Search for 1^{-+} charmoniumlike hybrid via $e^+e^- \to \gamma\eta^{(\prime)}\eta_c$ at center-of-mass energies between 4.258 and 4.681 GeV

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Using e^+e^- collision data corresponding to an integrated luminosity of 10.6 fb^{-1} collected at center-of-mass energies between 4.258 and 4.681 GeV with the BESIII detector at the BEPCII collider, we search for the 1^{-+} charmoniumlike hybrid via $e^+e^- \to \gamma\eta\eta_c$ and $e^+e^- \to \gamma\eta'\eta_c$ decays for the first time. No significant signal is observed, and the upper limits on the Born cross sections for both processes are set at the 90% confidence level.

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I. INTRODUCTION

Quantum chromodynamics (QCD) allows the existence of exotic hadron states beyond the quark model, such as glueballs, hybrids, multiquark states, and hadronic molecules. The search for these QCD exotic states is crucial for quantitatively testing the theory of strong interactions in nonperturbative regions and for understanding confinement. However, it is difficult to distinguish the exotic hadron states from the conventional mesons. Hadrons with exotic J^{PC} quantum numbers, such as 0^{--}, even^{+-}, and odd^{-+}, cannot arise from ordinary $q\bar{q}$ states. Searching for such hadrons offers one of the most direct and unambiguous ways to establish the existence of exotic hadron states.

Lattice QCD predicts the existence of a series of light hybrid multiplets ($J^{PC} = 0^{-+}, 1^{--}, 1^{-+}$, and 2^{-+}), with the exotic 1^{-+} nonet being the lightest [1]. Similar to the case of the hybrid multiplets composed of light quarks ($n\bar{n}g$), $c\bar{c}$ can also form analogous hybrid multiplets ($c\bar{c}g$) [2,3]. In the charmonium sector, four confirmed states, $\psi(4230)$, $\psi(4360)$, $\psi(4390)$, and $\psi(4660)$, fall within the mass range expected for 1^{-+} hybrid charmonia [4–7].

Three light isovector states, the $\pi_1(1400)$, $\pi_1(1600)$, and $\pi_1(2015)$ [8–11], have been experimentally identified as exotic hadrons exhibiting the quantum numbers $J^{PC} = 1^{-+}$. Recently, BESIII collaboration performed a partial wave analysis of the $J/\psi \to \gamma\eta\eta'$ decay process, and reported the first observation of a nonconventional state $\eta_1(1855)$ with the exotic quantum numbers $I^G J^{PC} = 0^+1^{-+}$ [12,13]. However, no state with manifestly exotic J^{PC} has been observed in the charmonium region. Analogous to the $\eta_1(1855) \to \eta\eta'$ process, a possible η_{c1} state could decay into $\eta^{(\prime)}\eta_c$ final states. Additionally, some theoretical predictions suggest that the 1^{-+} charmoniumlike hybrid state might also decay to $\eta^{(\prime)}\eta_c$ final states [14,15].

In this paper, we report a study of $e^+e^- \to \gamma\eta^{(\prime)}\eta_c$ to search for the 1^{-+} charmoniumlike hybrid state based on data samples collected with the BESIII detector at center-of-mass (c.m.) energies between 4.258 and 4.681 GeV, listed in Table I. The integrated luminosities of these data samples are determined by analyzing large-angle Bhabha scattering events with an uncertainty of 1.0%, and the c.m. energies are measured using the di-muon process [16,17].

II. BESIII DETECTOR AND MONTE CARLO SIMULATION

The BESIII detector [18] records symmetric e^+e^- collisions provided by the BEPCII storage ring [19] in the c.m. energy range from 1.84 to 4.95 GeV, with a peak luminosity of 1.1×10^{33} $\text{cm}^{-2}\,\text{s}^{-1}$ achieved at $\sqrt{s} =$ 3.773 GeV. BESIII has collected large data samples in this energy region [20,21]. The cylindrical core of the BESIII detector covers 93% of the full solid angle and consists of a helium-based multilayer drift chamber (MDC), a time-of-flight system (TOF), and a CsI(Tl) electromagnetic calorimeter (EMC), which are all enclosed in a superconducting solenoidal magnet providing a 1.0 T magnetic field. The solenoid is supported by an octagonal flux-return yoke with resistive plate counter muon identification modules interleaved with steel. The charged-particle momentum resolution at 1 GeV/c is 0.5%, and the dE/dx resolution is 6% for electrons from Bhabha scattering. The EMC measures photon energies with a resolution of 2.5% (5%) at 1 GeV in the barrel (end cap) region. The time resolution of the plastic scintillator TOF in

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TABLE I. Datasets and results of the upper limits on Born cross sections of $e^+e^- \to \gamma\eta^{(\prime)}\eta_c$: the integrated luminosities $\mathcal{L}$, the upper limits of observed signal yields $N_{\rm UL}^{\rm obs}$, the ISR correction $(1+\delta)$, the vacuum polarization correction factor $\frac{1}{|1-\Pi|^2}$, the sum of the products of the branching fraction and efficiency $\sum \mathcal{B}_i\epsilon_i$, the upper limits of Born cross sections $\sigma_{\rm UL}^{\rm Born}$(pb), and the statistical significance $\mathcal{S}$.

		$e^+e^- \to \gamma\eta\eta_c$						$e^+e^- \to \gamma\eta'\eta_c$					
$\sqrt{s}$ (GeV)	$\mathcal{L}$(pb^{-1})	$1+\delta$	$\frac{1}{\lvert1-\Pi\rvert^2}$	$N_{\rm UL}^{\rm obs}$	$\sum_i(\mathcal{B}_i\epsilon_i)(\%)$	$\sigma_{\rm UL}^{\rm Born}$ (pb)	$\mathcal{S}(\sigma)$	$1+\delta$	$\frac{1}{\lvert1-\Pi\rvert^2}$	$N_{\rm UL}^{\rm obs}$	$\sum_i(\mathcal{B}_i\epsilon_i)(\%)$	$\sigma_{\rm UL}^{\rm Born}$ (pb)	$\mathcal{S}(\sigma)$
4.258	828.4	0.86	1.05	76.8	0.38	27.3	0.1	0.85	1.05	65.8	0.17	51.2	2.8
4.267	531.1	0.86	1.05	62.3	0.37	35.3	0.1	0.85	1.05	45.6	0.17	56.4	1.5
4.278	175.7	0.86	1.05	28.2	0.36	49.1	2.2	0.85	1.05	28.3	0.16	110.1	1.9
4.288	502.4	0.86	1.05	30.6	0.37	18.5	0.6	0.86	1.05	33.4	0.17	44.5	2.5
4.308	45.1	0.85	1.05	36.2	0.37	240.8	2.5	0.84	1.05	12.6	0.18	178.9	1.7
4.312	501.2	0.85	1.05	48.5	0.36	29.6	1.9	0.87	1.05	43.7	0.17	56.5	2.8
4.337	505.0	0.85	1.05	61.3	0.37	26.8	0.9	0.87	1.05	44.2	0.17	55.2	2.8
4.358	543.9	0.85	1.05	38.8	0.38	21.1	0.6	0.84	1.05	65.0	0.18	75.5	2.4
4.377	522.7	0.84	1.05	48.4	0.37	28.2	1.5	0.86	1.05	40.2	0.18	48.5	1.0
4.387	55.6	0.84	1.05	13.7	0.38	73.6	2.5	0.84	1.05	14.6	0.18	165.2	1.3
4.396	507.8	0.84	1.05	35.1	0.37	21.1	2.5	0.86	1.05	34.1	0.18	42.7	0.6
4.416	1043.9	0.83	1.05	45.2	0.37	13.2	0.1	0.84	1.05	70.9	0.18	41.9	2.3
4.436	569.9	0.83	1.05	91.3	0.38	49.3	1.1	0.85	1.05	32.4	0.18	35.3	1.1
4.467	111.1	0.82	1.05	27.5	0.38	77.1	0.8	0.82	1.05	13.7	0.18	79.3	0.9
4.527	112.1	0.81	1.05	60.0	0.38	38.9	2.0	0.81	1.05	16.2	0.19	90.0	1.0
4.574	48.9	0.79	1.05	24.1	0.38	179.7	1.5	0.79	1.05	12.6	0.20	158.7	0.4
4.600	586.9	0.78	1.05	60.6	0.38	32.7	2.4	0.78	1.05	17.4	0.20	18.4	0.9
4.611	103.65	0.77	1.05	24.0	0.38	78.5	0.7	0.77	1.05	12.9	0.20	78.3	0.1
4.628	521.53	0.77	1.05	77.6	0.38	48.8	1.3	0.77	1.05	27.4	0.20	33.7	1.2
4.641	551.65	0.76	1.05	28.7	0.38	17.3	2.2	0.76	1.05	25.1	0.20	28.8	0.2
4.661	529.43	0.75	1.05	55.9	0.38	35.4	1.2	0.75	1.05	29.0	0.20	34.4	1.5
4.681	1667.39	0.75	1.05	71.8	0.38	14.5	1.4	0.78	1.05	46.1	0.20	16.5	0.4

the barrel region is 68 ps, while that in the end cap region is 110 ps. In 2015, the end cap TOF system was upgraded with multigap resistive plate chamber technology, improving the time resolution to 60 ps, which benefits approximately 68% of the data used in this analysis [22–24].

Monte Carlo (MC) simulated data samples produced with a GEANT4-based software package [25], which includes the geometric description of the BESIII detector and the detector response, are used to determine detection efficiencies and to estimate backgrounds. The simulation models the beam energy spread and initial state radiation (ISR) in the e^+e^- annihilations with the generator KKMC [26,27]. In this analysis, 100,000 MC events are generated for each decay mode of η_c at each c.m. energy with KKMC and EVTGEN [28,29]. The inclusive MC samples include the production of open-charm processes, the ISR production of vector charmonium(like) states, and the continuum processes incorporated in KKMC. All particle decays are modeled with EVTGEN using branching fractions taken from the Particle Data Group (PDG) [30], when available, or otherwise estimated with LUNDCHARM [31]. Final-state radiation from charged final-state particles is incorporated using the PHOTOS package [32].

III. EVENT SELECTION AND STUDY OF BACKGROUND

To select candidate events for $e^+e^- \to \gamma\eta^{(\prime)}\eta_c$, the η' is reconstructed through the final states of $\eta\pi^+\pi^-$, the η_c is reconstructed through 16 hadronic final states: $p\bar{p}$, $2(\pi^+\pi^-)$, $2(K^+K^-)$, $K^+K^-\pi^+\pi^-$, $p\bar{p}\pi^+\pi^-$, $3(\pi^+\pi^-)$, $K^+K^-2(\pi^+\pi^-)$, $K^+K^-\pi^0$, $p\bar{p}\pi^0$, $K_S^0K^\pm\pi^\mp$, $K_S^0K^\pm\pi^\mp\pi^\pm\pi^\mp$, $\pi^+\pi^-\eta$, $K^+K^-\eta$, $2(\pi^+\pi^-)\eta$, $\pi^+\pi^-\pi^0\pi^0$, and $2(\pi^+\pi^-)\pi^0\pi^0$, in which K_S^0 is reconstructed from its $\pi^+\pi^-$ decay, π^0 and η from their $\gamma\gamma$ final state.

Charged tracks detected in the MDC must be within a polar angle (θ) range of $|\cos\theta| < 0.93$, where θ is defined with respect to the z-axis, the symmetry axis of the MDC. For charged tracks not originating from K_S^0 decays, the distance of closest approach to the interaction point (IP) must be less than 10 cm along the z-axis, $|V_z|$, and less than 1 cm in the transverse plane, $|V_{xy}|$. By combining the energy deposit dE/dx and the TOF information, the $\chi^2_{\rm PID}(i)$ (where $i = K$, π, or p) is calculated for each charged track under different hadron hypotheses. Both PID and kinematic fit information are used to determine the particle type of each charged track.

