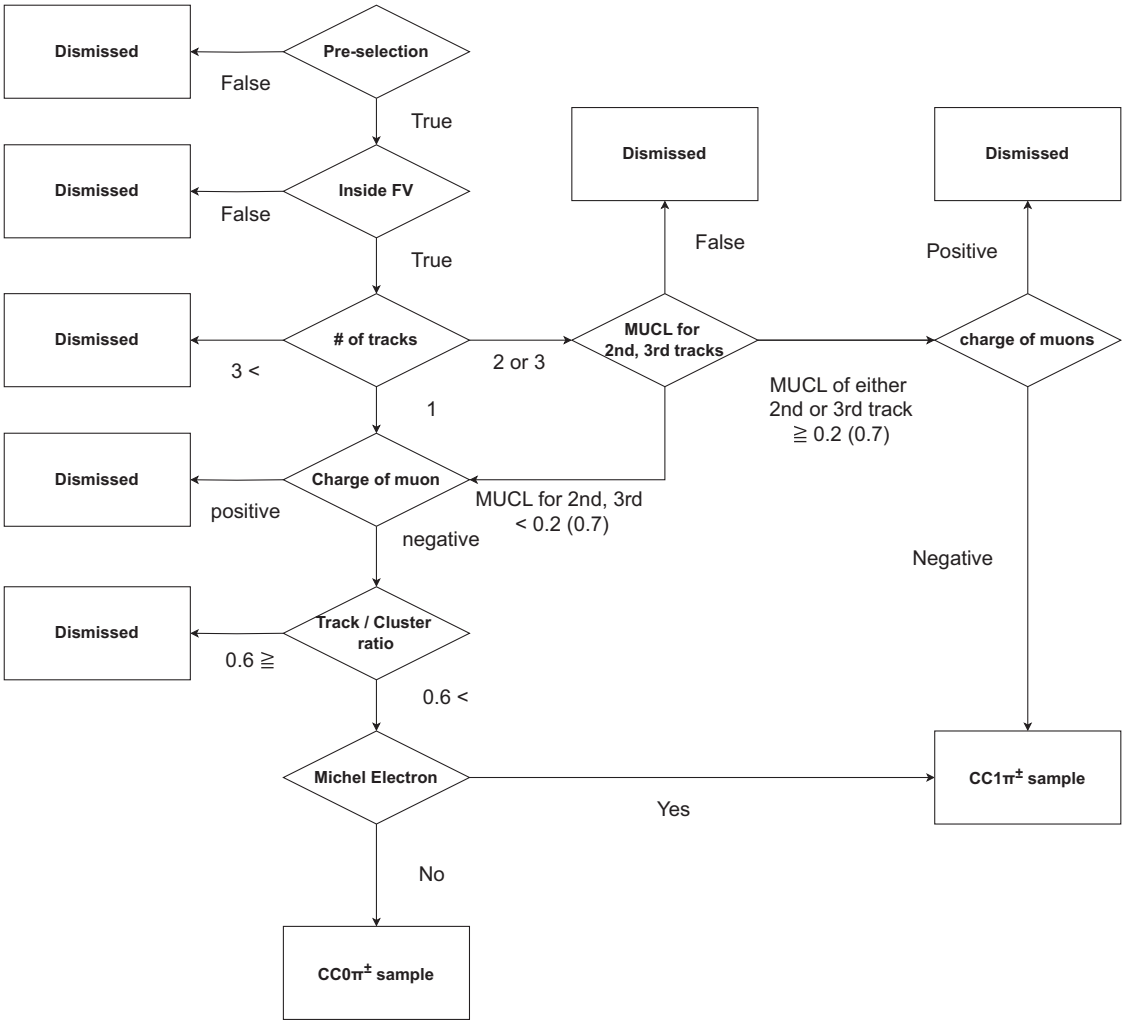

FIG. 5. Overview of the selection criteria for the CC0$\pi^{\pm}$ and CC1$\pi^{\pm}$ samples.

the hit detection efficiency of several MPPC channels in the WAGASCIs in the simulation. The difference in the number of selected events between the nominal and modified detection efficiency of MPPC channels was accounted for as one of the detector systematic uncertainties for this analysis.

2. Number of tracks

In the CC0$\pi^{\pm}$ sample, one muon and up to two protons were expected in the final state. When the number of tracks exceeded three, the purity of the CC0$\pi^{\pm}$ events in the selected sample was low. In this analysis, only events with at most three tracks were selected. This cut reduced the background due to ν_{μ} charged current (CC) interactions other than CC0$\pi^{\pm}$ and CC1$\pi^{\pm}$ which were dominated by deep inelastic scattering (DIS).

3. Particle identification

When there was only one track associated with an event, that track was taken as the muon candidate. The CC0$\pi^{\pm}$ events sometimes have multiple tracks if a proton or kaon undergoes secondary interactions. In that case, we used particle identification (PID) on all tracks except the longest matching track, which was always assumed to be a muon. We introduced a discriminator, "muon confidence level (MUCL)," for the particle identification by energy deposition [26]. MUCL is defined by

$$\mathrm{MUCL} = P \times \sum_{i=0}^{n=1} \frac{(-\ln P)^i}{i!}, \quad 2P = \prod_{i=1}^{n}, \quad \mathrm{CL}_i, \qquad (2)$$

where n refers to the number of planes having a hit and CL_i is each confidence level for a hit on the ith plane, which is defined by a cumulative function of dE/dx distribution for each detector.

The MUCL distributions are shown in Fig. 7. When the MUCL exceeded 0.2 (0.7) for a PM (WAGASCI) event the track was identified as a muonlike particle, and when it was under 0.2 (0.7) it was identified as a protonlike track. The PM has more light yield inside the scintillator than the

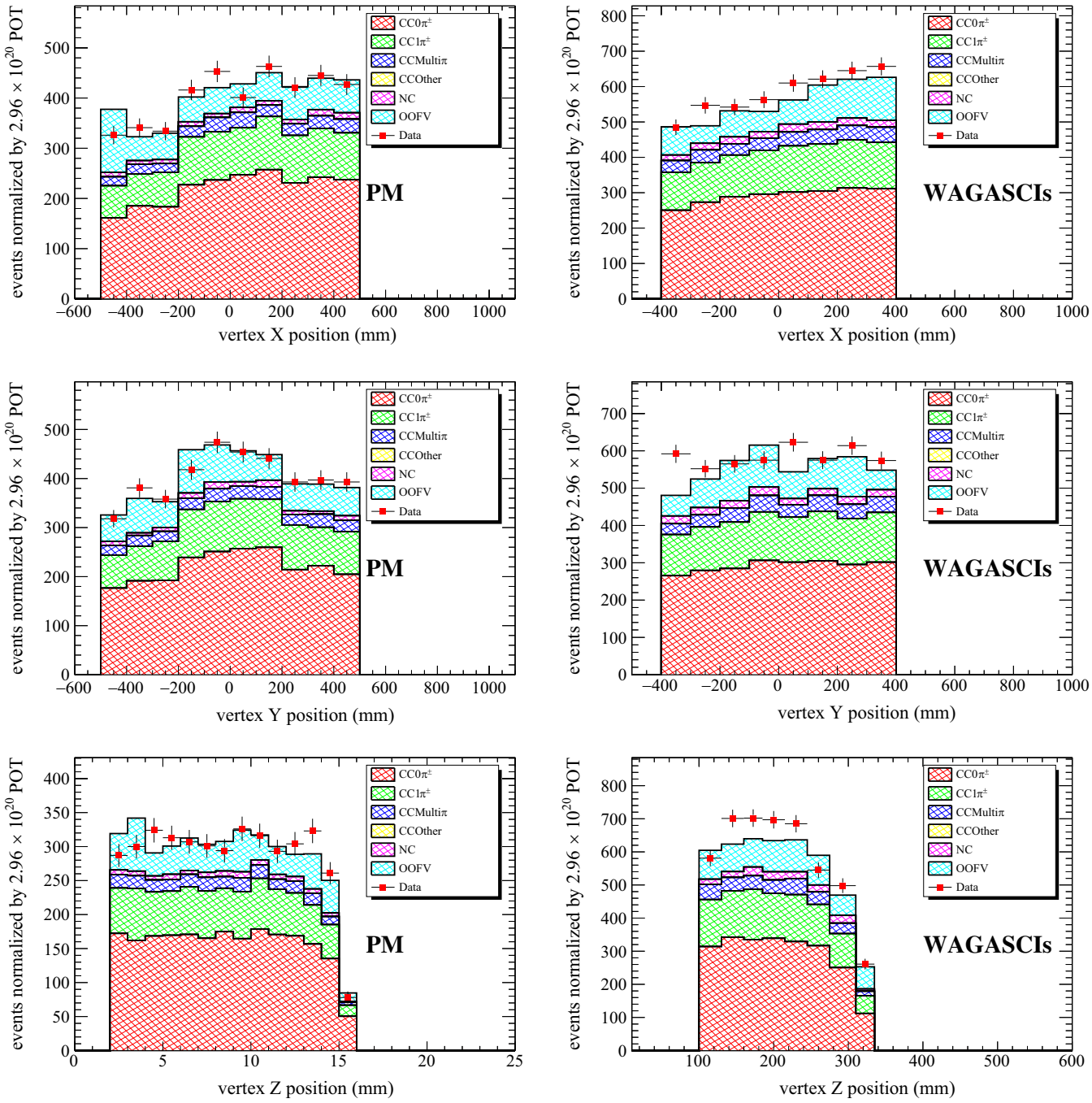

FIG. 6. Data-MC comparison of the vertex distributions in the X (top), Y (middle), and Z (bottom) directions for the control samples for the PM (left) and the WAGASCI (right). The MC predictions are normalized by accumulated POT.

WAGASCI and tended to have higher MUCL values for muonlike tracks. The different values come from the figure of merit optimization. When there were two or three tracks from a reconstructed vertex, it was required that the second and third tracks were protonlike tracks. This selection step increases the sample purity by 10%.

4. Charge of muon

As we measured the cross section of the muon neutrino, the muon candidate should be negatively charged. The charge identification was applied if the muon candidate was contained within BabyMIND. This detector has an iron-core magnet in each steel plane, producing a magnetic field where charged particles are bent upwards if positively charged, or downwards if negatively charged. The discriminator for the charge identification was defined by a log-likelihood ratio, which is a ratio of the likelihood of μ^- or μ^+ calculated using the track curvature. The distribution of the log-likelihood ratio is shown in Fig. 8. When the log-likelihood ratio was less than 4, the track was selected as a

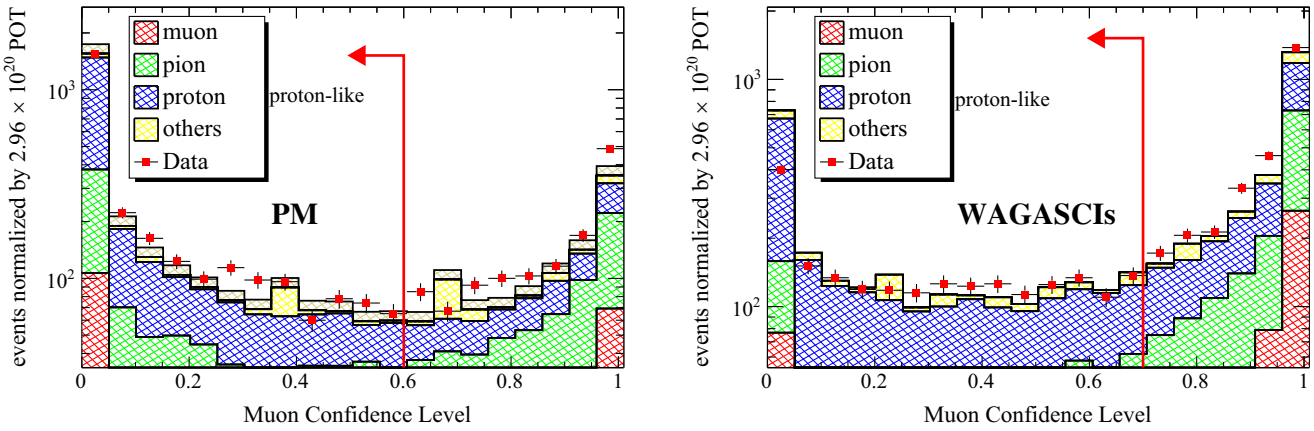

FIG. 7. Data-MC comparison of the muon confidence level for the PM (left) and the WAGASCI (right) for the CC-inclusive samples.

negatively charged particle. This selection helps to reduce backgrounds from opposite-sign neutrino interactions. This background was due to a contamination of muon antineutrinos in the predominantly muon neutrino flux.

5. Track-associated hit ratio

The track-associated hit ratio is defined as

$$R_{\text{track-associated hit}} = \frac{N_{\text{rechits}}}{N_{\text{allhits}}}, \tag{3}$$

where N_{rechits} was the number of hits in the vertex detector from all reconstructed tracks associated with the same vertex. N_{allhits} was the number of hits in all tracks obtained in the vertex detector, including tracks not associated with the vertex. The hit ratio represented the fraction of hits in an event associated with a given track. This was applied only to the WAGASCI events because the wall background constituted around 20% of the total number of WAGASCI events without this cut. This selection reduced the background from OOFV events, in particular from interactions in the wall. Particles produced within the wall sometimes produced tracks in the vertex detectors within the neutrino bunch timing, and such an event has a lower track-associated hit ratio. When all hits in a vertex detector ended up in the reconstructed tracks for the event, the ratio was 1.0. When the track-associated hit ratio of an event was larger than 0.6, it was selected as a signal event. After this selection was applied, the contamination of OOFV background was reduced to around 10%, a similar level as in the PM sample.

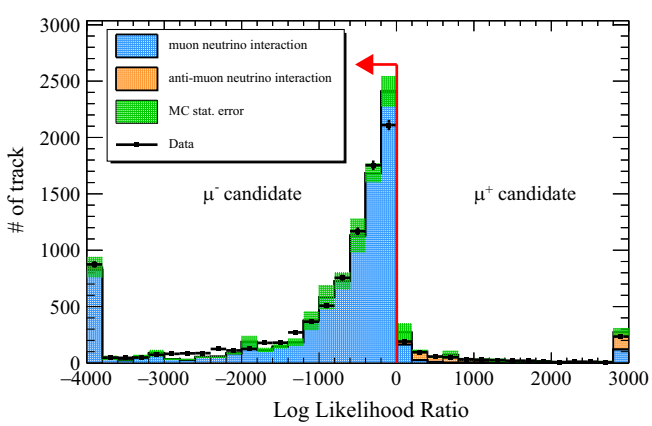

FIG. 8. Data-MC comparison of the log-likelihood ratio of track charge for the stopping muon sample.

6. Michel electron tagging

A Michel electron is the electron from the decay of a muon. Particles are produced by the J-PARC accelerator in bunches, with each bunch around 500 ns in length, whereas the typical lifetime of a muon is 2.2 μs. We searched for Michel electron hits originating from a pion track in each event in order to identify nonreconstructed pions. The presence of a Michel electron was a sign that a pion was produced in the neutrino interaction. The tagging proceeded in the following way:

(i) Identify hit clusters outside the beam bunch timing. Here, a hit cluster was a group of hits within a 100 ns time window.
(ii) If the distance between the earliest hit in the cluster and the vertex of the neutrino event was less than 150 mm in the X, Y, and Z directions, select it for the next step.
(iii) Count the number of hits in the cluster that satisfy the above criteria. When the number of hits exceeds two, the event was tagged as having a Michel electron.

As our signal did not contain any charged pion in the final state, events with a Michel electron must be rejected. The Michel electron tagging increases the signal purity by about 5%.

7. Stop inside the MRD detectors

When measuring the differential cross section against momentum, an additional requirement was added that the

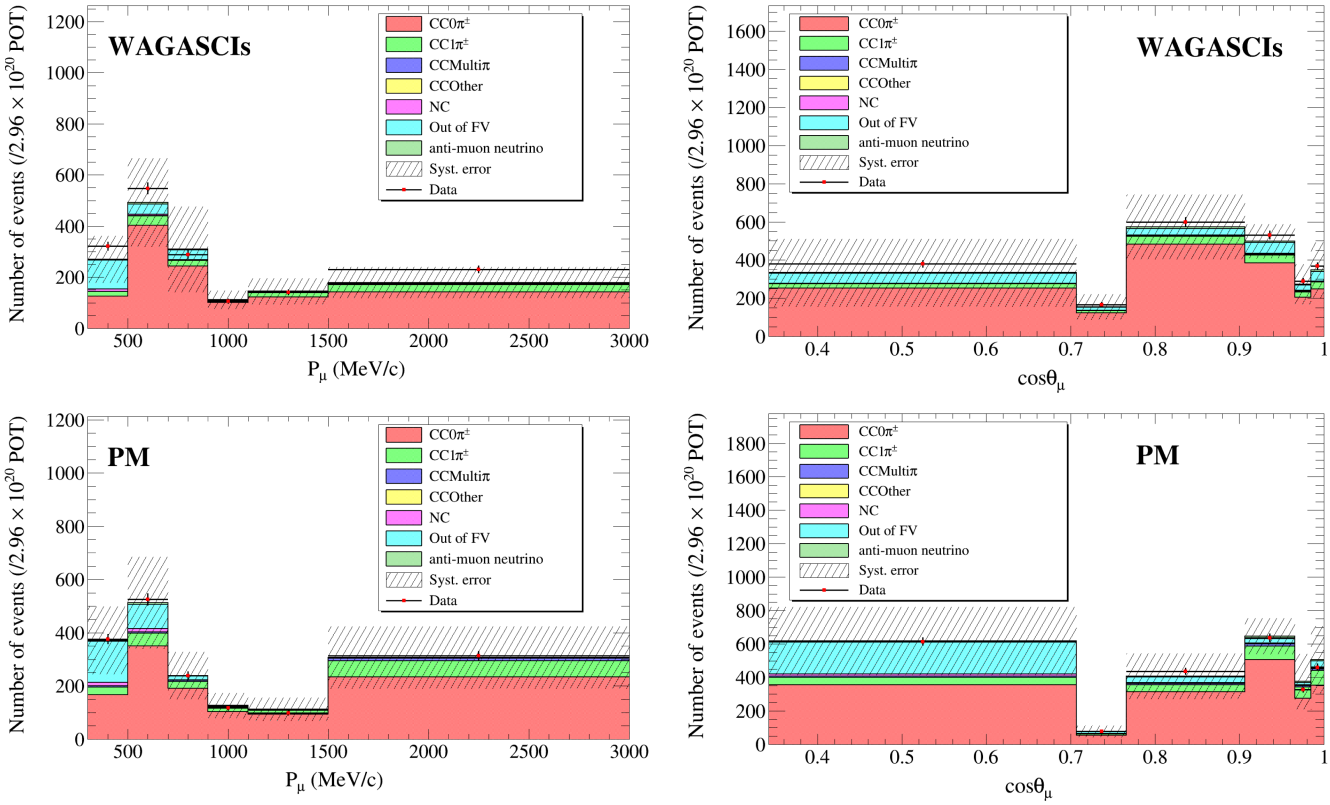

FIG. 9. Kinematic variables (momentum and angle) of the outgoing lepton for the selected events in the WAGASCI (top) and PM (bottom) samples.