Photon candidates are identified using isolated showers in the EMC. The deposited energy of each shower must exceed 25 MeV in the barrel region ($|\cos\theta| < 0.80$) and 50 MeV in the end cap region ($0.86 < |\cos\theta| < 0.92$). To exclude showers that originate from charged tracks, the angle between the EMC shower position and the closest charged track at the EMC must exceed 10 degrees, as measured from the IP. To suppress electronic noise and unrelated showers, the difference between the EMC time and the event start time must be within the range [0,700] ns.

Each K_S^0 candidate is reconstructed from two oppositely charged tracks satisfying $|V_z| < 20$ cm. The two charged tracks are assigned as $\pi^+\pi^-$ without imposing additional PID criteria. They are constrained to originate from a common vertex and are required to have an invariant mass within $|M_{\pi^+\pi^-} - m_{K_S^0}| < 20$ MeV/c^2, where $m_{K_S^0}$ is the K_S^0 nominal mass [30]. The decay length of the K_S^0 candidate is required to be greater than twice the vertex resolution away from the IP. The $\pi^0(\eta)$ candidates are selected with the invariant mass of $\gamma\gamma$ pair satisfying $|M_{\gamma\gamma} - m_{\pi^0(\eta)}| < 15$ MeV/c^2, where $m_{\pi^0(\eta)}$ is the nominal mass of $\pi^0(\eta)$ [30]. To improve the energy resolution, a one-constraint (1C) kinematic fit is performed with a constraint on the $\pi^0(\eta)$ mass.

After the above selections, four-constraint (4C) kinematic fits are performed for each event, imposing overall energy-momentum conservation with the $3\gamma(\pi^+\pi^-) +$ hadrons hypothesis, where hadrons represents the corresponding final states of the η_c decay modes. The chi-square values of the 4C kinematic fit $\chi^2_{\mathrm{4C}(3\gamma+\mathrm{hadrons})}$ and $\chi^2_{\mathrm{4C}(3\gamma\pi^+\pi^-+\mathrm{hadrons})}$ are required to be less than 20 and 30, respectively, to suppress background events with different final states. For each η_c decay mode, if there are multiple combinations satisfying the above criteria, only the one with the minimum total chi-square $\chi^2_{\mathrm{tot}} = \chi^2_{\mathrm{4C}(3\gamma(\pi^+\pi^-)+\mathrm{hadrons})} + \chi^2_{\mathrm{PID}} + \chi^2_{\mathrm{1C}} + \chi^2_{\mathrm{vertex}}$ is retained, where χ^2_{PID} is the sum of the $\chi^2_{\mathrm{PID}}(i)$ for each charged track in the event, χ^2_{1C} is from the 1C kinematic fit for the $\pi^0(\eta)$ mass, and χ^2_{vertex} is the χ^2 of the K_S^0 secondary vertex fit. If there is no $\pi^0/\eta(K_S^0)$ in an event, the corresponding $\chi^2_{\mathrm{1C}}(\chi^2_{\mathrm{vertex}})$ is set to zero.

For the $e^+e^- \to \gamma\eta\eta_c$ process, 4C kinematic fits are performed by constraining energy-momentum conservation

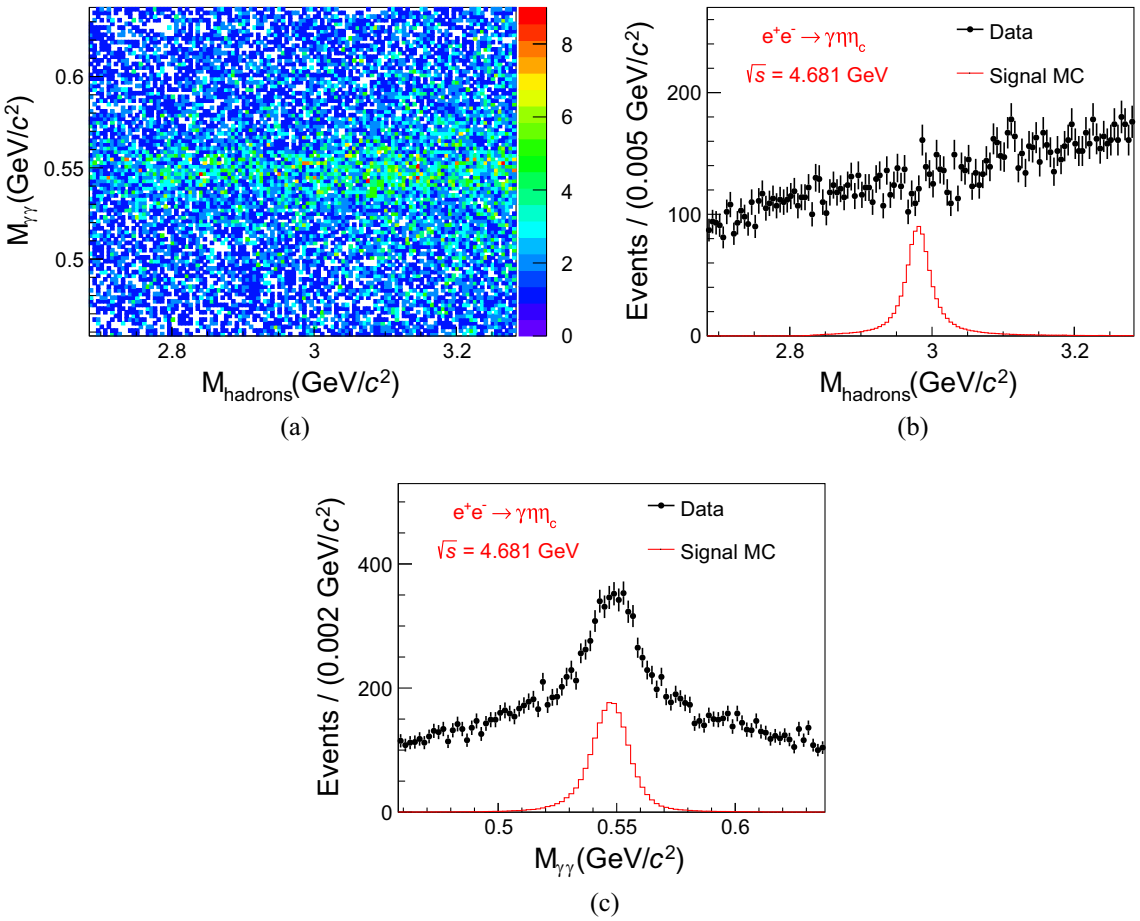


FIG. 1. The distributions of (a) $M_{\gamma\gamma}$ versus M_{hadrons}, (b) M_{hadrons}, and (c) $M_{\gamma\gamma}$ at $\sqrt{s} = 4.681$ GeV. For (b) and (c), the dots with error bars are data, and the red histograms represent the signal MC.

under the hypotheses $e^+e^- \to 2\gamma + \text{hadrons}$ and $e^+e^- \to 4\gamma + \text{hadrons}$, to suppress the backgrounds from processes with two or four photons in the final state. The $\chi^2_{4C(3\gamma+\text{hadrons})}$ is required to be less than all possible $\chi^2_{4C(2\gamma+\text{hadrons})}$ and $\chi^2_{4C(4\gamma+\text{hadrons})}$. In case of multiple η_c candidates in an event, the one with the invariant mass closest to the η_c nominal mass is selected to reconstruct the η_c meson. Finally, the remaining η candidate is chosen to reconstruct the η meson from the e^+e^- collision.

For the $e^+e^- \to \gamma\eta'\eta_c$ process, the η_c and η' candidates are formed from hadrons and $\eta\pi^+\pi^-$ combinations, respectively, with the least $\frac{(M_{\text{hadrons}}-m_{\eta_c})^2}{\sigma^2_{m_{\eta_c}}} + \frac{(M_{\eta\pi^+\pi^-}-m_{\eta'})^2}{\sigma^2_{m_{\eta'}}}$. Here, m_{η_c} and $m_{\eta'}$ are the nominal masses of η_c and η', respectively [30], M_{hadrons} is the invariant mass of the 16 different decay modes of η_c mentioned above, $M_{\eta\pi^+\pi^-}$ is the invariant mass of $\eta\pi^+\pi^-$, and $\sigma_{m_{\eta'}}$ and $\sigma_{m_{\eta_c}}$ are the visible widths, determined by fitting the individual distributions with a Gaussian function and a Breit-Wigner function, respectively.

After applying the reconstructed selection criteria to all data samples, the two-dimensional distributions of $M_{\gamma\gamma}$ versus M_{hadrons} and $M_{\eta\pi^+\pi^-}$ versus M_{hadrons} in data and MC simulation at $\sqrt{s} = 4.681$ GeV are shown in Figs. 1(a) and 2(a), where $M_{\gamma\gamma(\eta\pi^+\pi^-)}$ is the invariant mass of the reconstructed $\eta^{(\prime)}$ from e^+e^- collision. No significant $e^+e^- \to \gamma\eta^{(\prime)}\eta_c$ signals are observed in the projections of $M_{\gamma\gamma(\eta\pi^+\pi^-)}$ versus M_{hadrons}. The distributions of M_{hadrons} and $M_{\gamma\gamma(\eta\pi^+\pi^-)}$ at $\sqrt{s} = 4.681$ GeV are shown in Figs. 1(b), 1(c), 2(b), and 2(c). Additionally, the distribution of $M_{\gamma\gamma}$ used for the reconstruction of the η' is shown in Fig. 2(d).

Since the luminosity of data samples at $\sqrt{s} = 4.681$ GeV is the largest, we use the inclusive MC sample at this energy point, with the luminosity 40 times larger than the data to study the background components. After applying the mentioned selection criteria to the inclusive MC sample, no significant peaking backgrounds containing both η_c and $\eta^{(\prime)}$ simultaneously are observed. However, for the $e^+e^- \to \gamma\eta\eta_c$ process, there are some background

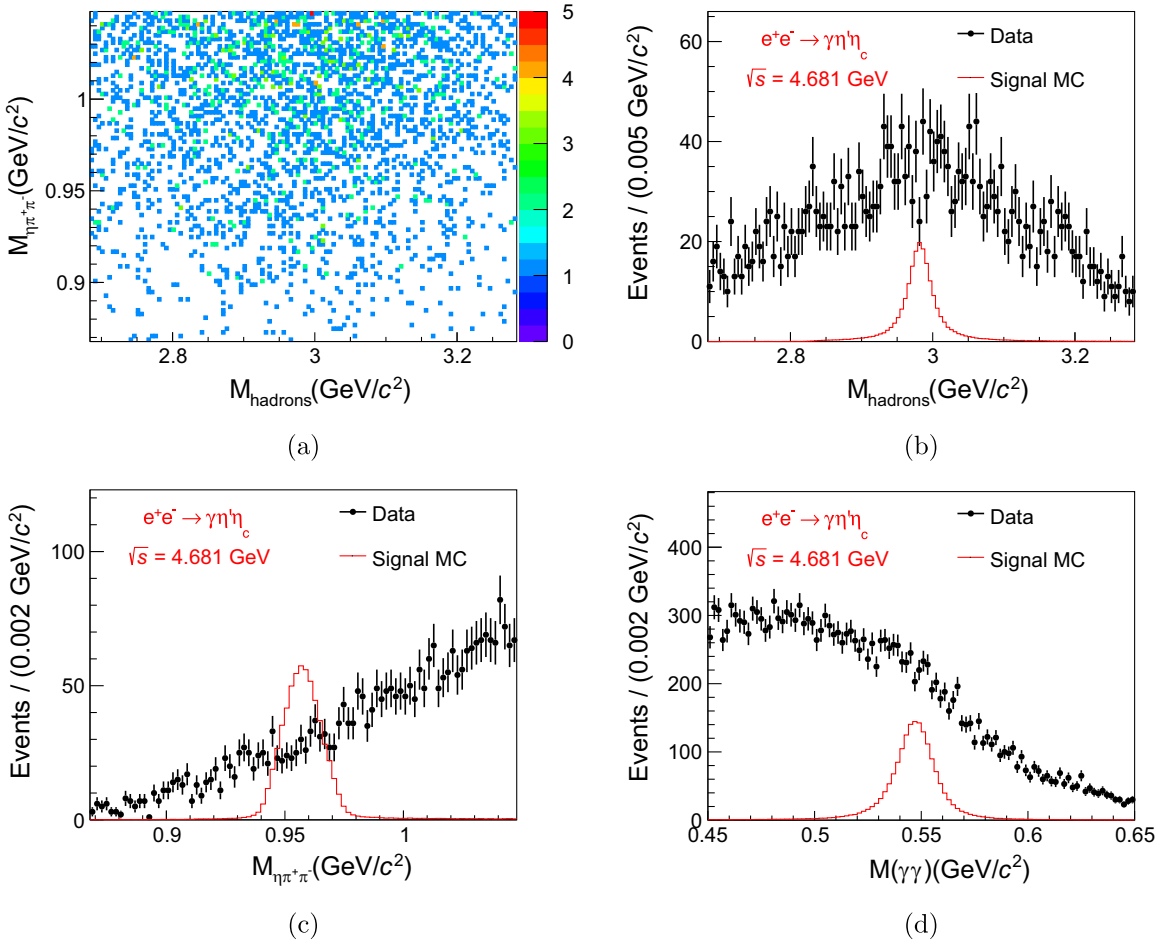


FIG. 2. The distributions of (a) $M_{\eta\pi^+\pi^-}$ versus M_{hadrons}, (b) M_{hadrons}, (c) $M_{\eta\pi^+\pi^-}$, and (d) $M_{\gamma\gamma}$ at $\sqrt{s} = 4.681$ GeV. For (b), (c), and (d), the dots with error bars are data, and the red histograms represent the signal MC.