track stops inside the muon range detectors so that the track momentum by range could be evaluated.

The uncertainties on the selection cut parameters were considered by alternating the cut values, which is described in Sec. V.

G. Kinematic distributions

Figure 9 shows the kinematic distributions of the outgoing leptons for selected events in the WAGASCI and the PM. The purity of the CCQE sample on the CH and H_2O target is 49.7% and 53.0%, respectively. Focusing on the data-MC comparison, the PM sample shows good consistency between data and MC, however, the number of events in the data was about 10% larger than in the MC for the WAGASCI sample.

H. Sideband selection

Figure 5 also shows the selection scheme for the muon neutrino CC1$\pi^{\pm}$, which was the sideband sample of this measurement. Each cut has already been described in the CC0$\pi^{\pm}$ selection (Sec. III F), and to select the sideband only the Michel electron cut was reversed.

The selection was divided into two branches depending on whether a pion was reconstructed as a track or not. The first branch of CC1$\pi^{\pm}$ selection includes pion tracks below the tracking threshold. The whole selection criteria in this path had the same scheme as in the selection of the CC0$\pi^{\pm}$ sample, except for reversing the final cut for Michel electron tagging. For this CC1$\pi^{\pm}$ selection, the Michel electron must be detected. The second branch includes pion tracks that were above the tracking threshold. A pion track is considered to be more like a muonlike track than a protonlike track in terms of its MUCL value, hence in this scenario the MUCL cut was reversed. The charge cut was applied in order to reduce the opposite-sign background and select muon neutrino CC1$\pi^{\pm}$ interactions with the appropriate sign.

I. Number of target nucleons

The cross sections were normalized per nucleon (either proton or neutron) in the target material. Table I

TABLE I. The number of target nucleons inside the fiducial volume for each vertex detector. Each number refers to the number of nucleons (both protons and neutrons) in the CH or H_2O.

Target material		Number of target nucleons	
		Measured (10^{28})	Uncertainty (10^{28})
PM	CH	18.66	0.045 (0.24%)
WAGASCI	CH	3.64	0.011 (0.30%)
	H_2O	13.77	0.048 (0.35%)

summarizes the number of target nucleons in the CH and H_2O targets.

IV. CROSS SECTION EXTRACTION

The selected samples of data contain CC0$\pi^{\pm}$ events as a signal and backgrounds such as events with pions produced in neutrino interactions, neutral current interactions, etc. In order to extract the signal components in the selected samples, we applied a binned likelihood approach performed with the MINUIT2 [27] algorithm. The fitting method was similar to that previously used in T2K cross section analyses [28]. Here, a brief summary of the method is provided.

The binned likelihood function is schematically defined as

$$-2\ln\mathcal{L}(\vec{y};\vec{\theta}) = -2\ln\mathcal{L}_{\rm stat}(\vec{y};\vec{\theta}) - 2\ln\mathcal{L}_{\rm syst}(\vec{y};\vec{\theta}), \quad (4)$$

where $\mathcal{L}$ is the likelihood function, $\vec{y}$ is a vector of data, and $\vec{\theta}$ is a set of parameter values.

The statistical part of the likelihood function is given by

$$-2\ln\mathcal{L}_{\rm stat}(\vec{y};\vec{\theta}) = \sum_{j}^{\rm reco\ bins} 2\left(\beta_j N_j^{\rm exp} - N_j^{\rm obs} + N_j^{\rm obs}\ln\frac{N_j^{\rm obs}}{\beta_j N_j^{\rm exp}} + \frac{(\beta_j-1)^2}{2\sigma_j^2}\right), \quad (5)$$

where j runs over each reconstructed bin for all samples and $N^{\rm exp}(N^{\rm obs})$ is the number of selected events predicted by MC (obtained in the data), β_j are the Barlow-Beeston scaling parameters which account for the uncertainty of finite MC simulation (for the definition see [28]), and σ is the MC statistical uncertainty.

The binned expected number of selected events, $N_j^{\rm exp}$, is given for each value of $\vec{\theta}$ as a sum of two contributions, one from the signal, $N_j^{\rm exp,sig}$, and another from the background, $N_j^{\rm exp,bg}$. The signal contribution was calculated with the true signal events multiplied with a detector smearing matrix to provide the number of true signal events in the reconstructed bin.

We then introduce multiplicative parameters to weight events. Template parameters denoted by c_i are given for each true bin i, to weight the number of selected events in MC, $N_i^{\rm MC,sig}$. The template parameters scale the number of signal events of MC in each true bin to reproduce the data and are free parameters with no prior uncertainty (or penalty term). Besides the template parameters, there were three types of systematic parameters from neutrino flux, neutrino interaction, and detector systematics. The expected number of events was weighted by these parameters too. They were mainly sensitive to the shape of the input distributions.

The complete expression for the expected number of events is

$$N_j^{\rm exp} = \sum_{i}^{\rm true}\left[c_i\left(N_i^{\rm MC,sig}\prod_{a}^{\rm int} w(a)_i^{\rm sig}\right) + \sum_{k}^{\rm bg} N_{ik}^{\rm MC,bg}\prod_{a}^{\rm int} w(a)_i^{\rm k}\right] t_{ij} r_j \sum_{n}^{E_\nu} v_{\rm in} f_n, \quad (6)$$

where a runs over the interaction parameters, $w(a)$ refers to each weight, and k is an index running over interaction modes. They affect the number of selected events in the MC, changing its shape or normalization. t_{ij} is the transfer matrix. n runs over the neutrino energy corresponding to the true bin i. The $v_{\rm in}$ is the fractional contribution in the ith bin by neutrinos having energy n. f_n terms are the weights from flux systematics. The reconstructed signal events were multiplied by the smearing matrix to calculate the true number of signal events.

With the assumption that the systematics uncertainties follow a Gaussian probability distribution, the systematic part of the likelihood function is given in

$$-2\ln\mathcal{L}_{\rm syst} = \sum_{\rm syst}((\vec{p}-\vec{p}_{\rm prior})(V_{\rm cov}^{\rm syst})^{-1}(\vec{p}-\vec{p}_{\rm prior})^T), \quad (7)$$

where p runs over all systematic parameters and $V_{\rm cov}^{\rm syst}$ are covariance matrices for each prior parameter. This acts as a penalty term for moving the systematic parameters away from their prior values. We have a sufficient number of events in each bin for this assumption.

The cross section fitter provides the best-fit values for template parameters and systematic parameters. The expected signal events were then calculated by

$$\hat{N}_i^{\rm exp,sig} = \sum_{j}^{\rm recon}\left(\hat{c}_i N_i^{\rm MC,sig}\prod_{a}^{\rm int}\hat{w}(a)_i^{\rm sig}\right)(t_{ij})^{-1}\hat{r}_j\sum_{n}^{E_\nu} v_{\rm in}\hat{f}_n, \quad (8)$$

where the "hat" means the best-fit value. Then, the differential cross section is calculated by

$$\frac{d\sigma}{dx_i} = \frac{\hat{N}_i^{\rm exp,sig}}{\epsilon_i\Phi N_{\rm nucleons}^{\rm FV}}\times\frac{1}{\Delta x_i}, \quad (9)$$

where σ is the flux-integrated cross section and x is a muon kinematic variable, while $\epsilon, \Phi, N_{\rm nucleons}^{\rm FV}$, and Δx_i are the detection efficiency, integrated flux, number of target nucleons in the fiducial volume, and the bin width of the true bin i, respectively. Since we report a single differential cross section as a function of muon kinematics, x refers to either p_μ or $\cos\theta_\mu$.

When we calculate a cross section there are multiple ways of treating the neutrino flux. In this approach a flux-integrated cross section rather than a flux-unfolded one, was calculated to avoid model dependence (or at least to reduce it) in terms of the shape of the neutrino energy spectrum.

V. SYSTEMATICS UNCERTAINTIES

This section is organized into three subsections: neutrino flux, neutrino interaction, and detector systematics. For neutrino flux and detector systematics, systematic parameters were summarized in covariance matrices, which were used when fitting the data. For neutrino interactions, a different approach based on MC event reweighting was used.

A. Neutrino flux systematics

Neutrino flux uncertainties were evaluated using a method employed previously in other T2K studies [23]. The covariance matrix binning has been chosen to ensure approximately equal statistics in each bin, as can be seen in Table II, and the resultant matrix is shown in Fig. 10.

In Fig. 11 the fractional error on the muon neutrino flux is shown by the colored spectrum. In the background, the curve filled with gray shows the neutrino flux as a function of neutrino energy at the 1.5° off-axis angle. The uncertainties stem from several factors, including the hadron production model, the profile of the proton beam, the off-axis angle, the horn current, horn alignment, wrong-sign ($\nu/\bar{\nu}$) neutrino contamination, and others. The T2K replica target hadron production measurements in NA61/SHINE [29–31] were used to define the hadron uncertainties reported here. How each source of error impacts the flux prediction is detailed in [23].

B. Neutrino interaction systematics

Our MC simulation generated particles from interaction vertices based on theoretical models that incorporate our current understanding of neutrino interactions. However, these models rely on approximations due to limited experimental data and/or the complexity of underlying theoretical models. We used the NEUT software [24] to simulate neutrino interactions.

TABLE II. Energy binning for flux uncertainty distribution. Bins in a given energy range have the same width.

Energy range (GeV)	Number of bins	Width in energy per bin (GeV)
0.0–3.0	15	0.2
3.0–4.0	1	1.0
4.0–10.0	3	2.0
10.0–30.0	1	20.0

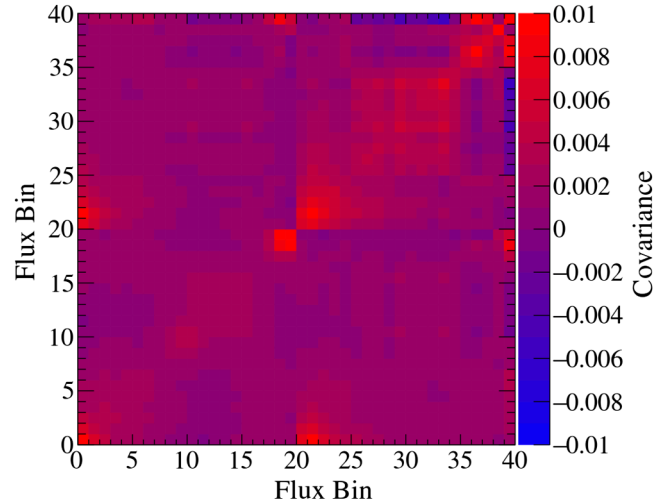

FIG. 10. Covariance matrix for the neutrino flux uncertainty at the 1.5° off-axis angle where the WAGASCI-BabyMIND is located. The bins 0–19 correspond to the ν_μ component and bins 20–39 correspond to the $\bar{\nu}_\mu$ component of the beam.

Neutrino interaction models include a set of parameters called dials. Dials can be scalar quantities, such as a dimensional parameter affecting a physical process, a nondimensional quantity tuning interaction strength, or a boolean variable controlling a model feature.

Our method for estimating uncertainties due to neutrino interaction models assumed that varying all dials within their stated uncertainty fully accounts for the overall uncertainty of the cross section measurement. A limitation of this method was that the models themselves might be incomplete and some sources of uncertainty might not be accounted for. To cover such cases, we performed the validations described in Sec. VI.

Prior knowledge about each dial comes from theoretical calculations and previous measurements. While a complete account of each and every dial is out of the scope of this paper, in Table III we list all the dials used in our cross

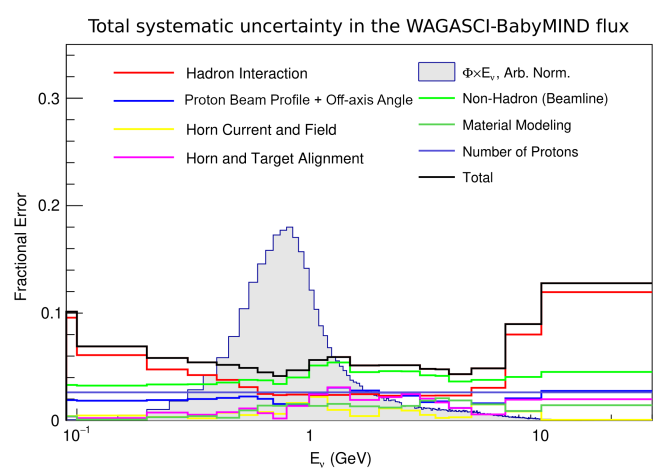

FIG. 11. Flux uncertainties for ν_μ in forward Hall current mode at the WAGASCI-BabyMIND position.

TABLE III. List of all systematic parameters from neutrino interaction models that were included in the analysis. The column "Dial name" is the name of the parameter as it appears in the source code. The column "Prior" is the parameter's prior value before variation. The column "Uncertainty" represents the $\pm 1\sigma$ prior uncertainty. The column "Target" indicates which type of target material is affected, "CH" is a shorthand for hydrocarbon, while "Both" refers to both water and hydrocarbon. The column "Description" contains a short description of the meaning of the parameter. No single parameter dominates the systematic uncertainty from the neutrino interaction models, in the sense that no parameter contributes more than 50% to the total systematic error.

Dial name	Prior	Uncertainty	Target	Description
			CCQE	
MaCCQE	1.21 GeV	−0.3, +0.3	Both	CCQE axial mass
QETwk_High_Q2_Weight_1	1	−0.11, +0.11	Both	Reweight CCQE events with $0.25 < Q^2 < 0.5$
QETwk_High_Q2_Weight_2	1	−0.18, +0.18	Both	Reweight CCQE events with $0.5 < Q^2 < 1$
QETwk_High_Q2_Weight_3	1	−0.4, +0.4	Both	Reweight CCQE events with $Q^2 > 1$
SF_OptPotTwkDial_O16	0	−0, +0.49	Water	SF optical potential correction, O
SF_OptPotTwkDial_C12	0	−0, +0.49	CH	SF optical potential correction, C
SF_P1_2Shell_MeanF_Norm_O	0	−0.2, +0.2	Water	Norm of Gaussian positioned at some E_m for restricted p_m
SF_P1_2Shell_MeanF_PMissShape_O	0	−1, +1	Water	Template normalization in p_m in some range of p_m, E_m
SF_P3_2Shell_MeanF_Norm_O	0	−0.4, +0.4	Water	Norm of Gaussian positioned at some E_m for restricted p_m
SF_P3_2Shell_MeanF_PMissShape_O	0	−1, +1	Water	Template normalization in p_m in some range of p_m, E_m
SF_PBTwkDial_Hybrid_C12_nu	0	−2, +0.6	CH	Hybrid nuclear mom cutoff and template normalization in q_3, q_0
SF_PBTwkDial_Hybrid_C12_nubar	0	−2, +0.6	CH	Hybrid nuclear mom cutoff and template normalization in q_3, q_0
SF_PBTwkDial_Hybrid_O16_nu	0	−2, +0.6	Water	Hybrid nuclear mom cutoff and template normalization in q_3, q_0
SF_PBTwkDial_Hybrid_O16_nubar	0	−2, +0.6	Water	Hybrid nuclear mom cutoff and template normalization in q_3, q_0
SF_PShell_MeanF_Norm_C	0	−0.2, +0.2	CH	Norm of Gaussian positioned at some E_m for restricted p_m
SF_PShell_MeanF_PMissShape_C	0	−1, +1	CH	Template normalization in p_m in some range of p_m, E_m
SF_SRC_Norm_C	1	−1, +1	CH	Overall normalization in some range of p_m, E_m
SF_SRC_Norm_O	1	−1, +1	Water	Overall normalization in some range of p_m, E_m
SF_SShell_MeanF_Norm_C	0	−0.4, +0.4	CH	Norm of Gaussian positioned at some E_m for restricted p_m
SF_SShell_MeanF_Norm_O	0	−0.2, +0.2	Water	Norm of Gaussian positioned at some E_m for restricted p_m
SF_SShell_MeanF_PMissShape_C	0	−1, +1	CH	Template normalization in p_m in some range of p_m, E_m
SF_SShell_MeanF_PMissShape_O	0	−1, +1	Water	Template normalization in p_m in some range of p_m, E_m
			2p2h	
MECTwkDial_Norm_C12	1	−0.99, +0.99	CH	2p2h Normalization carbon
MECTwkDial_Norm_O16	1	−0.99, +0.99	Water	2p2h Normalization oxygen
MECTwkDial_Norm_Other	1	−0.49, +0.49	Both	2p2h Normalization others
MECTwkDial_PDDWeight_C12_NN	0	+0.49, −0.49	CH	2p2h shape on carbon: contributions change for NN pairs
MECTwkDial_PDDWeight_C12_np	0	−0.49, +0.49	CH	2p2h shape on carbon: contributions change for NP pairs
MECTwkDial_PDDWeight_O16_NN	0	−0.49, +0.49	Water	2p2h shape on oxygen: contributions change for NN pairs
MECTwkDial_PDDWeight_O16_np	0	−0.49, +0.49	Water	2p2h shape on oxygen: contributions change for NP pairs
MECTwkDial_PNNN_Shape	0	−0.33, +0.33	Both	2p2h shape: NN or NP nucleon pair
			SPP	
RES_E_b_C_numu	25 MeV	−24.9, +24.9	CH	Resonant SPP E_b value (MeV) for muon neutrinos on carbon
RES_E_b_O_numu	25 MeV	−24.9, +24.9	Water	Resonant SPP E_b value (MeV) for muon neutrinos on oxygen
RES_E_b_C_numubar	25 MeV	−24.9, +24.9	CH	Resonant SPP E_b value (MeV) for $\bar{\nu}_\mu$ on carbon
RES_E_b_O_numubar	25 MeV	−24.9, +24.9	Water	Resonant SPP E_b value (MeV) for $\bar{\nu}_\mu$ on oxygen
BgSclRES	1.3	−0.15, +0.15	Both	$I_{\frac{1}{2}}$ nonresonant background
CA5RES	1.01	−0.15, +0.15	Both	CA5(0): value at $Q^2 = 0$ of the axial form factor
MaRES	0.95 GeV	−0.15, +0.15	Both	RES axial mass
			FSI	
PionFSI_AbsProb	1.404	−0.432, +0.432	Both	Pion FSI absorption (FEFABS)
PionFSI_CExHighMomProb	1.8	−0.288, +0.288	Both	Pion FSI single charge exchange (high energy) (FEFCXH)
PionFSI_CExLowMomProb	0.697	−0.305, +0.305	Both	Pion FSI single charge exchange (low energy) (FEFCX)
PionFSI_InelProb	1.002	−1.101, +1.101	Both	Pion FSI hadron (N + n pi) production (FEFINEL)
PionFSI_QEHighMomProb	1.824	−0.859, +0.859	Both	Pion FSI QE scattering (high energy) (FEFQEH)
PionFSI_QELowMomProb	1.069	−0.313, +0.313	Both	Pion FSI QE scattering (low energy) (FEFQE)
TwkDial_FateNucleonFSI	0	−0.3, +0.3	Both	Fate of final-state nucleons after the FSI interactions