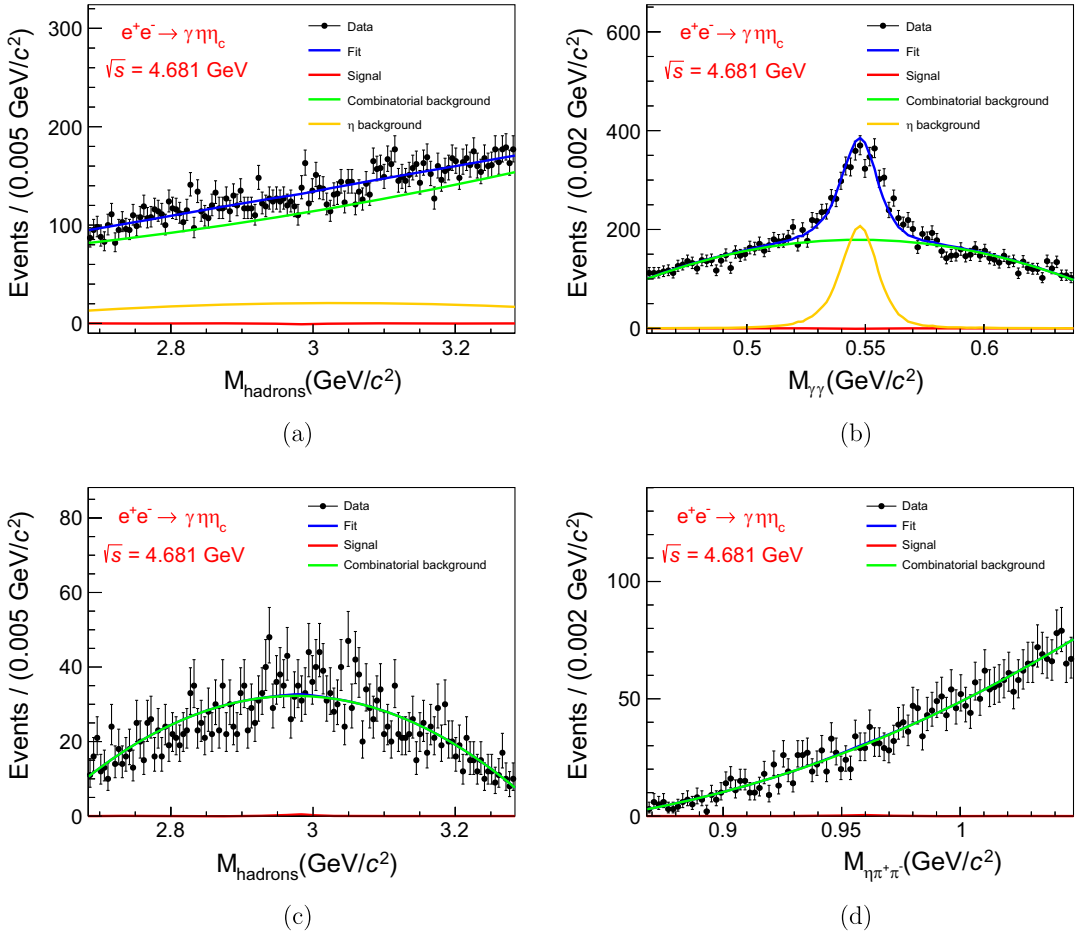


FIG. 3. Fits to the invariant mass distributions of (a, c) $M_{\rm hadrons}$, (b) $M_{\gamma\gamma}$, and (d) $M_{\eta\pi^+\pi^-}$ at $\sqrt{s} = 4.681$ GeV. The black dots with error bars are data, the red solid lines are the MC signals, the green solid lines are the flat background, and the orange solid lines indicate the background containing η.

events containing η mesons. These backgrounds are considered in the two-dimensional fit, as shown in Sec. IV.

IV. SIGNAL YIELD EXTRACTION

The signal yield of the $e^+e^- \to \gamma\eta^{(\prime)}\eta_c$ process is determined through an unbinned maximum likelihood fit to the two-dimensional distribution of $M_{\gamma\gamma(\eta\pi^+\pi^-)}$ versus $M_{\rm hadrons}$. The fit ranges are set as follows: $[0.458, 0.638]$ GeV/c^2 (for $M_{\gamma\gamma}$), $[0.868, 1.048]$ GeV/c^2 (for $M_{\eta\pi^+\pi^-}$), and $[2.684, 3.284]$ GeV/c^2 (for $M_{\rm hadrons}$). The signal is described by a combination of 16 weighted shapes obtained from the signal MC, where the weight is $\frac{\mathcal{B}_i\epsilon_i}{\sum_i \mathcal{B}_i\epsilon_i}$. Here, $\mathcal{B}_i$ denotes the branching fraction of the η_c decay to the ith decay mode, and ϵ_i represents the detection efficiency obtained from MC samples.

For the $e^+e^- \to \gamma\eta\eta_c$ process, the backgrounds are modeled using two distinct components, each described by a two-dimensional probability density function (PDF). The first component, corresponding to backgrounds containing only η, is parametrized using the MC shape of η in the $M_{\gamma\gamma}$ distribution, obtained from the MC sample, combined with a second-order Chebyshev polynomial in the $M_{\rm hadrons}$ distribution. The second component, representing the remaining backgrounds, is described by a two-dimensional second-order Chebyshev polynomial. For the $e^+e^- \to \gamma\eta'\eta_c$ process, since there is no background containing η', the background is described solely by a two-dimensional second-order Chebyshev polynomial. The two-dimensional fit results of η_c and $\eta(\eta')$, projected onto the distributions of $M_{\rm hadrons}$ and $M_{\gamma\gamma(\eta\pi^+\pi^-)}$ at $\sqrt{s} = 4.681$ GeV, are shown in Fig. 3. The signal yield of $e^+e^- \to \gamma\eta^{(\prime)}\eta_c$ at $\sqrt{s} = 4.681$ GeV is $-9.9 \pm 40.0 (5.2 \pm 11.2)$ with a statistical significance of $1.4\sigma(0.4\sigma)$. The significance is calculated from the change in the negative log-likelihood function lnL with and without assuming the presence of signal, while considering the change in degrees of freedom in the fits. The significance at other energy points is listed in Table I.

V. UPPER LIMIT ON BORN CROSS SECTIONS

The Born cross sections of $e^+e^- \to \gamma\eta^{(\prime)}\eta_c$ are calculated by

$$\sigma^{\rm Born} = \frac{N^{\rm obs}}{\mathcal{L}\cdot(1+\delta)\cdot\frac{1}{|1-\Pi|^2}\cdot\mathcal{B}\cdot\epsilon}. \quad (1)$$

Here, $N^{\rm obs}$ is the signal yield, $\mathcal{L}$ is the integrated luminosity of the data sample taken at each c.m. energy, and $\frac{1}{|1-\Pi|^2}$ is the vacuum polarization factor [33]. For $e^+e^- \to \gamma\eta\eta_c$, $\mathcal{B}\cdot\epsilon = \mathcal{B}(\eta\to\gamma\gamma)\sum_i \mathcal{B}_i\epsilon_i$, while for $e^+e^- \to \gamma\eta'\eta_c$, $\mathcal{B}\cdot\epsilon = \mathcal{B}(\eta'\to\eta\pi^+\pi^-)\mathcal{B}(\eta\to\gamma\gamma)\sum_i \mathcal{B}_i\epsilon_i$, where $\mathcal{B}(\eta\to\gamma\gamma)$ and $\mathcal{B}(\eta'\to\eta\pi^+\pi^-)$ are the branching fractions of $\eta\to\gamma\gamma$ and $\eta'\to\eta\pi^+\pi^-$ taken from the PDG [30]. Then, $1+\delta$ is the radiative (ISR) correction factor, which is defined as

$$(1+\delta) = \frac{\int \sigma^{\rm dress}(s(1-x))F(x,s)dx}{\sigma^{\rm dress}(s)}. \quad (2)$$

Here, $F(x,s)$ is the radiator function, which is known from a QCD calculation with an accuracy of 0.1% [34], s is the square of the c.m. energy, and $x = 2E_{\gamma\rm ISR}/\sqrt{s}$, where $E_{\gamma\rm ISR}$ is the energy of the ISR photon. The $\sigma^{\rm dress}(s)$ is the dressed cross section.

Since no significant $e^+e^- \to \gamma\eta^{(\prime)}\eta_c$ signal is observed, we set the upper limit at the 90% confidence level (C.L.) on $\sigma(e^+e^- \to \gamma\eta^{(\prime)}\eta_c)$, incorporating the systematic uncertainty and using the Bayesian method [35]. The likelihood that produces the most conservative upper limit is selected after considering the additive systematic terms. To incorporate the multiplicative terms into the Born cross section limit, the probability of the signal yield $P(N)$ determined using a maximum likelihood fit is convolved with a PDF of the sensitivity. The details of systematic uncertainties can be found in Sec. VI. The upper limits of the signal yields ($N^{\rm obs}_{\rm UL}$) at the 90% C.L. are determined by

$$0.9\int_0^\infty P(N)dN = \int_0^{N^{\rm obs}_{\rm UL}} P(N)dN. \quad (3)$$

Using Eq. (1), we set the upper limits on the Born cross sections for $e^+e^- \to \gamma\eta^{(\prime)}\eta_c$ at 90% C.L. The results are summarized in Table I.

VI. SYSTEMATIC UNCERTAINTY

The sources of systematic uncertainties are categorized into two types: additive and multiplicative terms. The additive uncertainties arise from the fit range, signal shape, background shape, and the difference between the MC sample and data. A conservative approach is adopted by considering all possible variations and selecting the one that yields the largest upper limit, as follows:

(i) The systematic uncertainty arising from the fit range is determined by varying the fit ranges of $M_{\gamma\gamma(\eta\pi^+\pi^-)}$ and $M_{\rm hadrons}$ by ±5 MeV/c^2 and ±10 MeV/c^2.

(ii) The nominal mass and width of η_c are 2984.1 MeV/c^2 and 30.5 MeV, respectively [30]. The uncertainty associated with the η_c shape is estimated by changing its mass and width parameters within their uncertainties.

(iii) The uncertainty due to the background shape is estimated by replacing the function from the second-order Chebyshev polynomial with both the first-order and the third-order Chebyshev polynomials.

(iv) The uncertainty due to the difference of mass resolution between data and MC simulation is estimated by convolving a Gaussian function to η_c signal shape, where the mean value is varied by ±1 MeV/c^2, and the standard derivation is varied by 1, 2, and 3 MeV/c^2. For the $e^+e^- \to \gamma\eta\eta_c$ process, the η signal shape is convolved with a Gaussian function parametrized by free parameters.