(Table continued)

TABLE III. *(Continued)*

Dial name	Prior	Uncertainty	Target	Description
			Other	
CC_DIS_norm_nu	1	−0.15, +0.15	Both	Normalization of CC DIS for neutrinos
CC_DIS_norm_nubar	1	−0.15, +0.15	Both	Normalization of CC DIS for antineutrinos
CC_MultiPi_norm_nu	1	−0.2, +0.2	Both	Multipion production normalization (nu)
CC_MultiPi_norm_nubar	1	−0.2, +0.2	Both	Multipion production normalization (nubar)

section measurement. How the variation of each dial was reflected into the cross section measurement is summarized in Sec. V B 1. In Secs. V B 2–V B 4, we discuss the dials expected to have the greatest impact.

It is important to stress that the systematic uncertainties listed below do not directly impact the fitting results, but affect them through changes in detection efficiencies, as each bin's signal count was fitted with the corresponding template parameter to reproduce the data.

1. Reweighting of MC events

In the course of a cross section analysis, it is customary to use MC simulations to model changes to the event selection under changes of a generic cross section dial ($\vec{x}$). We calculated a series of correction factors to the MC, i.e., for a change to dial $\vec{x} \to \overrightarrow{x'}$ for each event i, then we calculated a weight

$$w_i = \frac{\sigma(\overrightarrow{x'})}{\sigma(\vec{x})}, \tag{10}$$

which is the ratio of the nominal cross section $\sigma(\vec{x})$ to an updated cross section $\sigma(\overrightarrow{x'})$. Applying the individual weights to the MC sample will function in much the same way as a regenerated MC sample with the modified dial, and this procedure is called "reweighting."

The weights were then organized into a set of splines, allowing for smooth interpolation between the node in a certain analysis bin, when the value of the dial was varied with respect to the nominal value. These splines allow for smooth interpolation between dial values, enabling continuous variation of model parameters. They constitute one of the inputs passed to the cross section fitter. This approach is the same as the one adopted in many other T2K cross section analyses [11].

2. CCQE and the axial mass

CCQE interactions are dominant at T2K energies. The CCQE cross section on a single nucleon depends on vector and axial form factors [7]. Vector form factors are known precisely from electron scattering data [32], due to the conserved vector current hypothesis. However, for the axial form factor the situation is different, and it was a dominant source of uncertainty. A dipole expression is assumed with an axial mass parameter $M_A^{\mathrm{QE}} = 1.21$ GeV, which is constrained by past neutrino-deuterium scattering measurements [33].

In CCQE interactions on a nucleon, within a nucleus such as oxygen or carbon, the effects of nuclear binding were modeled using the Benhar spectral function (SF) model [34], which provides a realistic shell model–based description of the nuclear ground state and is strongly favored over relativistic Fermi gas models [35] by electron scattering data [36].

In our study, we treated M_A^{QE} like an effective parameter to account for uncovered effects, such as a nondipole expression for the axial form factor. Hence, a large uncertainty was assumed to let the data determine its best value.

3. Multinucleon interactions (2p2h)

The term "2p2h process" refers to neutrino interactions on pairs of correlated nucleons. They give rise to an important fraction of the events observed in T2K's energy range. In NEUT simulations 2p2h includes contributions from meson exchange currents, nucleon-nucleon correlations (NN), and their interference [37,38], as described by the Valencia model [39]. It was assumed that the 2p2h contribution populates a kinematic region of momentum transfer $|\vec{q}| \leq 1.2$ GeV/c. Since precise 2p2h cross section measurements are unavailable, a conservative approach was taken in setting priors for its dials. A set of normalization dials scaling the whole 2p2h contribution (depending on the neutrino flavor and target nucleus) was considered in this analysis.

4. Single-pion production

Single-pion final states arise from resonance excitation, coherent pion production, and multipion processes. As already mentioned in Sec. I, the neutrino flux observed at the off-axis angle of the WAGASCI-BabyMIND is shifted toward higher energies with respect to ND280, resulting in an increased probability of pion production from the neutrino interactions, thus making their correct characterization important for our analysis. The resonance excitation mechanism is modeled by NEUT with the Rein-Sehgal model [40,41].

The most important dials were M_A^{RES} (RESonance axial-vector mass), $C_5^A(0)$ (normalization of the leading axial

form factor), and $I_{1/2}$, (the amount of nonresonance contribution with isospin 1/2 in the Rein-Sehgal model). The nominal values were taken from theoretical models tuned to external data [42,43].

C. Detector systematics

In this analysis, detector systematic uncertainties were separated into three categories: detector-related parameters (Sec. V C 1), track reconstruction–related parameters (Sec. V C 2), and sample selection–related parameters (Sec. V C 3). The covariance matrix, V_{ij}, for each systematic uncertainty was calculated from the change in the predicted number of events by

$$V_{ij} = \frac{1}{2}\frac{(\phi^i_{\rm nom} - \phi^i_+)(\phi^j_{\rm nom} - \phi^j_+)}{\phi^i_{\rm nom}\phi^j_{\rm nom}} + \frac{1}{2}\frac{(\phi^i_{\rm nom} - \phi^i_-)(\phi^j_{\rm nom} - \phi^j_-)}{\phi^i_{\rm nom}\phi^j_{\rm nom}}, \tag{11}$$

where i and j cover the binning of Tables VI and VII. $\phi^i_{\rm nom}$ is the number of selected events in the nominal setting in the ith

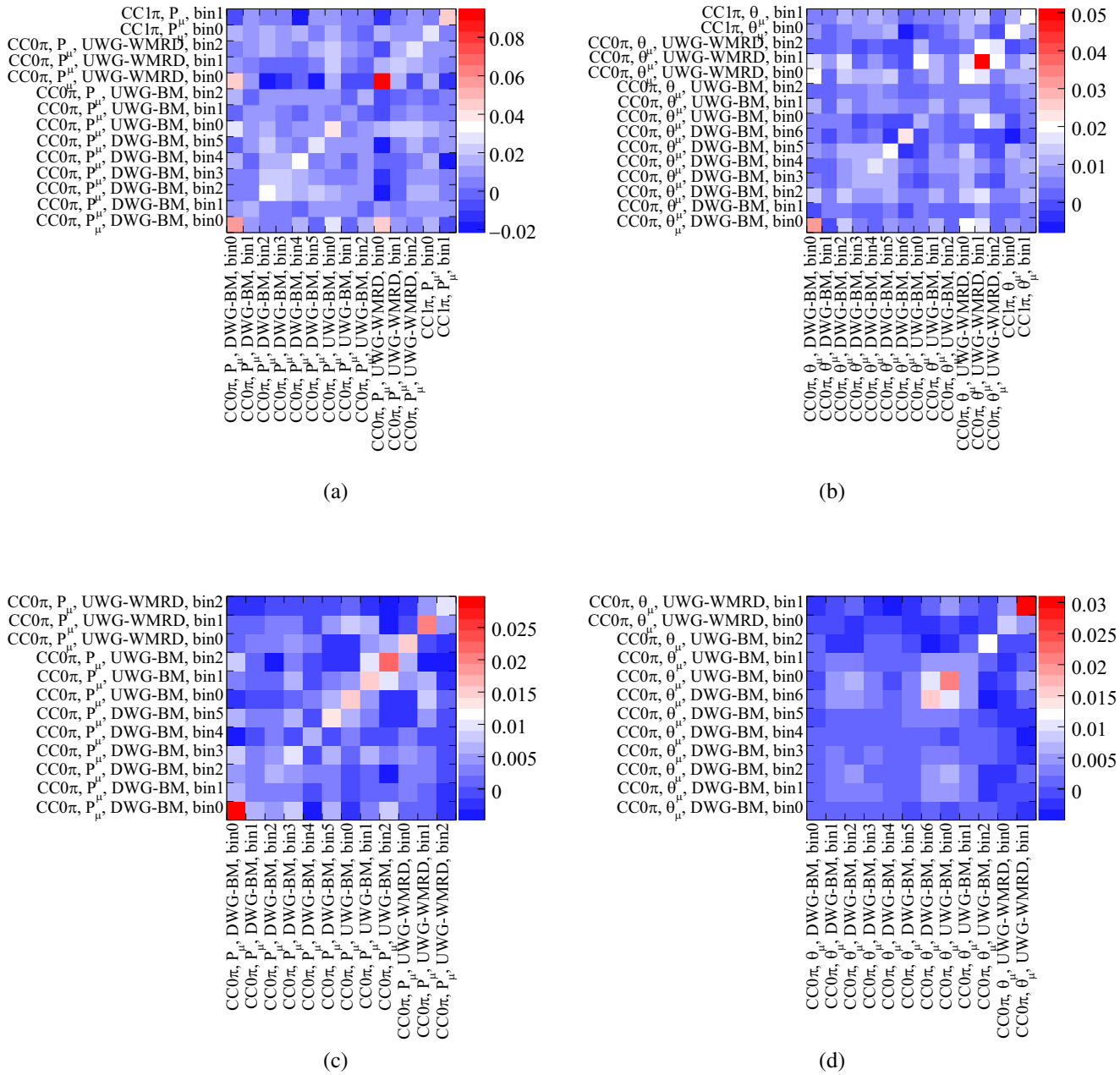

FIG. 12. Covariance matrix for the detector systematic uncertainties on the number of selected events given as a fractional change for the WAGASCI and PM. (a) WAGASCIs: muon momentum. (b) WAGASCIs: muon angle. (c) PM: muon momentum. (d) PM: muon angle.

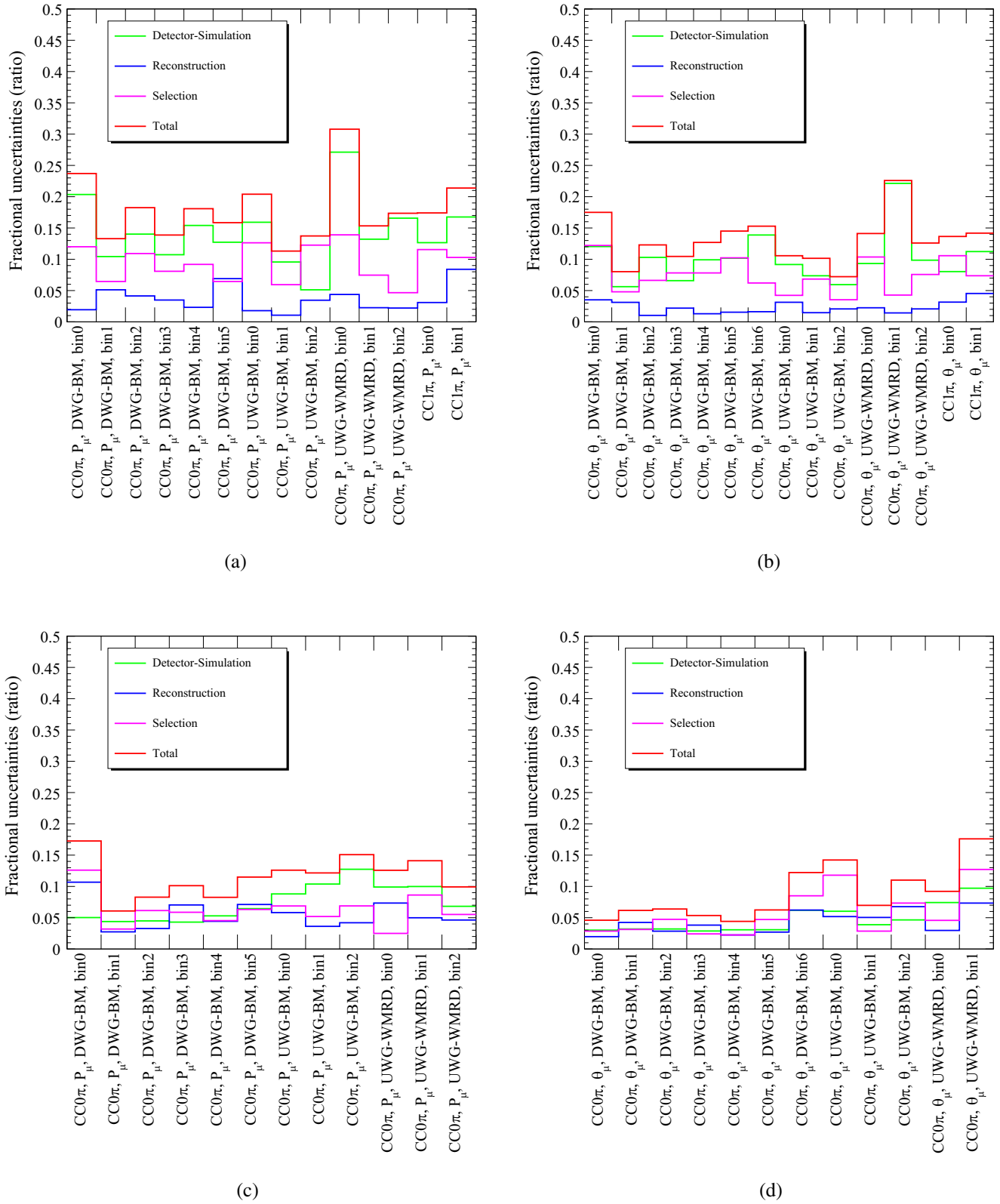

FIG. 13. Fractional errors due to the detector systematic uncertainties on the number of selected events. (a) and (b) correspond to the WAGASCI sample, while (c) and (d) correspond to the PM sample. The muon momentum binning is the same as in Table VI and the muon angle binning is the same as in Table VII. Systematic uncertainties arising from the neutrino interaction model are not included in this plot, only detector and reconstruction-related systematic uncertainties are included. (a) WAGASCIs: muon momentum. (b) WAGASCIs: muon angle. (c) PM: muon momentum. (d) PM: muon angle.

TABLE IV. List of the detector systematic parameters.

Parameter	Category
Target mass	Detector performance
Magnetic field	Detector performance
Detector alignment	Detector performance
MPPC noise	Detector performance
Light yield	Detector performance
Hit threshold	Detector performance
Crosstalk	Detector performance
Scintillator inefficiency	Detector performance
Pion secondary interaction	Detector performance
Two-dimensional tracking efficiency	Track reconstruction
Threshold for track connection between detectors	Track reconstruction
Threshold for determination of vertex	Track reconstruction
Bunch timing selection	Event selection
Fiducial volume	Event selection
Contained volume	Event selection
Particle identification	Event selection
Charge identification	Event selection
Track-associated hit ratio	Event selection
Michel electron tagging	Event selection
Event pileup	Event selection

bin, while ϕ^i_+ and ϕ^i_- refer to the number of selected events in the ith bin when the parameter was varied from the right boundary (+) to the left boundary (−) of its range. Equation (11) is applicable when the parameter in question affects the event rate in a monotonic manner, which holds true for all parameters considered in this analysis.

The sums of the covariance matrices of all of the parameters are shown in Fig. 12. The fractional uncertainty on the number of selected events for each category of detector systematic uncertainties is shown in Fig. 13. The obtained covariance matrix was used to extract the cross section as described in Eq. (7) of Sec. IV. Table IV shows the detector parameters considered in this analysis. We discuss these parameters in Sec. V C 1.

1. Detector-related parameters

Detector-related parameters encompass various factors intrinsic to the detector's physical properties and operational conditions. They were tuned with actual measurements of the detector performance. The variations around the nominal value were chosen so that they cover the discrepancy between MC and the measurements.

2. Track reconstruction–related parameters

The change of the detection efficiency was evaluated by varying the tolerances of each of the track reconstruction steps and calculating a covariance matrix in a similar way as described in Sec. V C 1.