The multiplicative systematic uncertainty is considered by convolving a Gaussian function to the likelihood distribution. These uncertainties include the following sources:

(i) The integrated luminosity is determined using Bhabha scattering events, with a relative uncertainty of 1.0% uniformly assigned to all the measured energy points [16,17].

(ii) The systematic uncertainty of the ISR correction factor $1+\delta$ is estimated by comparing the difference between factors obtained by the flat line shape and $\psi(4660)$, with mass set to 4641 MeV/$c^2 \pm 5$, 10 MeV/c^2, and width to 73 MeV $\pm$ 5, 10 MeV/c^2.

(iii) The parts of the Born cross sections' uncertainties associated with the branching fraction are calculated by $\frac{\sqrt{\sum_{i=1}^{16}(\epsilon_i\cdot\delta\mathcal{B}_i)^2}}{\sum_{i=1}^{16}(\epsilon_i\cdot\mathcal{B}_i)}$, where $\delta\mathcal{B}_i$ is the total branching fraction uncertainty after error propagation. The uncertainties of the branching fractions of $\eta_c \to$ hadrons are obtained from the BESIII measurement result [36], and the others are from the PDG [30].

(iv) The uncertainty from tracking or PID for charged tracks is determined to be 1.0% per track using the control samples $J/\psi \to \pi^+\pi^-\pi^0$, $J/\psi \to p\bar{p}\pi^+\pi^-$, and $J/\psi \to K^0_S K^\pm\pi^\mp$ + c.c. [37].

(v) The systematic uncertainty due to the photon detection is assigned as 1.0% per photon by analyzing the control samples $J/\psi \to \rho^0\pi^0$ and $e^+e^- \to \gamma\gamma$ [38].

(vi) The systematic uncertainty due to the K^0_S reconstruction is studied using control samples $J/\psi \to K^{*\pm}K^\mp$ and $J/\psi \to \phi K^0_S K^\pm\pi^\mp$, and estimated to be 1.0% [39].

TABLE II. Relative systematic uncertainties (%) on $\sigma^{\rm Born}(e^+e^- \to \gamma\eta^{(\prime)}\eta_c)$ at $\sqrt{s} = 4.681$ GeV.

Source		$\sigma^{\rm Born}(e^+e^- \to \gamma\eta\eta_c)$	$\sigma^{\rm Born}(e^+e^- \to \gamma\eta'\eta_c)$
Luminosity		1.0	1.0
ISR correction		3.3	0.9
$\sum_i \mathcal{B}_i\epsilon_i$	$\mathcal{B}_{\eta_c\to X_i}$	18.1	18.1
	Tracking	3.3	5.1
	Photon selection	3.0	3.1
	PID	3.3	5.1
	K_S^0 reconstruction	0.1	0.1
	π^0 reconstruction	0.4	0.4
	η reconstruction	0.3	0.3
	Kinematic fit	1.1	1.0
	Contamination	1.2	0.6
Total		19.3	19.9

(vii) Using a high-purity control sample of $J/\psi \to \pi^0 p\bar{p}$ or $J/\psi \to \eta p\bar{p}$, the systematic uncertainty from the π^0 or η reconstruction is determined to be 1.0% [40].

(viii) The systematic uncertainty associated with the kinematic fit is assigned as the difference between the detection efficiencies before and after the helix parameter corrections [41] in the signal MC simulation.

(ix) The contamination among the 16 decay modes of η_c is calculated by using the signal MC simulation.

Table II summarizes the multiplicative systematic uncertainties. All sources are treated as uncorrelated, and the total systematic uncertainty is obtained by adding them in quadrature.

VII. SUMMARY

Based on e^+e^- annihilation data corresponding to an integrated luminosity of 10.6 fb^{-1} collected with the BESIII detector at the BEPCII collider for c.m. energies in the range $\sqrt{s} = 4.258$–4.681 GeV, we searched for the 1^{-+} charmoniumlike hybrid via $e^+e^- \to \gamma\eta^{(\prime)}\eta_c$ for the first time. No significant signal was observed, and the upper limits at the 90% C.L. on the Born cross sections for $e^+e^- \to \gamma\eta\eta_c$ and $e^+e^- \to \gamma\eta'\eta_c$ were determined. Some theoretical calculations also predict that η_{c1} can decay to the open-charm final states, such as $D_1\bar{D}$, $D^*\bar{D}$ and $D^*\bar{D}^*$ [15]. With future datasets of higher statistics, searches for the η_{c1} in these final states can be further explored.

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DATA AVAILABILITY

The data that support the findings of this article are not publicly available upon publication because it is not technically feasible and/or the cost of preparing, depositing, and hosting the data would be prohibitive within the terms of this research project. The data are available from the authors upon reasonable request.

APPENDIX

Figures 4–8 display the distributions of $M_{\gamma\gamma}$ versus $M_{\rm hadrons}$, $M_{\rm hadrons}$, and $M_{\gamma\gamma}$ for each data sample. Figures 9–12 display the distributions of $M_{\eta\pi^+\pi^-}$ versus $M_{\rm hadrons}$, $M_{\rm hadrons}$, $M_{\eta\pi^+\pi^-}$, and $M_{\gamma\gamma}$ for each data sample. Figures 13–16 are the fit results to the invariant mass distributions for each data sample.

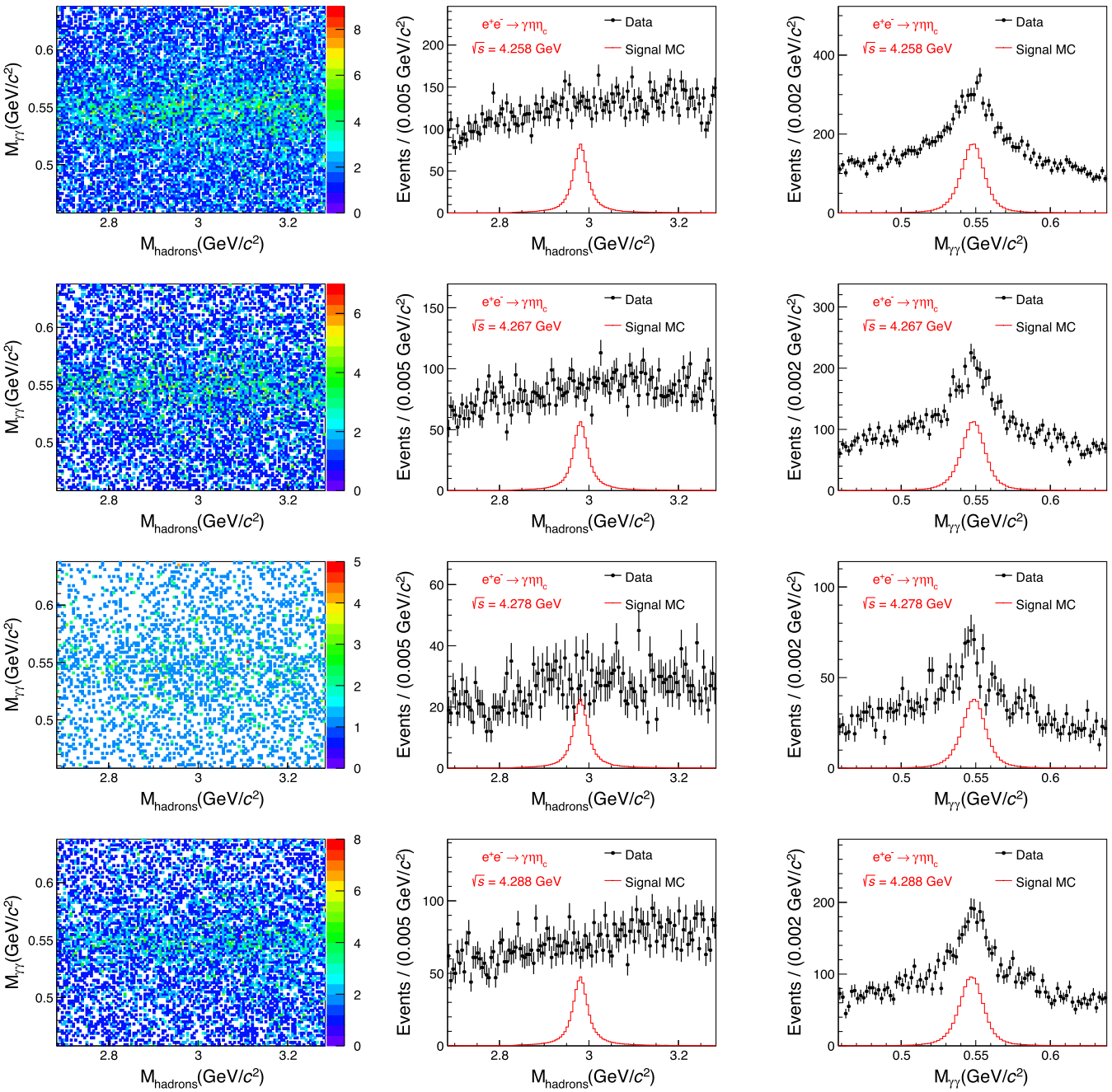


FIG. 4. The distributions of (left) $M_{\rm hadrons}$ versus $M_{\gamma\gamma}$, (middle) $M_{\rm hadrons}$, and (right) $M_{\gamma\gamma}$ for $e^+e^- \to \gamma\eta\eta_c$ candidate events. The rows show the distributions at $\sqrt{s} = 4.258$–4.288 GeV.

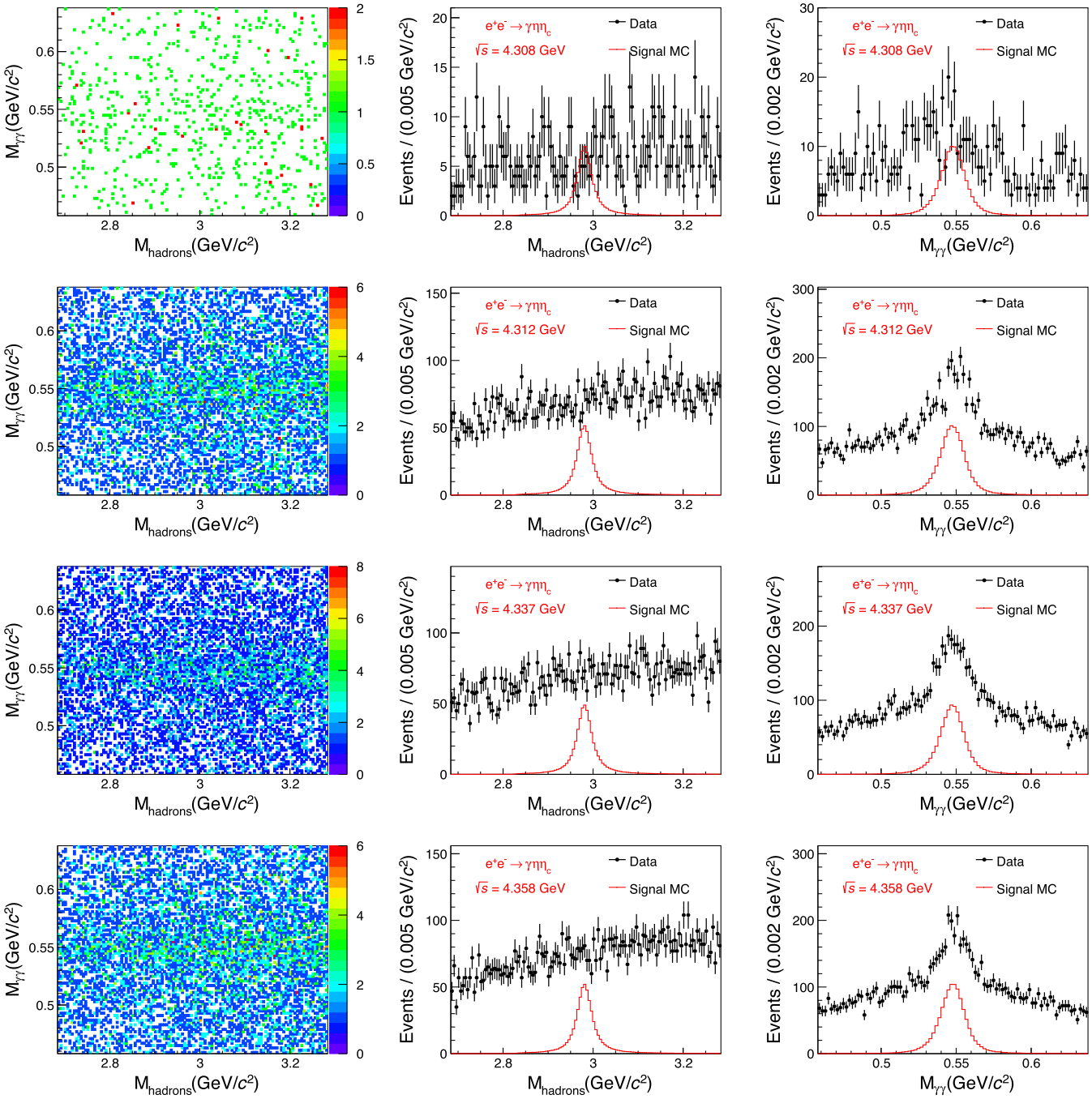


FIG. 5. The distributions of (left) $M_{\rm hadrons}$ versus $M_{\gamma\gamma}$, (middle) $M_{\rm hadrons}$, and (right) $M_{\gamma\gamma}$ for $e^+e^- \to \gamma\eta\eta_c$ candidate events. The rows show the distributions at $\sqrt{s} = 4.308$–4.358 GeV.