3. Sample selection–related parameters

These parameters refer to criteria and thresholds used to select specific events of interest from the overall data collected by the detector. Below, we highlight those that contribute most significantly to the overall uncertainty:

(1) *Contained volume cut*: To ensure accurate momentum measurements, we analyzed only muons which stopped inside a defined volume of the muon range detectors. We defined variations in the contained volume for different detector modules to estimate the impact on event selection.

(2) *Fiducial volume cut*: We adjusted the boundaries of the fiducial volume, which was defined within the target detector mass, to account for uncertainties in selecting events which happen near the edge of the fiducial volume.

4. Out-of-fiducial-volume background

We used a sand muon sample to estimate the normalization of wall-generated background events. A 13% difference (data exceeding MC) was observed in the number of sand muon events estimated by the MC and data with a partial dataset of 1.5×10^{20} POT. This difference might arise from disparities in the density and composition of the pit wall materials *in situ* and as modeled in the MC simulation. A 13% normalization error was assigned to cover the difference between MC and data in this sample.

VI. SIMULATED DATA STUDIES

We performed simulated data studies using the selected samples and the evaluated systematic uncertainties. These studies aimed to confirm that no significant bias was introduced into the analysis and validate the fitting method and prepared inputs. Several kinds of alternative datasets

were prepared and used in turn as input to the fitter. The pseudodatasets were made using the alternative interaction models or using the nominal interaction model where some parameters were tweaked from their nominal value. The psuedodatasets used are listed below.

Tweaked M_A^{RES}: The parameter value of M_A^{RES} was changed by 20%, leaving all other parameters unchanged.

Alternative RPA model (BeRPA): The pseudodata were made with an alternate random phase approximation model (BeRPA) for CCQE interactions instead of the default RPA Nieves model [39,44].

*Alternative CCRES model (*low-Q^2 *suppression)*: This alternative model accounts for the difference between data and MC reported by the MINERvA experiment [45] and the MINOS experiment [46]. The difference emerges in the low-energy transfer region (sub-GeV), where the data were smaller than the MC prediction.

Alternative NEUT *model*: One of the significant changes in the alternative NEUT model is that the M_A^{QE} value was set to 1.05 $\mathrm{GeV/c^2}$ while the nominal value was 1.21 $\mathrm{GeV/c^2}$. Another change was the use of the Nieves 1p1h model without spectral function as a CCQE model.

Signal from GENIE: The pseudodata were produced by the GENIE neutrino interaction generator (version: v3, tune: G18_02b [47]). Only the signal events were replaced by the GENIE prediction (CC0$\pi^{\pm}$ events), while the background events remained the same as in the nominal NEUT prediction.

We validated both inputs and fitter by confirming that the calculated differential cross sections using each psuedodataset were consistent with the nominal simulation within the systematics uncertainty.

VII. RESULTS

A. Integrated cross section result

We report as our main result the flux-integrated total cross section within the phase space, $\cos\theta_\mu > 0.34$ and $p_\mu > 300$ MeV/c, on both targets using the angular binning samples (without the contained cut in the MRDs). The integrated cross section values are shown in Table V.

TABLE V. Results for the integrated cross section obtained from θ_μ and p_μ distributions on H_2O and CH targets. Different event selections were used for the angular differential cross section and the momentum differential cross section, which causes the ~1% difference in the cross sections for the H_2O target.

Kinematics	Target	Integrated cross section (10^{-39} cm^2/nucleon) Data	MC
θ_μ	H_2O	1.44 ± 0.21(stat + syst)	1.197
	CH	1.26 ± 0.18(stat + syst)	1.165
p_μ	H_2O	1.40 ± 0.28(stat + syst)	1.215
	CH	1.24 ± 0.17(stat + syst)	1.165

B. Differential cross section result

The results for the differential cross section in momentum (angle) bins are shown in Table VI (Table VII). The errors include both statistical and systematic contributions. The corresponding plots are shown in Fig. 14. The differential cross sections on the H_2O and CH targets are consistent within errors with the MC prediction in most of the bins. The H_2O and CH measurements are shown in Fig. 14.

C. Comparison with different interaction models

The reported measurement results were compared to predictions from MC generators GENIE and NEUT to see how well they agree with our measurements. The agreement between the measurement and models was quantified by the value of χ^2 defined by

TABLE VI. The results of the differential cross section measurement as a function of the muon momentum in units of $(\mathrm{cm^2})/(\mathrm{nucleon}\cdot\mathrm{GeV/c})$.

Target material	Range (GeV/c)	Cross section (10^{-39})	Error (10^{-39})	Relative error (%)	MC (10^{-39})	Data/MC
H_2O	0.3–0.5	1.794	0.707	39.4	1.225	1.464
	0.5–0.7	1.867	0.388	20.8	1.553	1.202
	0.7–0.9	1.099	0.365	33.2	1.010	1.089
	0.9–1.1	0.404	0.184	45.5	0.513	0.787
	1.1–1.5	0.133	0.138	103.5	0.259	0.514
	1.5–30.0	0.011	0.003	25.5	0.007	1.623
CH	0.3–0.5	1.309	0.373	28.5	1.227	1.067
	0.5–0.7	1.589	0.359	22.6	1.570	1.012
	0.7–0.9	1.013	0.283	28.0	1.034	0.980
	0.9–1.1	0.581	0.168	28.9	0.536	1.084
	1.1–1.5	0.244	0.077	31.5	0.266	0.919
	1.5–30.0	0.009	0.002	21.1	0.008	1.089

TABLE VII. The results of the differential cross section measurement as a function of the cosine of the muon scattering angle in units of cm^2/nucleon.

Target material	Range in cosine angle/angular bins	Cross section (10^{-39})	Error (10^{-39})	Relative error (%)	MC (10^{-39})	Data/MC
H_2O	0.34–0.71	1.097	0.311	28.4	0.884	1.241
	0.71–0.77	2.358	0.906	38.4	1.613	1.462
	0.77–0.91	2.326	0.440	18.9	2.329	0.998
	0.91–0.94	5.103	1.095	21.5	3.491	1.462
	0.94–0.97	5.922	1.519	25.7	4.080	1.451
	0.97–1.00	7.776	1.496	19.2	6.269	1.240
CH	0.34–0.71	0.911	0.184	20.2	0.895	1.018
	0.71–0.77	2.176	0.718	33.0	1.615	1.347
	0.77–0.91	2.639	0.402	15.2	2.357	1.133
	0.91–0.94	3.724	0.819	22.0	3.509	1.067
	0.94–0.97	4.882	1.087	22.3	4.392	1.196
	0.97–1.00	5.599	0.947	16.9	6.739	0.893

$$\chi^2 = \sum_{ij}^{N} \left(\left(\frac{d\sigma}{dx}\right)_{i,\mathrm{data}} - \left(\frac{d\sigma}{dx}\right)_{i,\mathrm{model}} \right) \mathbf{V}_{ij}{}^{-1} \times \left(\left(\frac{d\sigma}{dx}\right)_{j,\mathrm{data}} - \left(\frac{d\sigma}{dx}\right)_{j,\mathrm{model}} \right),$$

where N is the number of cross section bins, i and j are the ith and jth kinematic bins, respectively, and $\mathbf{V}_{ij}$ is the covariance matrix. The MC generators used in this study were as follows:

NEUT *alternative version*: We used NEUT with a different choice of interaction models. One difference was in the treatments of the nuclear ground state. The alternative model described the ground state with a global Fermi gas model [48]. The CCQE model was the Nieves 1p1h model without the RPA correction,

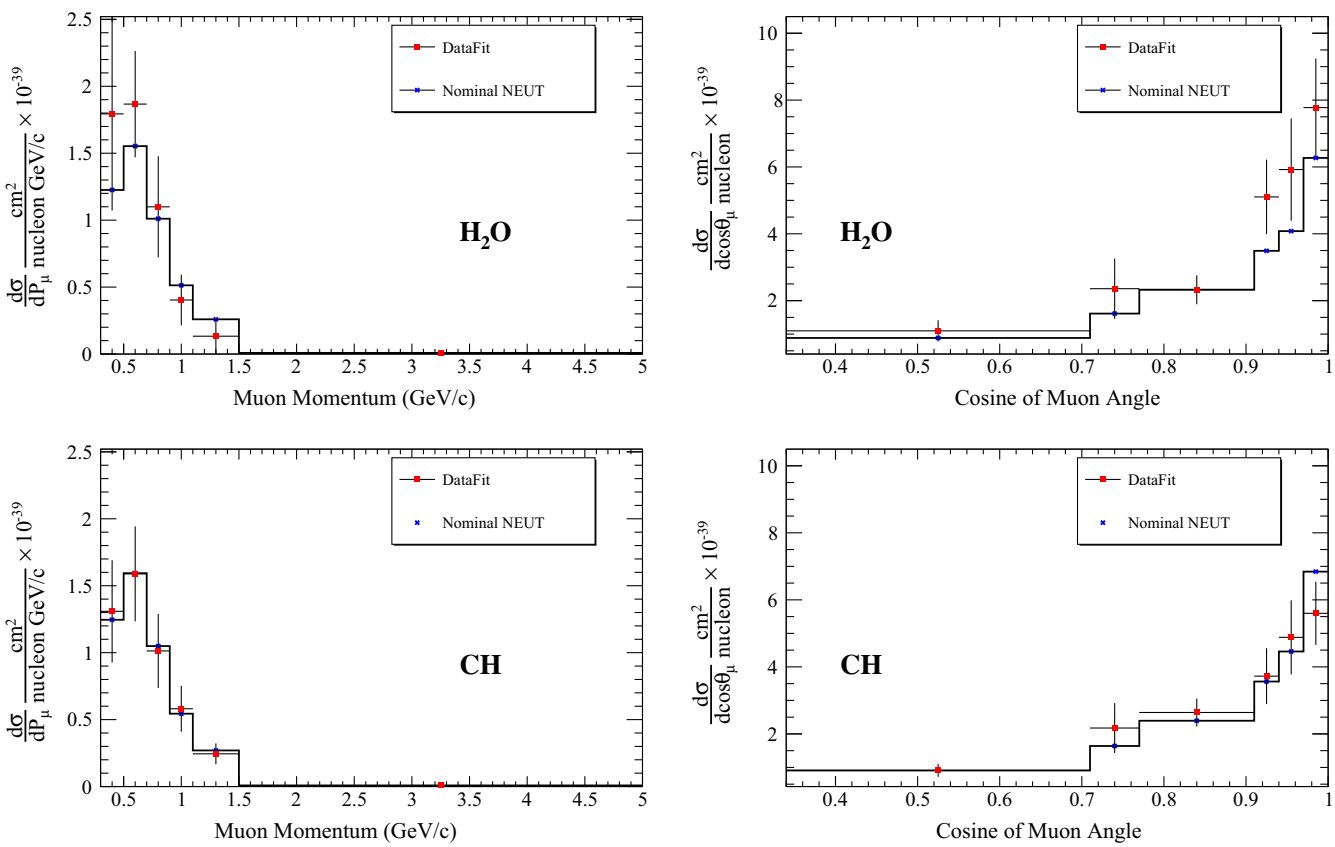

FIG. 14. Differential cross section result. The plots on the top refer to the H_2O target and the ones on the bottom to the CH target.

TABLE VIII. Comparison between the results obtained in this paper and those simulated with various models, as measured by the χ^2, see Sec. VII C. The number of degrees of freedom is 12.

	χ^2/NDF in momentum binning			χ^2/NDF in angle binning		
Model	CH	H_2O	total	CH	H_2O	total
NEUT nominal	0.493/12	5.619/12	6.673/12	4.040/12	5.082/12	9.005/12
NEUT alternative version	1.827/12	5.550/12	7.611/12	4.279/12	6.615/12	11.29/12
GENIE	1.086/12	6.030/12	7.667/12	2.199/12	4.783/12	6.955/12

with M_A^{QE} set to 1.03 GeV, compared to 1.21 GeV in the original NEUT model. The expected number of CCQE events decreased by about 15% in this model.

GENIE: GENIE allows for various combinations of interaction models to be simulated and tested. In this study the CCQE model was the same as NEUT but with a different M_A^{QE} (0.99 GeV). Final-state interactions were modeled with the hN model [49] and the treatment of the ground state of a nucleus was also different. The NEUT model utilized the Benhar SF model, whereas GENIE adopts a relativistic Fermi gas model.

The calculated χ^2 values are shown in Table VIII. Model predictions for the differential cross sections are shown in Fig. 15 together with the data points. The number of degrees of freedom is 12 for when binning the differential cross section by both momentum and cosine of the angle. No particular model is rejected or favored based on the results and all are within the stated experimental uncertainty. This result is consistent with the simulated data studies, where simulated data were generated by alternative NEUT and GENIE models, showing their agreement with the nominal NEUT model.

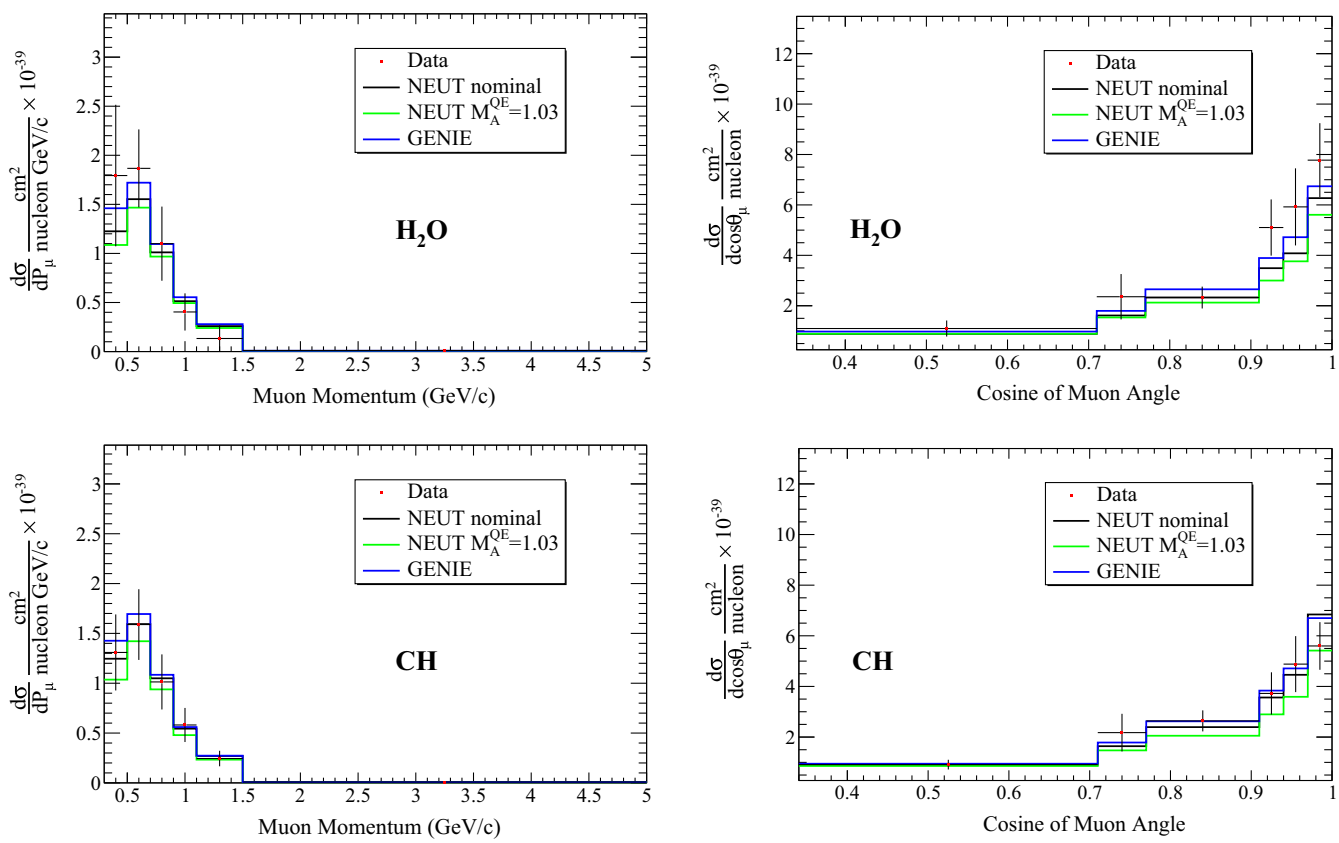

FIG. 15. Extracted differential cross section compared to nominal MC and alternative MC models as a function of P_μ and $\cos\theta_\mu$. Extracted differential cross section compared to nominal MC and alternative MC models (see the text) as a function of momentum (left) and cosine of muon angle (right). The H_2O results are shown on the top and CH results on the bottom. The color corresponds to each model; black, the nominal NEUT version; green, the alternative version of NEUT with M_A^{QE} set to 1.03 GeV/c^2; blue, GENIE; and red, post-fit ND tune.

VIII. CONCLUSIONS

In this paper we presented the measurement of the ν_μ cross section on H_2O and CH with the WAGASCI-BabyMIND using 2.96×10^{20} POT of data collected during J-PARC Run 10 (November 2019 to February 2020) and Run 11 (March to April 2021). This is the first ν_μ cross section measurement of neutrino interactions at 1.5° off-axis with T2K neutrino mode data. The results are consistent with the neutrino interaction model used for the T2K neutrino oscillation measurements. The data-MC agreement of the differential cross section is better in the momentum binning than in the angle binning with the current dataset, although the difference is not statistically significant. This study has laid the foundation for the next-generation of analyses with WAGASCI-BabyMIND. Future planned operations will further increase the datasets of WAGASCI-BabyMIND and we, therefore, expect future results to report measurements of neutrino interaction cross sections in water and carbon with the WAGASCI-BabyMIND with even greater precision, including double differential measurements on muon kinematics for events without charged pions. The measurement presented in this article is the first step toward using the data of the WAGASCI-BabyMIND to benefit future T2K neutrino oscillation analyses by validating the required neutrino interaction models.

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DATA AVAILABILITY

The data that support the findings of this article are openly available [50].

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