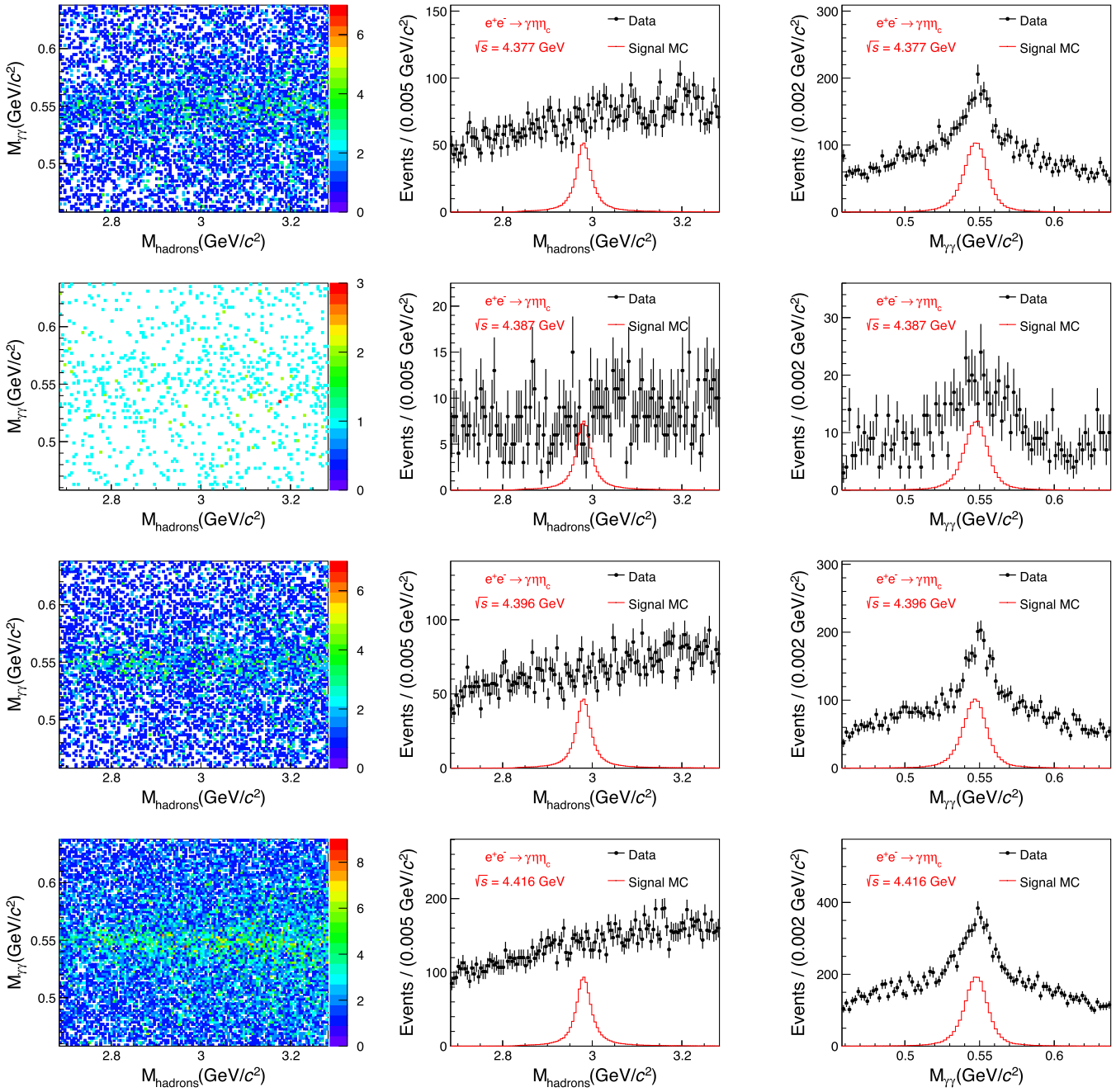


FIG. 6. The distributions of (left) $M_{\rm hadrons}$ versus $M_{\gamma\gamma}$, (middle) $M_{\rm hadrons}$, and (right) $M_{\gamma\gamma}$ for $e^+e^- \to \gamma\eta\eta_c$ candidate events. The rows show the distributions at $\sqrt{s} = 4.377$–4.416 GeV.

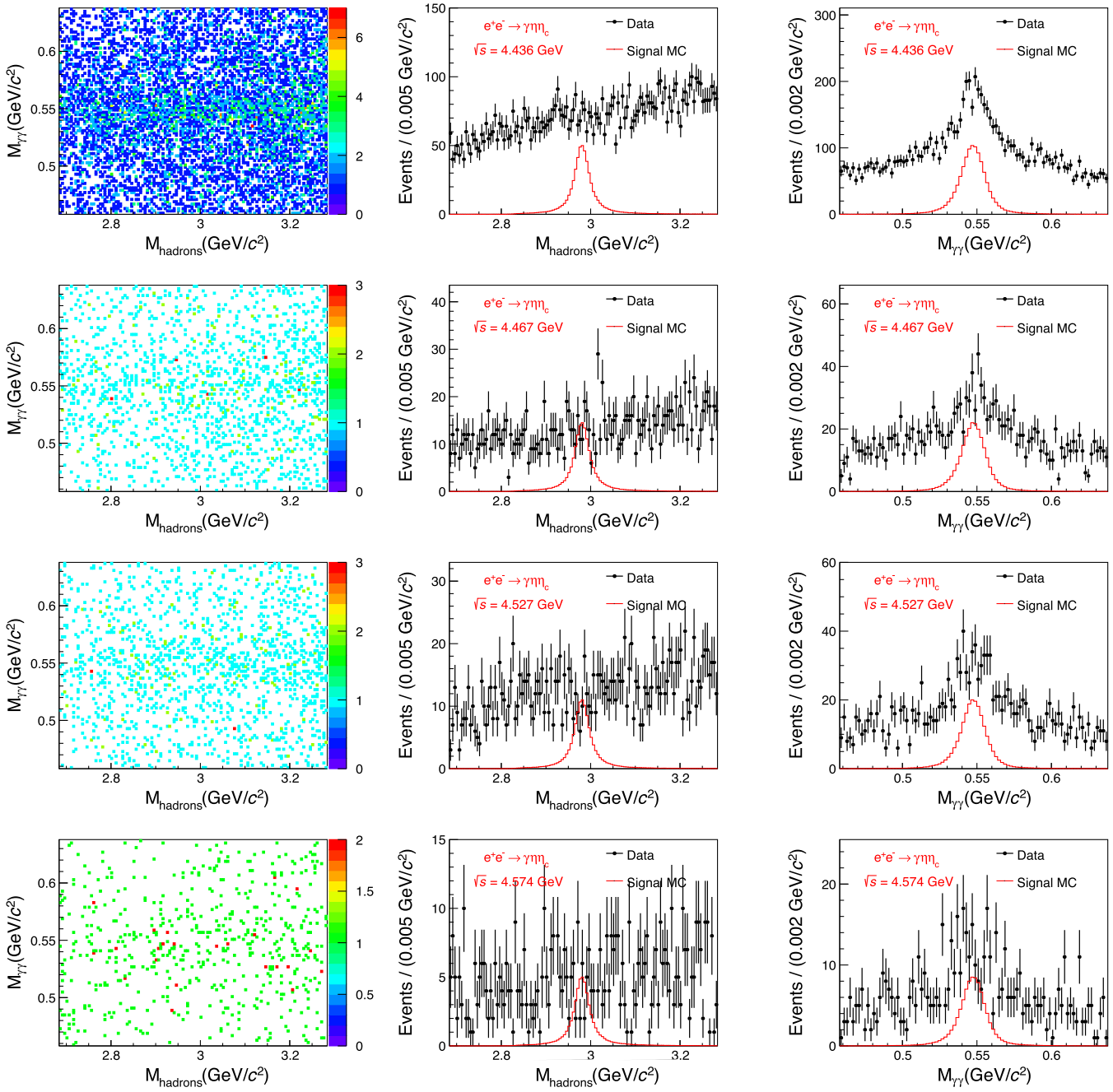


FIG. 7. The distributions of (left) $M_{\rm hadrons}$ versus $M_{\gamma\gamma}$, (middle) $M_{\rm hadrons}$, and (right) $M_{\gamma\gamma}$ for $e^+e^- \to \gamma\eta\eta_c$ candidate events. The rows show the distributions at $\sqrt{s} = 4.436$–4.574 GeV.

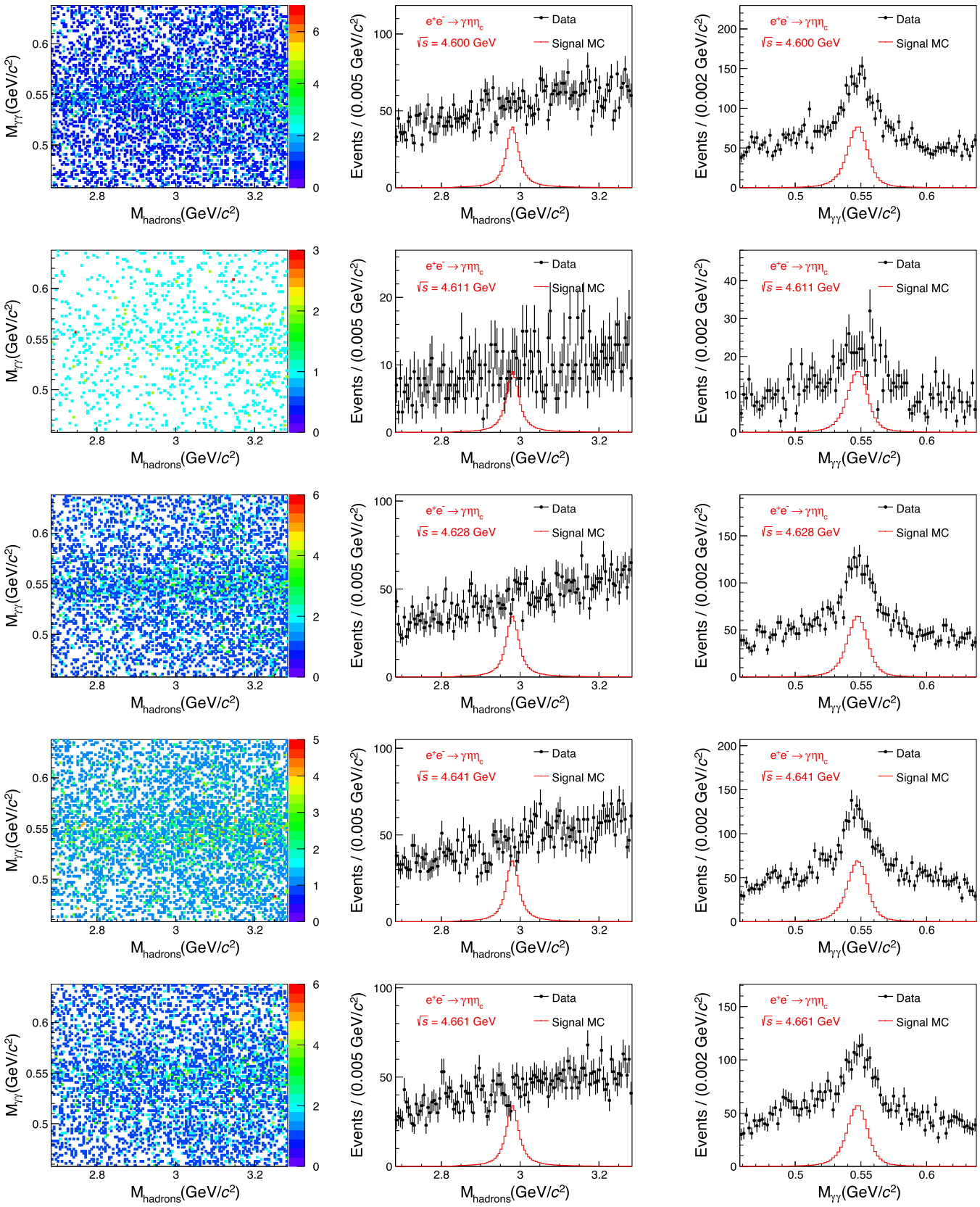


FIG. 8. The distributions of (left) $M_{\rm hadrons}$ versus $M_{\gamma\gamma}$, (middle) $M_{\rm hadrons}$, and (right) $M_{\gamma\gamma}$ for $e^+e^- \to \gamma\eta\eta_c$ candidate events. The rows show the distributions at $\sqrt{s} = 4.600$–4.661 GeV.

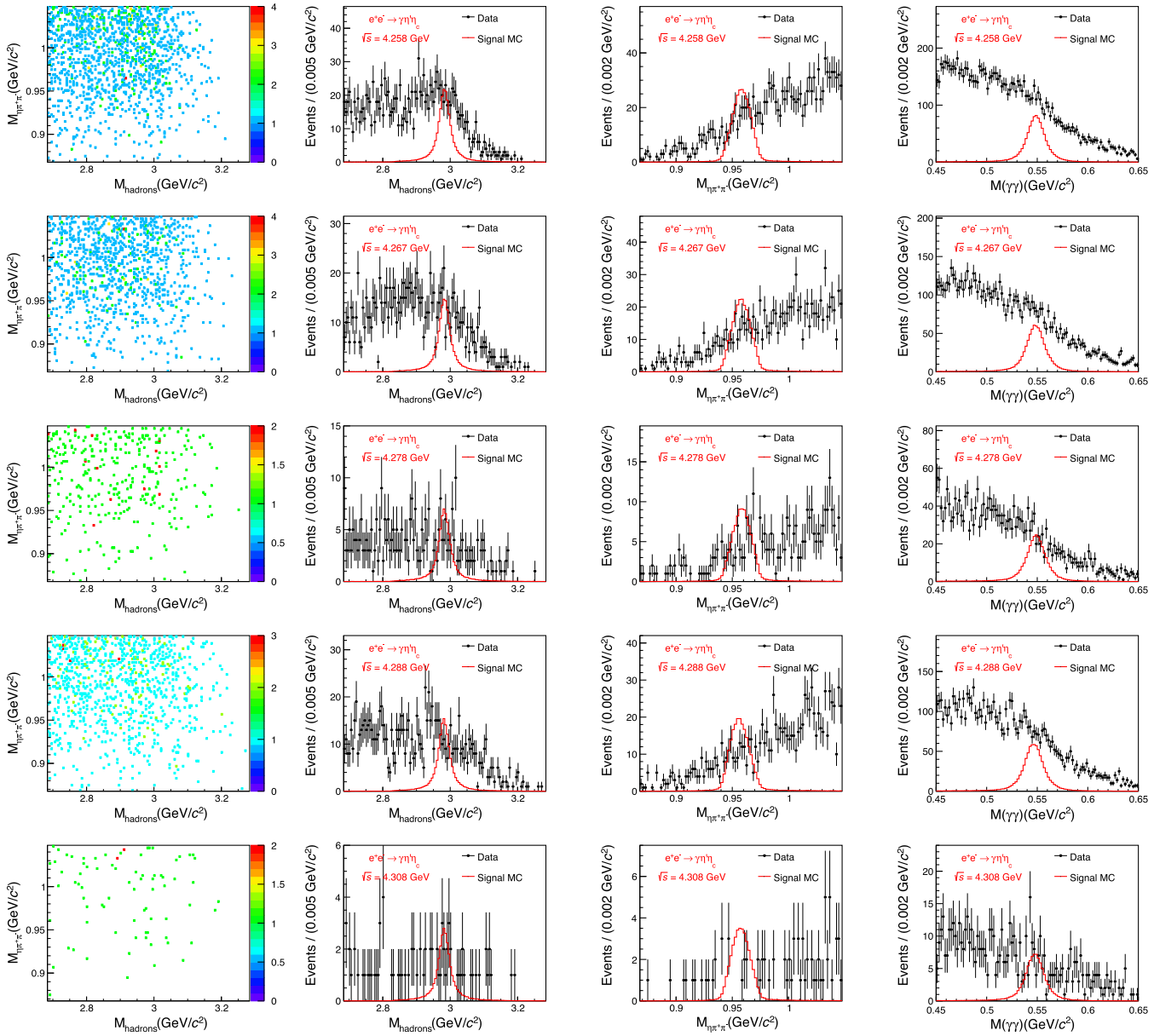


FIG. 9. The distributions of (left) $M_{\rm hadrons}$ versus $M_{\eta\pi^+\pi^-}$, (middle left) $M_{\rm hadrons}$, (middle right) $M_{\eta\pi^+\pi^-}$, and (right) $M_{\gamma\gamma}$ for $e^+e^- \to \gamma\eta'\eta_c$ candidate events. The rows show the distributions at $\sqrt{s} = 4.258$–4.308 GeV.

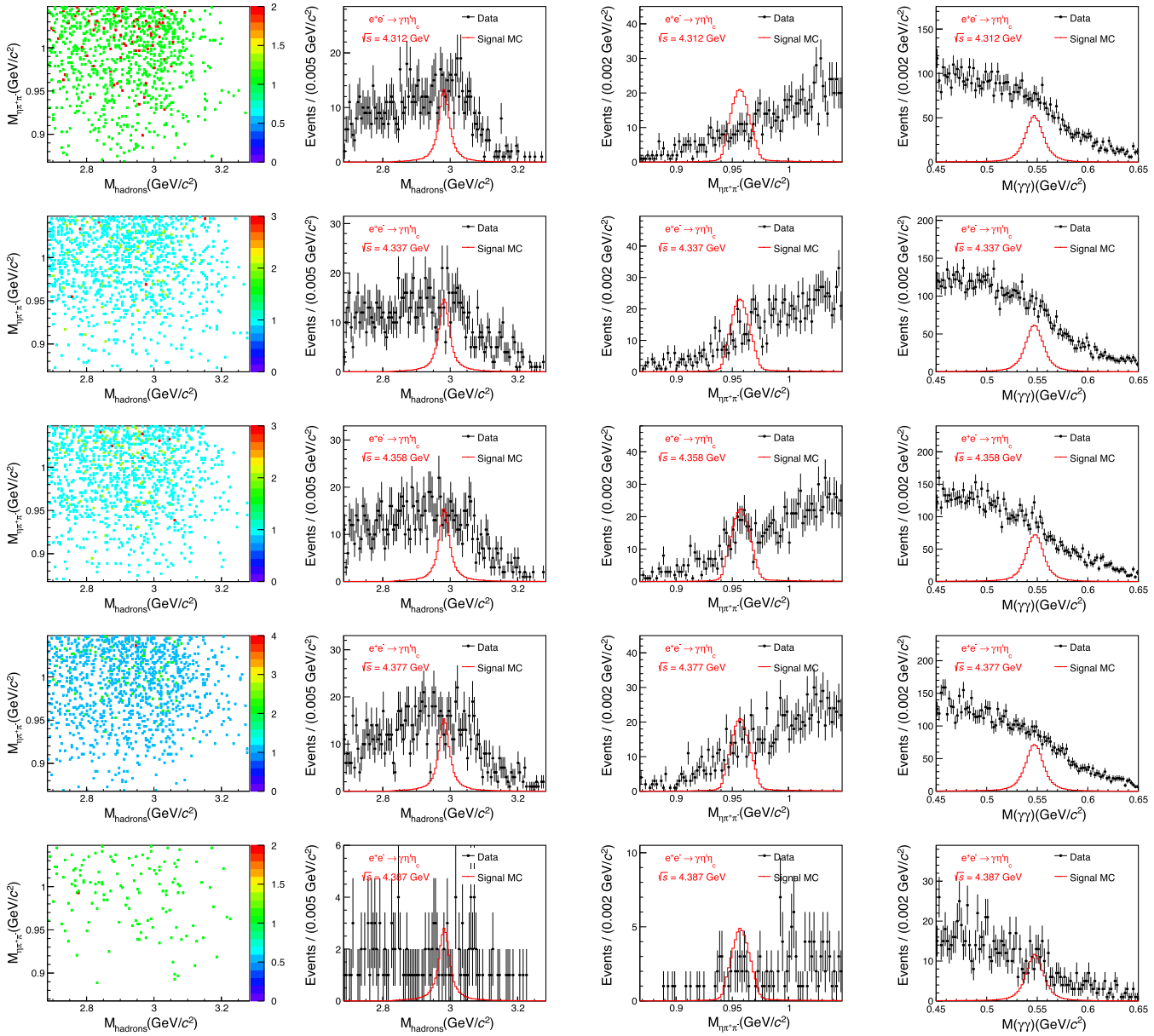


FIG. 10. The distributions of (left) $M_{\rm hadrons}$ versus $M_{\eta\pi^+\pi^-}$, (middle left) $M_{\rm hadrons}$, (middle right) $M_{\eta\pi^+\pi^-}$, and (right) $M_{\gamma\gamma}$ for $e^+e^- \to \gamma\eta'\eta_c$ candidate events. The rows show the distributions at $\sqrt{s} = 4.312$–4.387 GeV.

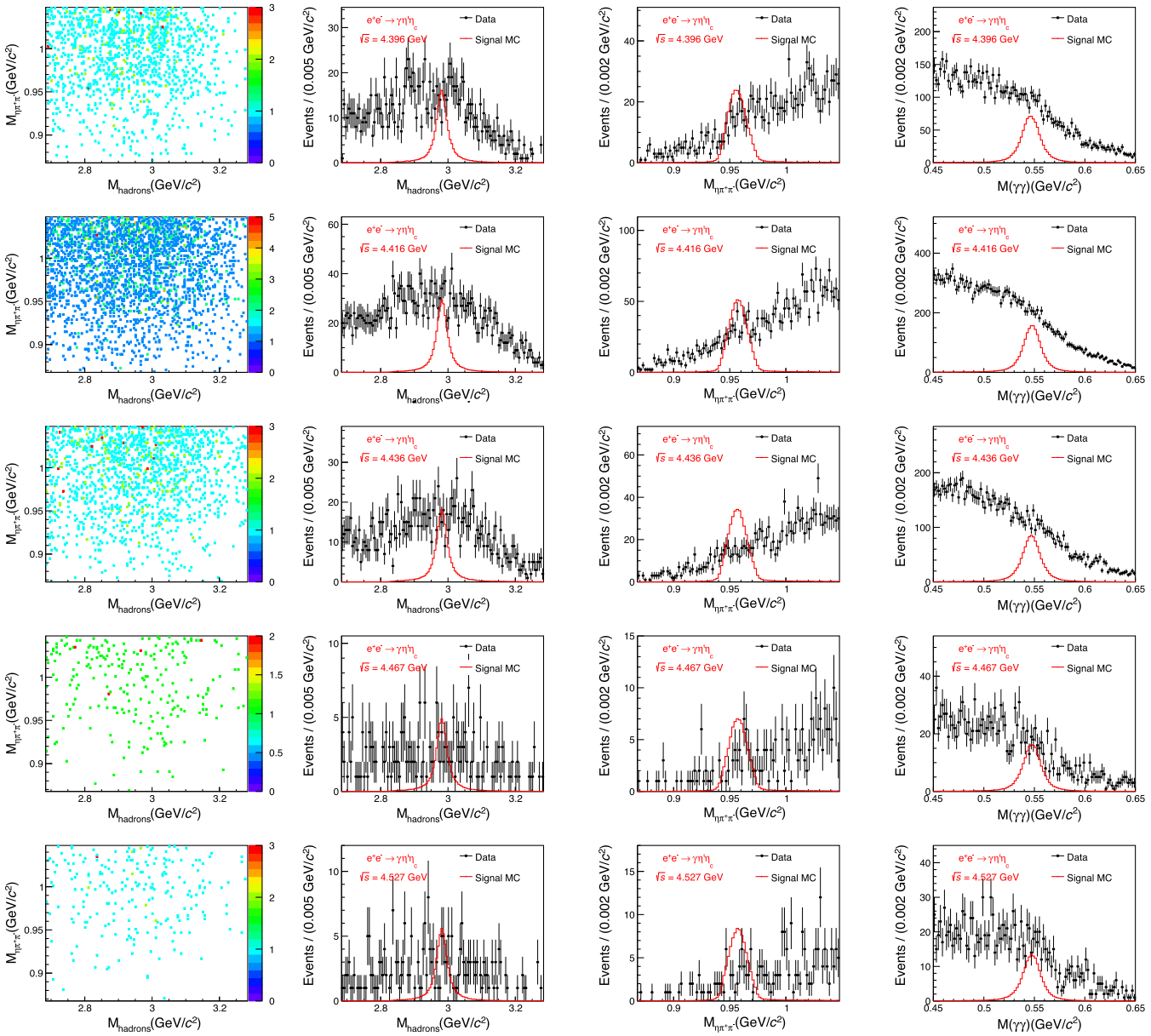


FIG. 11. The distributions of (left) $M_{\rm hadrons}$ versus $M_{\eta\pi^+\pi^-}$, (middle left) $M_{\rm hadrons}$, (middle right) $M_{\eta\pi^+\pi^-}$, and (right) $M_{\gamma\gamma}$ for $e^+e^- \to \gamma\eta'\eta_c$ candidate events. The rows show the distributions at $\sqrt{s} = 4.396$–4.527 GeV.

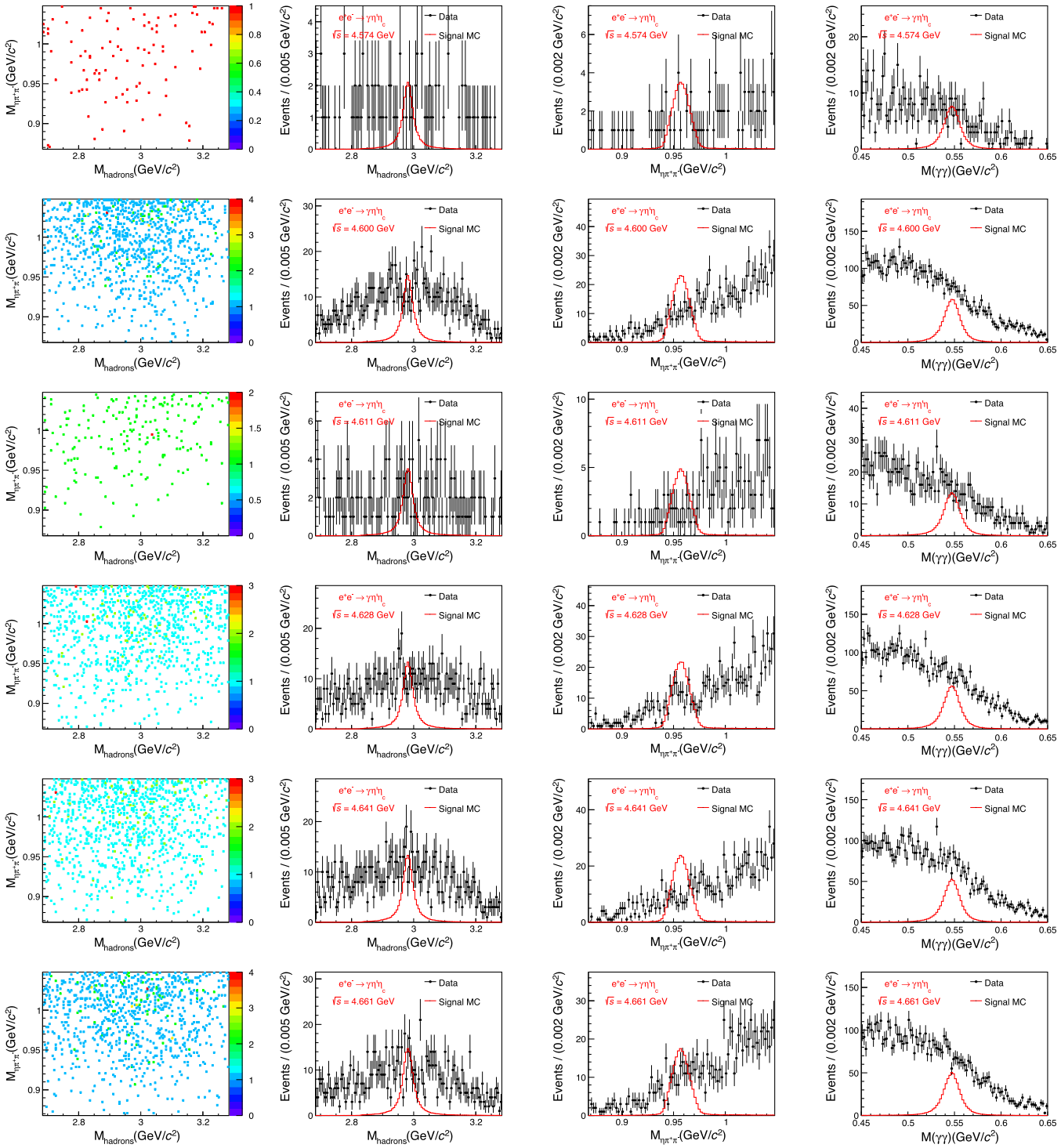


FIG. 12. The distributions of (left) $M_{\rm hadrons}$ versus $M_{\eta\pi^+\pi^-}$, (middle left) $M_{\rm hadrons}$, (middle right) $M_{\eta\pi^+\pi^-}$, and (right) $M_{\gamma\gamma}$ for $e^+e^- \to \gamma\eta'\eta_c$ candidate events. The rows show the distributions at $\sqrt{s} = 4.574$–4.661 GeV.

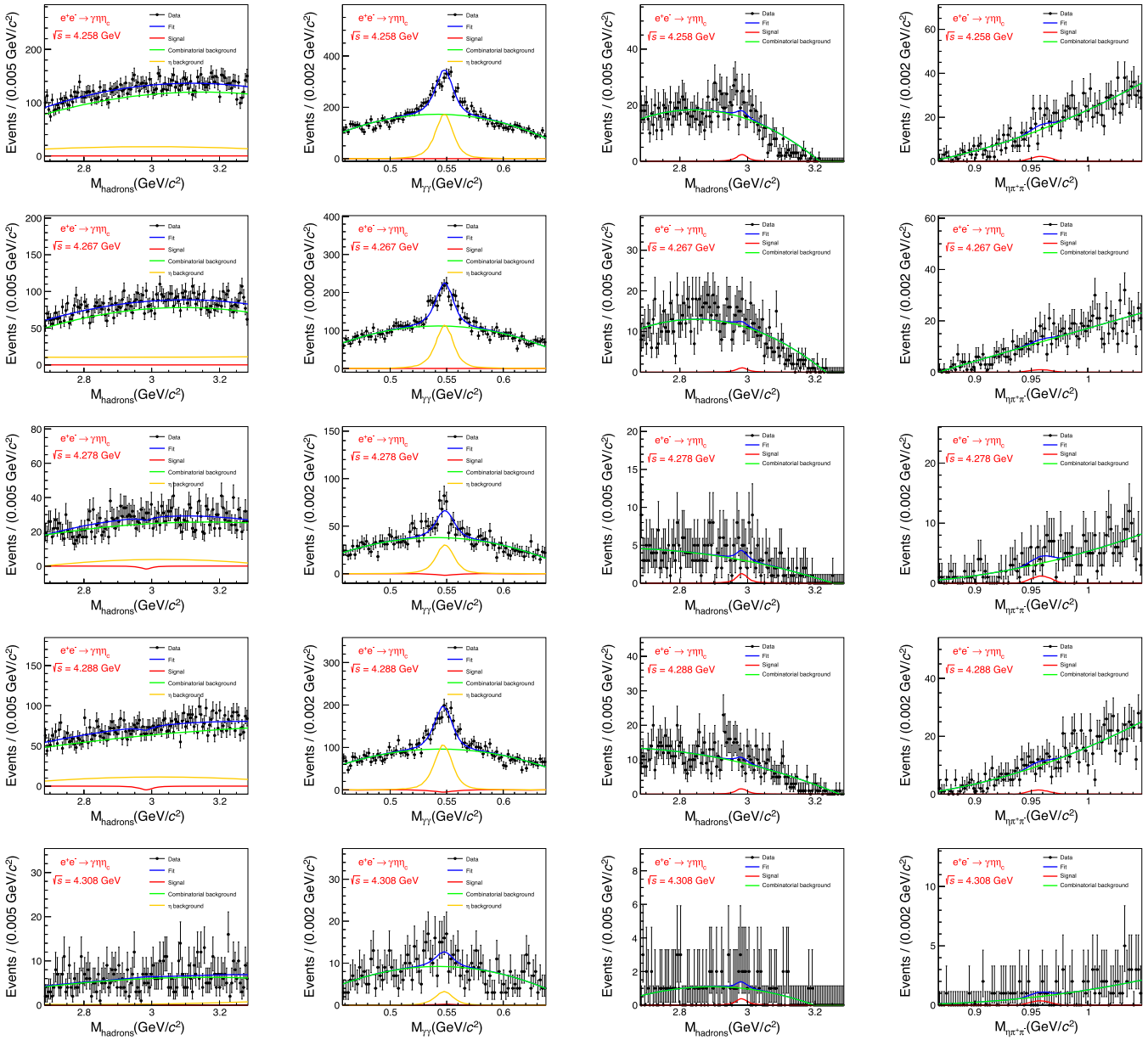


FIG. 13. Fits to the invariant mass distributions of (left) $M_{\rm hadrons}$ and (middle left) $M_{\gamma\gamma}$ for $e^+e^- \to \gamma\eta\eta_c$ candidate events, and (middle right) $M_{\rm hadrons}$ and (right) $M_{\eta\pi^+\pi^-}$ for $e^+e^- \to \gamma\eta'\eta_c$ candidate events. The rows show the distributions at $\sqrt{(}s) = 4.258$–4.308 GeV.

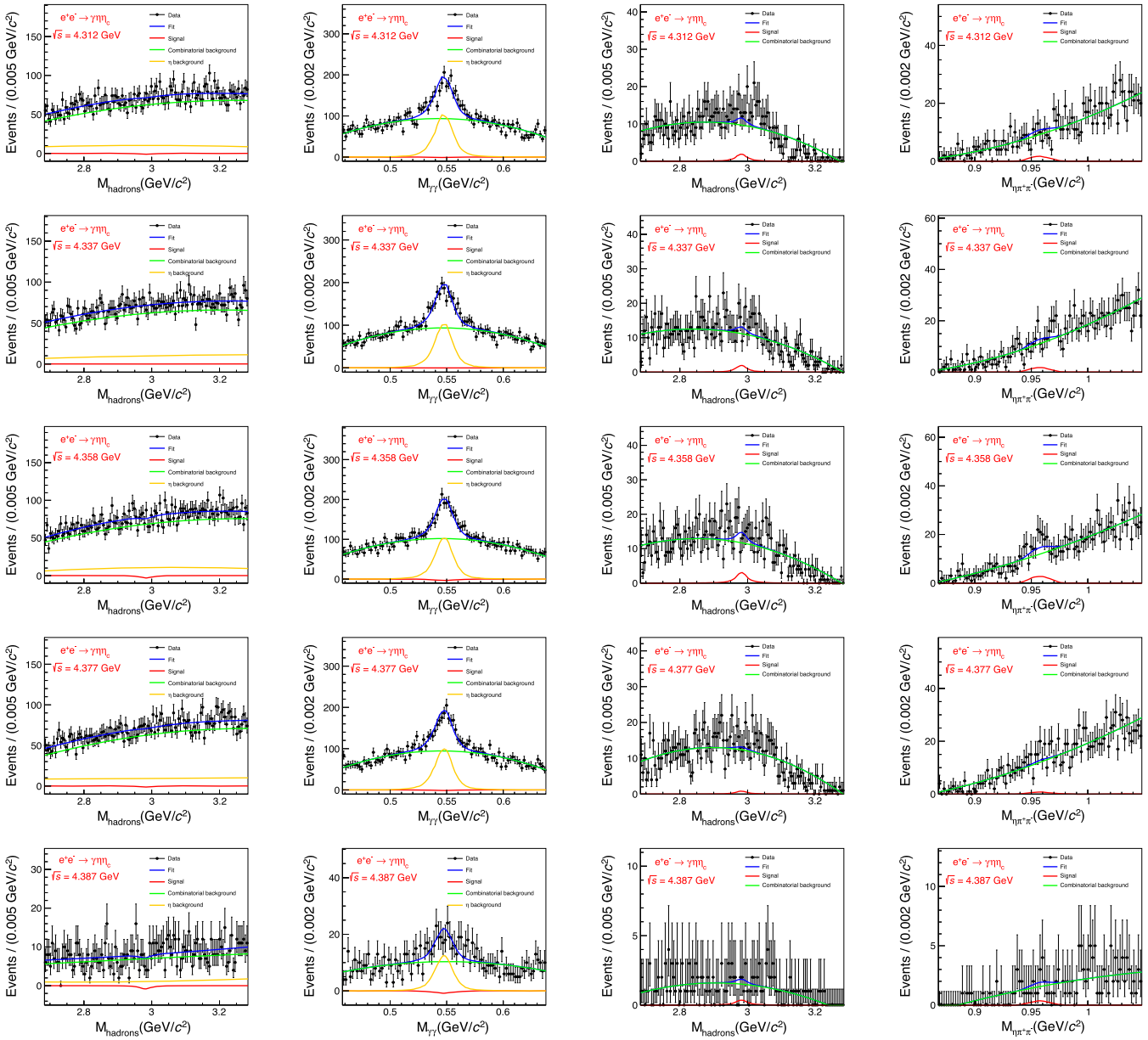


FIG. 14. Fits to the invariant mass distributions of (left) $M_{\rm hadrons}$ and (middle left) $M_{\gamma\gamma}$ for $e^+e^- \to \gamma\eta\eta_c$ candidate events, and (middle right) $M_{\rm hadrons}$ and (right) $M_{\eta\pi^+\pi^-}$ for $e^+e^- \to \gamma\eta'\eta_c$ candidate events. The rows show the distributions at $\sqrt{(s)} = 4.312$–4.387 GeV.

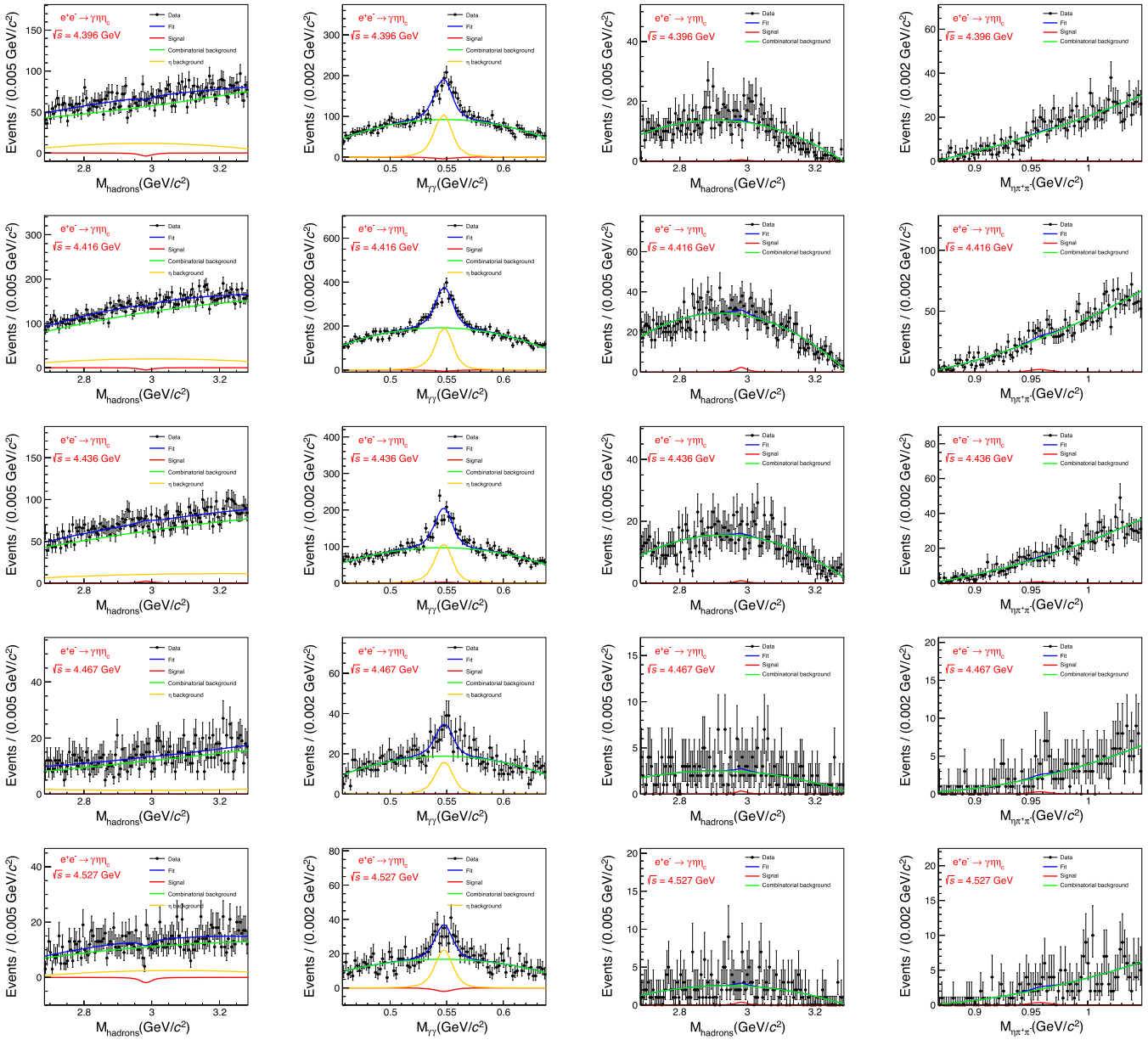


FIG. 15. Fits to the invariant mass distributions of (left) M_{hadrons} and (middle left) $M_{\gamma\gamma}$ for $e^+e^- \to \gamma\eta\eta_c$ candidate events, and (middle right) M_{hadrons} and (right) $M_{\eta\pi^+\pi^-}$ for $e^+e^- \to \gamma\eta'\eta_c$ candidate events. The rows show the distributions at $\sqrt{(s)} = 4.396$–4.527 GeV.

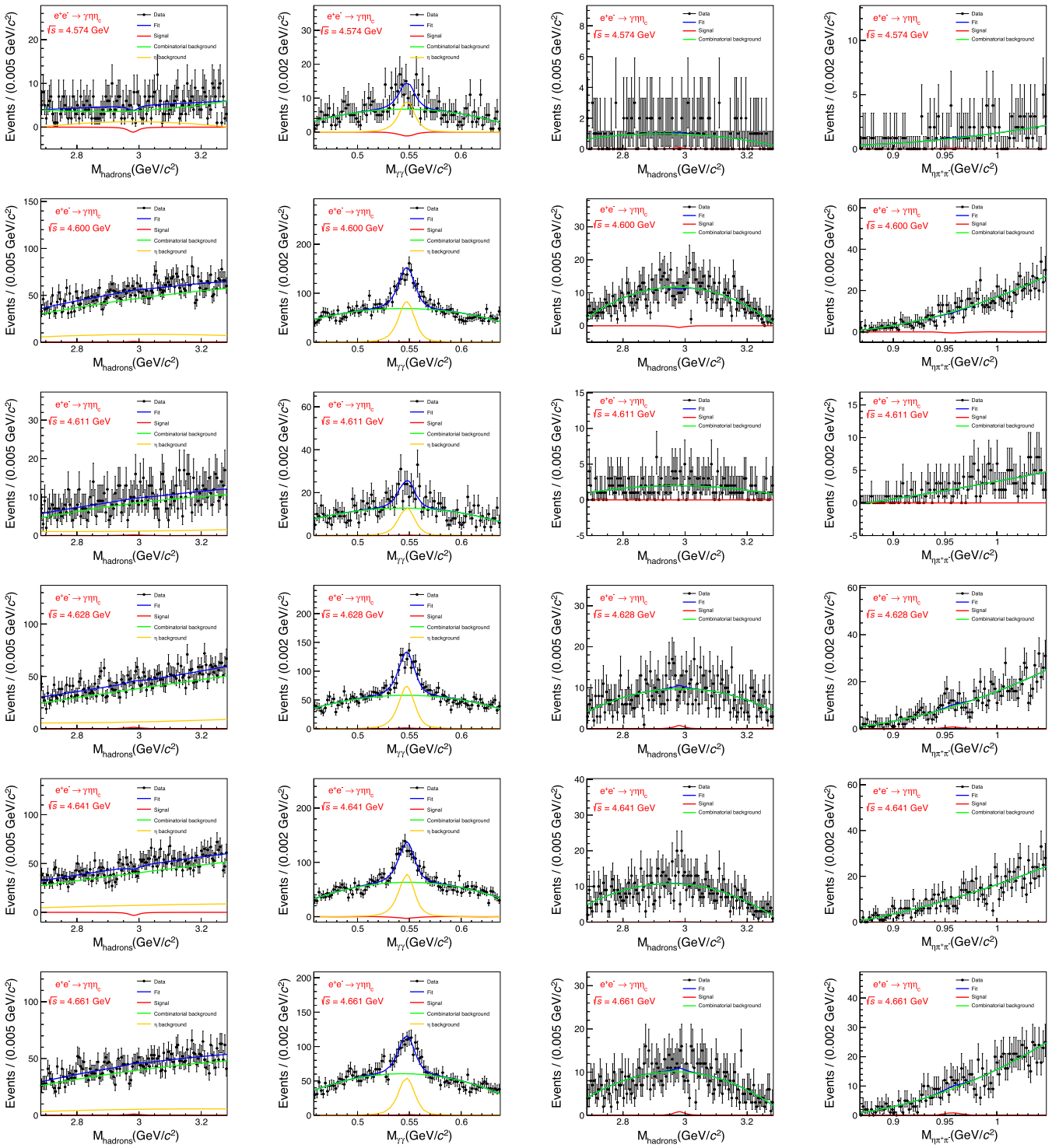


FIG. 16. Fits to the invariant mass distributions of (left) $M_{\rm hadrons}$ and (middle left) $M_{\gamma\gamma}$ for $e^+e^- \to \gamma\eta\eta_c$ candidate events, and (middle right) $M_{\rm hadrons}$ and (right) $M_{\eta\pi^+\pi^-}$ for $e^+e^- \to \gamma\eta'\eta_c$ candidate events. The rows show the distributions at $\sqrt{(}s) = 4.574$–4.661 GeV.

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